Information in Sequential Evaluations: the Good and the Bad

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- Many risky opportunities are offered sequentially to multiple parties until one takes it:
 - The seller of an asset can contact many interested buyers
 - Consumers home buyers have many banks to apply to for credit
 - Entrepreneurs contact many VCs or angel investors for (seed) funding
- Whoever gets an offer must evaluate whether opportunity is profitable or not

So: more information \longrightarrow better judgements of opportunity \longrightarrow better off evaluators?

• But: the evaluators also face an adverse selection problem:

How many were offered and rejected the opportunity before it was my turn?

Information shapes adverse selection:

Maybe: more information \longrightarrow more adverse selection $\stackrel{??}{\longrightarrow}$ worse off evaluators?

When does more information leave evaluators better off? (read: improve selection quality)

Important policy question, one example is credit scoring in banking.

- Banks want better statistical scoring models for competitiveness and quality lending:
 - Do not necessarily know why & how models work: neural networks, SVMs...
- Regulators want them to have & use better information, too!

Basel II: allowed Internal Ratings Based systems instead of Standardised Scoring to:

"provide a more risk-sensitive approach to measuring credit risk"

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Basel III after the subprime mortgage crisis:

"CVA is a complex risk ... cannot be modelled by banks in a robust and prudent manner. The revised framework removes the use of an internally modelled approach ..."

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Important policy question, one example is credit scoring in banking.

- Banks want better statistical scoring models for competitiveness and quality lending:
 - Do not necessarily know why & how models work: neural networks, SVMs...
- Regulators want them to have & use better information, too! But sometimes not!

Banks disagree with Basel III... for the same reason:

"[Internal assessments] by banks allow for the most accurate measurement of risk ... Relying on regulators' assessments ... will be rough approximations at best ... a major step backwards"

Kenneth Bentsen, CEO of Global Financial Markets Association

The Model

- APPLICANT with unknown quality $\theta \in \{L, H\}$ seeks approval from one evaluator.
 - Prior belief $\rho \in (0,1)$ that applicant is **born** with *High* quality.
- He sequentially visits $n \ge 2$ EVALUATORS, at random order τ .
 - τ is a permutation of $\{1,2,...,n\}$, chosen **privately** and **uniformly at random** by applicant.
- EV approves \longrightarrow payoff $\mathbb{1}\left\{\theta=H\right\}-c$, $c\in(0,1)$. Game ends, other EV.s get 0 payoff. EV rejects \longrightarrow 0 payoff. Applicant keeps applying. If no EV left \rightarrow game ends.

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- EVs do not know θ or τ . But: receive private IID signals x about quality θ :

$$x \in \{s_1, s_2, ..., s_m\} \subset [0, 1] \qquad \quad x \mid heta \stackrel{ ext{IID}}{\sim} p_{ heta} \qquad \quad s_i = rac{p_H(s_i)}{p_H(s_i) + p_L(s_i)} < s_{i+1}$$

- Equilibrium: symmetric strategy and interim belief profile (σ^*, ψ^*) for EVs such that:
 - $\psi^* = \mathbb{P}\left(\theta = H \mid \text{applicant visited me}\right)$ is *consistent* with strategy profile σ^*
 - $\sigma^*: \{s_1, s_2, ..., s_m\} \to [0, 1]$ optimal given ψ^* ; approve when $\mathbb{P}\left(\theta = H \mid x, \psi\right) > c$

Main Question and Takeaway

How does more information affect evaluators' equilibrium payoffs?

- Synonymous to **selection quality**: \uparrow eqm. payoffs when \downarrow false positives & negatives.
- Main problem: More information affects adverse selection (ψ^*). This indirect effect might backfire on selection quality.
- Main result: Characterise effect of arbitrary Blackwell improvements of EVs signals.
- Main takeaway: Depends on the kind of improvement. Roughly:
 - † approval confidence: good!
 † rejection confidence: eventually bad
 affect different applicants
 have different payoff effects

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affect different applicants \downarrow have different payoff effects

- Giving EVs information about **order** au
- EV makes take-it-or-leave-it price offer to applicant
- EVs compete on application costs

ask me after talk!

- Prior belief ρ that applicant is born with $\theta = H$ is a primitive.
- Interim belief $\psi = \mathbb{P}(\theta = H \mid \text{applicant visited me})$ is **endogenous**:
 - What is the chance applicant visited me after k rejections?
 - What do those rejections mean about his quality?
- ψ is *consistent* with the strategy σ for all evaluators, iff:

$$\psi = \frac{\rho \times \sum\limits_{k=1}^{n} r_{H}(\sigma)^{k}}{\rho \times \sum\limits_{k=1}^{n} r_{H}(\sigma)^{k} + (1-\rho) \times \sum\limits_{k=1}^{n} r_{L}(\sigma)^{k}} \quad \text{where } r_{\theta}(\sigma) = 1 - \sum\limits_{i=1}^{m} p_{\theta}(s_{i})\sigma(s_{i})$$

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$$\text{prob. High quality visit} \quad \text{prob. Low quality visit}$$

• Endogeneity means existence, number, or properties of equilibria are not automatic.

Proposition

Let $p_H \neq p_L$. The set of equilibrium strategies is non-empty and compact, and pointwise totally ordered. Furthermore:

- **1** all equilibrium strategies are monotone; $\sigma^*(s_i) > 0$ implies $\sigma^*(s_{i+1}) = 1$.
- 2 all equilibria exhibit adverse selection : $\psi^* \leq \rho$.
- Compact and totally ordered → we can talk about:
 - the highest (most embracive) equilibrium,
 - the *lowest* (most selective) equilibrium.

• (the sum of) Evaluators' equilibrium payoffs:

$$\Pi(\sigma) := \rho \times (1 - c) \times \mathbb{P}$$
(eventually approved $\mid \theta = H, \sigma) +$
 $-(1 - \rho) \times c \times \mathbb{P}$ (eventually rejected $\mid \theta = L, \sigma)$

- What do selective and embracive equilibria mean for payoffs?
- Different virtues: $selective \rightarrow filter\ Low\ quality\ approvals\ but\ miss\ out\ High\ quality$ $embracive \rightarrow secure\ High\ quality\ but\ overlook\ Low\ quality\ approvals$
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Proof Sketch:

- Take eqm. strategy σ^* , and consider marginally more embracive σ^{ε} : $||\sigma^{\varepsilon} \sigma^*|| = \varepsilon$
- Fix the signals all EVs would see if app. visited them all: $\{x_1, x_2, ..., x_n\}$.
- Only app. whose outcome changes: rejected by all under σ^* , approved by some under σ^{ε} .
- If ε is small, he was rejected by all under σ^* , approved by one under σ^{ε} .
- Bad news: that last evaluator gets negative expected payoffs
 - In eqm., would like to reject him under suspicion of adverse selection
 - Approving him when he is the most adversely selected cannot help

Proposition

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Proof Sketch:

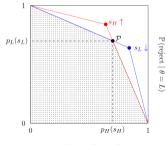
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- Bad news: that last evaluator gets negative expected payoffs
- Last step: payoffs are **single crossing** in embraciveness; where $\sigma'' > \sigma' > \sigma$

$$\Pi(\sigma') \leq \Pi(\sigma) \implies \Pi(\sigma'') \leq \Pi(\sigma')$$

Information and Equilibrium Payoffs

$$\begin{split} \Pi(\sigma) &:= \rho \times (1-c) \times \mathbb{P} \text{ (eventually approved } \mid \theta = H, \sigma) + \\ &- (1-\rho) \times c \times \mathbb{P} \text{ (eventually rejected } \mid \theta = L, \sigma) \end{split}$$

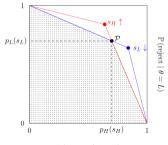
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- With *one* evaluator, **Blackwell more informative** signal $\stackrel{(\leftrightharpoons)}{\Longrightarrow}$ \uparrow payoffs for all c, ρ
- Reason: affords lower false positives & negatives
- Example: binary signal. $S = \{s_L, s_H\}$. A Blackwell improvement is $\downarrow s_L$ or $\uparrow s_H$.



Information and Equilibrium Payoffs

• What could go wrong? Let's rewrite EV i's payoff $\pi_i \left(= \frac{\Pi}{n} \right)$:

```
\pi_i(\sigma) = \mathbb{P} 	ext{ (applicant visits } i) 
 \times \left[ \psi \times (1-c) \times \mathbb{P} \left( i \text{ approves } \mid \theta = H \right) + (1-\psi) \times (-c) \times \mathbb{P} \left( i \text{ approves } \mid \theta = L \right) \right]
```

- The blue adverse selection terms are outside EV i's control: depend on others' strategies
- EVs do not take adverse selection they impose to others into account
- Maximising individual selection quality eq maximising **overall** selection quality

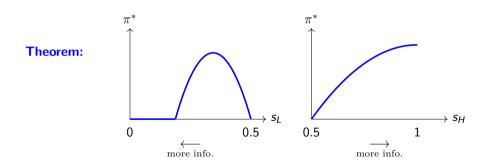
- Start from binary signals: main intuition and building block to full characterisation
- $x \in S = \{s_L, s_H\}$ more informative when $s_L \downarrow$: stronger evidence for *Low* quality and $s_H \uparrow$: stronger evidence for *High* quality

Theorem

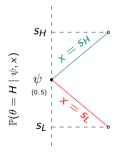
Let EVs have a binary signal, $x \in S = \{s_L, s_H\}$. Their equilibrium payoffs in the most selective (embracive) equilibria are weakly:

- increasing with stronger evidence for $\theta = H \ (\uparrow s_H)$,
- increasing with stronger evidence for $\theta = L \ (\downarrow s_L)$ when s_L is above a threshold,
- decreasing with stronger evidence for $\theta = L \ (\downarrow s_L)$ when s_L is below that threshold.

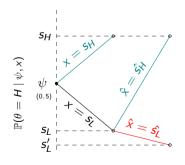
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- Consider decreasing s_L marginally. How to implement this Blackwell improvement?
- Fix strategies [handle in actual proof]: approve with high signal & reject with low signal

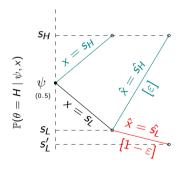


- Consider decreasing s_L marginally. How to implement this Blackwell improvement?
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- Construct an auxiliary signal \hat{x} .



- Like before, fix signal pairs (x, \hat{x}) all EVs would see.
- We created marginal admits: rejected by all in old signal structure, approved by some in new.
- All info. on marginal admits' quality \longrightarrow how many $\hat{x} = \hat{s_H}$ signals.

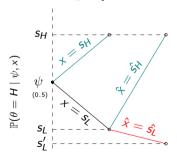
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- We created marginal admits: rejected by all in old signal structure, approved by some in new.
- All info. on marginal admits' quality \longrightarrow how many $\hat{x} = \hat{s_H}$ signals. **Answer: only one!**
- For marginal decrease in s_L , $\mathbb{P}(\hat{x} = \hat{s_H}) \propto \varepsilon \to 0$.
- Multiple $\hat{x} = \hat{s_H}$ has negligible probability.

Sketch Proof:

- Consider decreasing s_L marginally. How to implement this Blackwell improvement?
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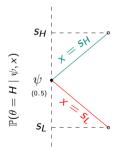


• Whether the marginal admit is profitable:

$$\underbrace{\frac{\rho}{1-\rho}}_{\text{prior}} \times \underbrace{\left(\frac{s_L}{1-s_L}\right)^{n-1}}_{n-1 \text{ low signals}} \times \underbrace{\frac{s_H}{1-s_H}}_{\text{the only high signal}} \lesssim \underbrace{\frac{c}{1-c}}_{\text{approval cos}}$$

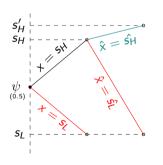
 Lesson: Whenever there is a threat of adverse selection, stronger evidence for θ = L hurts.

- Now consider increasing s_H marginally. How to implement this Blackwell improvement?
- Fix strategies as before: approve with high signal & reject with low signal



Sketch Proof:

- Now consider increasing s_H marginally. How to implement this Blackwell improvement?
- Fix strategies as before: approve with high signal & reject with low signal
- Construct an auxiliary signal \hat{x} .



- This time marginal rejects: approved by some before, rejected by all now.
- All EVs must have seen low signals.
- Marginal reject is always good to push out:

$$\underbrace{\frac{\rho}{1-\rho}}_{\text{prior}} \times \underbrace{\left(\frac{s_L}{1-s_L}\right)^n}_{n \text{ low signals}} < \underbrace{\frac{c}{1-c}}_{\text{approval cos}}$$

[actual proof: show this is the only relevant case]

- Main lesson from Theorem:
 - s_H ↑ benefits EVs → marginal rejects
 - $s_L \downarrow$ hurts EVs when s_L is below a threshold \longrightarrow marginal admits
- A candidate for the threshold came from sketch proof:

$$\underbrace{\frac{\rho}{1-\rho}}_{\text{prior}} \times \underbrace{\left(\frac{s_L^{\text{as}}}{1-s_L^{\text{as}}}\right)^{n-1}}_{n-1 \text{ low signals}} \times \underbrace{\frac{s_H}{1-s_H}}_{\text{the only high signal}} = \underbrace{\frac{c}{1-c}}_{\text{approval cos}}$$

- s_I^{as} : strongest evidence for $\theta = L$ where adverse selection is not a threat.
- Marginal admit hurts when $s_L < s_L^{as}$.

- The actual threshold depends more subtly on equilibrium dynamics.
- EVs might be stuck in eqa. where all applicants are approved when info. is too weak:

$$\underbrace{\frac{\rho}{1-\rho}}_{\text{prior}} \times \underbrace{\left(\frac{\mathbf{s}_{L}^{\text{mute}}}{1-\mathbf{s}_{L}^{\text{mute}}}\right)}_{\text{one low signal}} = \underbrace{\frac{c}{1-c}}_{\text{approval cost}}$$

when $s_L \geq s_L^{\mathrm{mute}}$, always an eqm: approve all o no adverse selection o approve all

Proposition

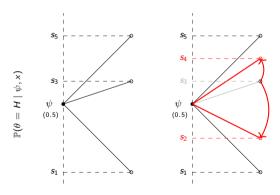
Let EVs have a binary signal $x \in \{s_L, s_H\}$. The threshold below which lower s_L weakly decreases their equilibrium payoffs is:

- $s_L^{as} \ge \min\{s_L^{mute}, s_L^{as}\}$ for the most embracive equilibrium.
- $s_L^{\rm as} \geq s_L^\dagger \geq \min\left\{s_L^{\rm mute}, s_L^{\rm as}\right\}$ for the most selective equilibrium.

- In many settings, EVs of risky opportunities have richer signal structures:
 - Analyst reports for stock traders: "Strong Sell", "Sell", "Buy", "Strong Buy".
 - Consumer credit scoring: multi-class scorecard might only eventually be aggregated to binary.
- Important to generalise from binary to Blackwell improvements of any discrete signal.
- Previously: auxiliary signal spreads belief further after initial $x = s_H$ or $x = s_L$
- Now generalise this idea: **local mean preserving spreads**.

Take two signals, $x \mid \theta \stackrel{\textit{IID}}{\sim} p_{\theta}$ and $x' \mid \theta \stackrel{\textit{IID}}{\sim} p'_{\theta}$. Joint support $S \cup S' = \{s_1, s_2, ..., s_M\}$.

x' differs from x by a local MPS at s_i if:



- p_{θ} places no mass at s_{i-1} or s_{i+1} .
- p'_{θ} places no mass at s_i .
- p_{θ} and p'_{θ} place equal mass to all points except $\{s_{i-1}, s_i, s_{i+1}\}.$
- p and p' have equal normalised means:

$$\sum_{j=1}^{M} s_{j} \times \left(\frac{p_{L}(s_{j}) + p_{H}(s_{j})}{2}\right) = \sum_{j=1}^{M} s_{j} \times \left(\frac{p'_{L}(s_{j}) + p'_{H}(s_{j})}{2}\right)$$

Local mean preserving spreads *characterise* Blackwell improvements:

Remark

If x' differs from x by a local MPS, x' is *Blackwell more informative than* x. Furthermore, if x' is *Blackwell more informative than* x, there is a finite sequence $x_1, x_2, ..., x_k$ such that:

- $x_1 = x$ and $x_k = x'$,
- x_{i+1} differs from x_i by a local MPS.
- Only slight refinement of classic Rothschild and Stiglitz, 1970 result.
- I will characterise the effect of a local MPS.

One more definition before result:

For a fixed signal x and strategy σ , adverse selection poses a threat at signal s if:

$$\underbrace{\frac{\rho}{1-\rho}}_{\text{prior}} \times \underbrace{\left(\frac{r_{H}(\sigma)}{r_{L}(\sigma)}\right)^{n-1}}_{n-1 \text{ past rejections}} \times \underbrace{\frac{s}{1-s}}_{\text{last signal is } s} \leq \underbrace{\frac{c}{1-c}}_{\text{approval cost}}$$

Theorem

Let x' differ from x by a local MPS at s_i . EVs' expected payoffs under the most embracive (selective) equilibrium are:

- **1** weakly higher under x' if $x = s_i$ leads to approvals under σ ; $\sigma(s_i) = 1$,
- 2 weakly lower under x', if:
 - 1 $x = s_i$ leads to rejections under σ ; $\sigma(s_i) = 0$, and
 - 2 adverse selection poses a threat at signal s_{i+1} , for signal structure x and strategy σ .

- Local MPS necessary, helps pin down equilibrium response to spread.
- Knowing when a spread must be harmful requires knowing equilibrium structure
- Unpleasant: WHY?
- We can offer a stronger sufficient condition that relies only on the local MPS performed:

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a fortiori:
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