# Committees

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COMMENTS ON!

#### Abstract

Orange notes: for Ian & Dan.

Green notes: for me (but Ian & Dan should feel free to chime in!).

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## 1 Introduction

#### 2 The Model

A committee of N members,  $m_1, ..., m_N$ , wish to decide whether to enact or block a policy. The benefit a member  $m_i$  obtains from enacting the policy depends on an unknown state of the world,  $\omega \in \{\omega_0, \omega_1\}$ . When the state is favourable,  $\omega = \omega_1$ , she obtains a payoff of  $u_i \geq 0$  from enacting the policy. When the state is unfavourable,  $\omega = \omega_0$ , she incurs a payoff loss of 1 instead. Blocking the policy, in contrast, yields her a payoff of 0 in either state. There is also a lobbyist outside the committee. He prefers the policy to be enacted regardless of the state.

At the outset of the game, the lobbyist and committee members share the prior belief that  $\omega = \omega_1$  with probability  $p \in [0,1]$ . The lobbyist can then provide additional public information about the state. He does so by committing to perform and publicly disclose the outcome of an (Blackwell) experiment of his choosing. Formally, an experiment is comprised of a measurable space  $(X, \mathcal{X})$  and, for each possible state  $\omega_k$ , a probability measure  $P_k$  over it. Upon observing the outcome of the lobbyist's experiment, players use Bayes Rule to update their prior belief p that  $\omega = \omega_1$  to an interim belief  $r \in [0, 1]$ .

I follow a belief-based approach<sup>1</sup> and model the lobbyist as directly choosing the distribution  $\mu_l$  his experiment will induce over interim beliefs. The distribution  $\mu_l$  must be Bayes plausible; i.e.,  $\mu_l \in \Delta_p([0,1])$ , where:

$$\Delta_{p}\left(\left[0,1\right]\right):=\left\{ \mu\in\Delta\left(\left[0,1\right]\right):\int_{0}^{1}rd\mu(r)=p\right\} \qquad \qquad \Delta\left(\left[0,1\right]\right):=\underset{p\in\left[0,1\right]}{\cup}\Delta_{p}\left(\left[0,1\right]\right)$$

After the lobbyist reveals the outcome of his experiment, each committee member acquires additional information about the state. She does so by choosing an additional experiment whose outcome she observes. Committee members acquire this additional information privately: neither the experiment  $m_i$  chooses to perform nor its outcome are disclosed to anyone.

Following the outcome of her experiment,  $m_i$  updates her interim belief r to a posterior belief  $q_i \in [0,1]$  that  $\omega = \omega_1$ . Again, I model each member  $m_i$  as choosing the distribution  $\mu_i(. \mid r) \in \Delta_r([0,1])$  her experiment will induce over her posterior beliefs, given her interim belief r. Conditional on the true state  $\omega$ , the outcomes of members' chosen experiments are independent.

Producing and providing public information is costless for the lobbyist. In contrast, acquiring private information is costly for committee members:  $m_i$  must pay a cost  $C_i(\mu)$  to observe the outcome of an experiment which induces the distribution  $\mu$  over her possible posterior beliefs. The

meaningless
to wonder
about corr.
between
exp.s—info.
acq. is private? introducing correlation only
strengthens result,

though.

<sup>&</sup>lt;sup>1</sup>See Kamenica and Gentzkow 2011 and Caplin and Dean 2013.

cost function  $C_i : \Delta([0,1]) \to \mathbb{R}^+$  is uniformly posterior separable<sup>2</sup>; i.e., there is a convex function  $c_i : [0,1] \to \mathbb{R}^+$  whose effective domain contains (0,1), such that<sup>3</sup>:

i assume

 $\infty - \infty = \infty$ 

check if this

with CDL

$$C_i(\mu) := \begin{cases} 0 & \text{for } \mu = \{\delta_0, \delta_1\} \\ \int c_i(q) d\mu(q) - c_i \left( \mathbb{E}_{\mu}[q] \right) & \text{otherwise} \end{cases}$$

Finally, each committee member casts a private vote into a voting mechanism. A voting mechanism is a tuple  $\left(D, \{V_i\}_{i=1}^N, \{\mathcal{V}_i\}_{i=1}^N\right)$  where  $V_i \ni v_i$  is a set of possible votes each member  $m_i$  may cast,  $\mathcal{V}_i$  is the  $\sigma$ -algebra over  $V_i$ , and the decision rule  $D: \underset{i=1}{\overset{N}{\times}} V_i \to [0,1]$  is a measurable mapping from the space of possible vote profiles to a probability that the policy is enacted.

I focus on the lobbyist-preferred perfect Bayesian equilibrium (hereon, simply "equilibrium") of this game for any given voting mechanism. An equilibrium consists of:

- 1. a voting strategy  $\{\tau_i^*(. \mid q, r)\}_{(q,r) \in [0,1]^2}$  where  $\tau_i^*(. \mid q, r) \in \Delta(V_i)$  for each member  $m_i$ ,
- 2. an information strategy  $\{\mu_i^*(. \mid r)\}_{r \in [0,1]}$  where  $\mu_i^*(. \mid r) \in \Delta_r([0,1])$  for each member  $m_i$ , and
- 3. a strategy  $\mu_l^* \in \Delta_p([0,1])$  for the lobbyist

such that under this fixed voting mechanism:

1. Given other members' strategies, member  $m_i$ 's voting strategy maximises her expected payoff at any pair of interim and posterior beliefs (r, q) she may hold:

i don't think i am missing off-path considerations..?

$$v_{i} \in \operatorname{supp} \tau_{i}^{*}(. \mid q, r)$$

$$\implies v_{i} \in \operatorname{argmax} \int_{[0,1]^{N-1}} [\mathbb{P}_{r,q_{1},\dots,q_{N}}(\omega_{1}) \times (u_{i}+1) - 1]$$

$$\times \left\{ \int_{V_{-i}} D(v, \mathbf{v_{-i}}) \tau_{-i}^{*}(d\mathbf{v_{-i}} \mid r, \mathbf{q_{-i}}) \right\} \frac{\mu^{*}(q, d\mathbf{q_{-i}} \mid r)}{\int_{Q_{-i}} \mu^{*}(q, \mathbf{q_{-i}} \mid r) d\mathbf{q_{-i}}}$$

where:

- $(V_{-i}, \mathcal{V}_{-i}) := \begin{pmatrix} \times V_j, \times \mathcal{V}_j \\ j \neq i & j \neq i \end{pmatrix}$  is the space of vote profiles members except  $m_i$  may submit, with  $\mathbf{v}_{-i} \in V_{-i}$ .
- $\tau_{-i}^*(. \mid r, \mathbf{q}_{-i}) := \underset{j \neq i}{\times} \tau_j^*(. \mid ; r, q_j)$  is the product measure over this space induced by those members' voting behaviour, given the vector  $\mathbf{q}_{-i} \in V_{-i}$  of their posterior beliefs.

surability; votes
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<sup>&</sup>lt;sup>2</sup>See, for instance, Caplin, Dean, and Leahy 2022.

<sup>&</sup>lt;sup>3</sup>For notational convenience, I assume that  $\infty - \infty = \infty$ .

- $\mu^*(. \mid r) := \underset{i=1}{\overset{N}{\times}} \mu_i^*(. \mid r)$  is the probability measure over the space of committee members' joint posterior beliefs induced by the information those members acquire, and
- $\mathbb{P}_{r,q_1,\ldots,q_N}(\omega_1)$  is the probability that  $\omega=\omega_1$  given members' interim and posterior beliefs:

$$\mathbb{P}_{q_1,\dots,q_N}(\omega_1) := \left(\mathcal{L}(r) \times \prod_{j=1}^N \frac{\mathcal{L}(q_j)}{\mathcal{L}(r)}\right) \times \left(1 + \mathcal{L}(r) \times \prod_{j=1}^N \frac{\mathcal{L}(q_j)}{\mathcal{L}(r)}\right)^{-1} \quad \text{where } \mathcal{L}(q) := \frac{q}{1-q}$$
This is expression.

tremely long..?

2. Given others' strategies, member  $m_i$ 's information strategy maximises her expected payoff at any interim belief r she may hold:

$$\mu_{i}^{*}(. \mid r) \in \underset{\mu \in \Delta_{r}[0,1]}{\operatorname{argmax}} \int \left[ \mathbb{P}_{q_{1},\dots,q_{N}}(\omega_{1}) \times (u_{i}+1) - 1 \right] \times \left\{ \int_{V_{i}} \int_{V_{-i}} D(v_{i}, \mathbf{v_{-i}}) \tau_{-i}^{*}(d\mathbf{v}_{-i} \mid r, q) \tau_{i}^{*}(dv_{i} \mid r, q) \right\} \frac{\mu(q_{i}, d\mathbf{q_{-i}} \mid r)}{\int_{Q_{-i}} \mu(q_{i}, \mathbf{q_{-i}} \mid r) d\mathbf{q_{-i}}} \mu_{i}(dq_{i} \mid r) - C_{i}\left(\mu\right)$$

where  $\mu(. \mid r) := \underset{j \neq i}{\times} \mu_j^*(. \mid r) \times \mu$  for  $m_i$ 's chosen distribution  $\mu$ .

3. Players' strategies maximise the probability that the policy is enacted among all strategy profiles which satisfy the two conditions above.

## Dominant Voting Mechanisms

I call a voting mechanism *dominant* if it gives rise to an equilibrium that yields:

- i. a (weakly) higher probability that the policy is blocked when  $\omega = \omega_0$ ,
- ii. a (weakly) higher probability that the policy is enacted when  $\omega = \omega_1$ , and

iii. a (weakly) lower expected cost of information acquisition for each committee member compared to any equilibrium under any other voting mechanism. If a dominant voting mechanism exists, it yields (weakly) higher equilibrium payoffs for all committee members compared to any other mechanism.

This paper asks whether such a mechanism indeed exists.

can we ensure this exists? does it matter for me?

if multiple exist there, the one with lowest info

### 3 Equilibria Under Dictatorships

A dictatorship—appointing a single member whose vote fully determines whether the policy is enacted—is among the simplest voting mechanisms the committee may adopt.

**Definition 1.** A voting mechanism  $\left(\overset{\bullet}{D_i}, \{V_j\}_{j=1}^N, \{V_j\}_{j=1}^N\right)$  is an  $m_i$ -dictatorship, if:

- 1.  $V_i = \{0, 1\}$ , and  $V_j$  is a singleton for all  $j \neq i$ .
- 2.  $D_i(\mathbf{v}) = v_i$  for any profile of votes  $\mathbf{v} = (v_1, ..., v_N)$ .

Despite dictatorships' simplicity, the main result of this paper (Theorem 1) establishes that there exists a member whose dictatorship is a dominant voting mechanism. This section sets the ground for this result by characterising the equilibrium a dictatorship induces.

"up to isomorphism", but how to say this nicer?

**Lemma 1.** In the equilibrium of an  $m_i$ -dictatorship:

- 1.  $\tau_{i;r,q}^* = \delta_{\mathbb{I}\{q \geq (1+u_i)^{-1}\}}$  for all interim beliefs  $r \in [0,1]$ .
- 2.  $\mu_{i;r}^*$  is the unique distribution for which supp  $\mu_{i;r}^* \subseteq \{\min\{r, \underline{q}_i^*\}, \max\{r, \overline{q}_i^*\}\}$ , for two threshold beliefs  $q_i^*$  and  $\overline{q}_i^*$ ,  $0 \le q_i^* \le \overline{q}_i^* \le 1$ .
- 3.  $\mu_l^*$  is the unique distribution for which supp  $\mu_l^* \subseteq \{0, \max\{p, \bar{q_i}^*\}\}$ .

Proof.

- 1. In an  $m_i$ -dictatorship, no vote except  $m_i$ 's of has any bearing on the outcome. So, the outcome may only reflect  $m_i$ 's posterior belief. Therefore,  $v_i \in \tau_{i;r,q}^*$  implies that  $v_i \in \arg\max_{v \in \{0,1\}} v \times [q \times (u_i + 1) 1]$ . This establishes that  $\tau_i^*(r, q_i) = \delta_{1\{q_i \ge (1 + u_i)^{-1}\}}$ .
- 2. Member  $m_i$  uses her information to decide between two possible votes; so, we can without loss of generality assume  $|\sup \mu_{i;r}^*| \leq 2$  for all  $r \in [0,1]$ . Furthermore, since information acquisition is costly, any additional information she acquires must have decision-making value; i.e.,  $(1+u_i)^{-1} \in \text{conv}\left(\sup \mu_{i;r}^*\right)$  whenever  $|\sup \mu_{i;r}^*| = 2$ . Lastly, note that Theorem 1 in Caplin, Dean, and Leahy 2022 implies that  $m_i$ 's strategy must be Locally Posterior Invariant since  $C_i$  is uniformly posterior separable; i.e., for any  $\tilde{r} \in \text{conv}\left(\sup \mu_{i;r}^*\right)$ ,  $\mu_{i;\tilde{r}}^*$  is the unique distribution such that  $\sup \mu_{i;\tilde{r}}^* = \sup \mu_{i;r}^*$ .

If  $m_i$  never acquires any information under the  $m_i$ -dictatorship; i.e.,  $\mu_{i;r}^* = \delta_r$  for all  $r \in [0,1]$ , we are done. Otherwise, for any r such that  $|\text{supp } \mu_{i;r}^*| = 2$ ,  $(1+u_i)^{-1} \in \text{conv } \left(\mu_{i;r}^*\right)$  implies that supp  $\mu_{i;r}^* = \text{supp } \mu_{i;(1+u_i)^{-1}}^*$ . Letting  $\{\underline{q}_i^*, \overline{q}_i^*\} := \text{supp } \mu_{i;(1+u_i)^{-1}}^*$  where  $\underline{q}_i^* \leq \overline{q}_i^*$ , we thus conclude:

add here
that these
two are outcome equivalent for the
lobbyist, so
also satisfy
lobbyistpreferred

- (a) for all  $r \in [\underline{q}_i^*, \overline{q}_i^*]$ ,  $\mu_{i;r}^*$  is the unique distribution such that  $\operatorname{supp} \mu_{i;r}^* = \{\underline{q}_i^*, \overline{q}_i^*\}$ .
- (b) for all  $r \notin [q_i^*, \bar{q}_i^*], \mu_{i:r}^* = \delta_r$ .

which proves our claim.

3. Given  $m_i$ 's equilibrium voting and information strategies, let  $\pi_{l;i}^*(r)$  be the equilibrium probability that the policy is enacted as a function of committee members' interim belief r. Further, let  $\hat{\pi_{l;i}}^*(r)$  be the concave envelope of this function. These two functions are then given by:

$$\pi_{l,i}^{*}(r) := \begin{cases} 0 & r \leq \underline{q}_{i}^{*} \\ \frac{r - \underline{q}_{i}^{*}}{\overline{q}_{i}^{*} - \underline{q}_{i}^{*}} & r \in [\underline{q}_{i}^{*}, \overline{q}_{i}^{*}] \\ 1 & r \geq \overline{q}_{i}^{*} \end{cases} \qquad \pi_{l,i}^{*}(r) := \begin{cases} \frac{r}{\overline{q}_{i}^{*}} & r \leq \overline{q}_{i}^{*} \\ 1 & r \geq \overline{q}_{i}^{*} \end{cases}$$

That  $\hat{\pi}_{l;i}^*(r)$  is indeed the concave envelope of  $\pi_{l;i}^*(r)$  can be easily verified by noting that any concave function which coincides with  $\pi_{l;i}^*$  at r=0 and  $r=\bar{q}_i^*$  must weakly lie above the function  $\hat{\pi}_{l;i}^*(r)$  on the interval  $[0,\bar{q}_i^*]$ .

By Kamenica and Gentzkow 2011, the condition  $\mathbb{E}_{\mu} \pi_{l;i}^*(.) = \hat{\pi_{l;i}}^*(p)$  is then sufficient for the optimality of  $\mu$  for the lobbyist. It is easily seen that the distribution  $\mu_l^*$  defined in Lemma 1 satisfies this condition.

Discuss this Lemma.

## 4 The Dominance of Dictatorships

**Definition 2.** Member  $m_i$  is the most-demanding member of the committee if  $\bar{q}_i^* = \max\{\bar{q}_1^*, \bar{q}_2^*, ..., \bar{q}_N^*\}.$ 

Discuss what makes a member most-demanding. Low  $u_i$  and "appropriately low" costs of acquiring information must interact.

**Theorem 1.** The dictatorship of the most demanding member is a dominant voting mechanism.

*Proof.* Where  $m_i$  is the most-demanding member, I use  $\overset{\bullet}{Q} := \bar{q}_i^*$  to simplify notation in the ensuing. I fix  $\left(\{V_j\}_{j=1}^N, \{\mathcal{V}_j\}_{j=1}^N, D\right)$  to be an arbitrary voting mechanism, and let  $\overset{\bullet}{D}$  denote the voting rule for the dictatorship of the most-demanding member.

I will use Claim 2 to establish the Theorem:

add the assumption that D must attain its min/max.

#### Claim 2. Any voting mechanism induces an equilibrium where committee members:

- (a) acquire no information for interim beliefs  $r \in \{0\} \cup [\overset{\bullet}{Q},1]$ ; i.e.,  $\mu_{1;r}^* = \ldots = \mu_{N;r}^* = \delta_r$  for such interim beliefs.
- (b) vote to maximise the probability that the policy is executed for interim beliefs  $r \geq \tilde{Q}$ , but to minimise it for r = 0; i.e.:

$$\mathbb{E}_{\tau_{1;r,r}^*,\dots,\tau_{N;r,r}^*} D(\mathbf{v}) = \begin{cases} \max_{\mathbf{v} \in V} D(\mathbf{v}) := \bar{D} & r \ge \tilde{Q} \\ \min_{\mathbf{v} \in V} D(\mathbf{v}) := \bar{D} & r = 0 \end{cases}$$

*Proof.* Assume that all members except  $m_i$  employ the asserted strategies. I will first show that the asserted strategies are a best response for  $m_i$ , in that case. I then show that, in the relevant subgames, there is no strategy profile that is (a) a mutual best response for all committee members, and (b) preferred by the lobbyist to those asserted above.

Now let  $\pi_i(q_i; r)$  be the payoff  $m_i$  expects under this voting mechanism given (i) the interim belief r, (ii) her posterior belief  $q_i$ , (iii) other members' strategies, and (iv) that she votes optimally at each posterior belief. Since other committee members acquire no private information, we have:

$$\pi_i(q_i; r) = \max_{\tau \in \Delta(V_i)} [q_i \times (1 + u_i) - 1] \times \int_{V_{-i}} \int_{V_i} D(v, \mathbf{v}_{-i}) \tau(dv) \tau^*_{-i; r, r}(d\mathbf{v}_{-i})$$

For  $q > (1 + u_i)^{-1}$ ,  $\pi_i(q; r)$  is strictly increasing in the probability that the policy is enacted. For  $q < (1 + u_i)^{-1}$ , it is strictly decreasing in the same probability. Thus, when  $q > (1 + u_i)^{-1}$ ,  $m_i$ 's optimal voting strategy must maximise the probability that the policy is enacted given others' voting strategies, but when  $q < (1 + u_i)^{-1}$ , it must minimise it. When  $q = (1 + u_i)^{-1}$ ,  $\pi_i(q_i; r) = 0$ ; so, any voting strategy is a best response.  $m_i$ 's equilibrium strategy must then be lobbyist-preferred one, and maximise the probability that the policy is enacted. This verifies Claim 2's assertion on optimal voting strategies, and gives:

$$\pi_i(q;r) = \begin{cases} \bar{D} \times [q \times (1+u_i) - 1] & q \ge (1+u_i)^{-1} \\ \underline{D} \times [q \times (1+u_i) - 1] & q < (1+u_i)^{-1} \end{cases}$$

whenever  $r \in \{0\} \cup [\overset{\bullet}{Q}, 1]$ .

When r = 0,  $\Delta_0([0,1]) = \delta_0$ ; so  $\mu_{i;0}^* = \delta_0$ . When  $r \geq \tilde{Q}$ , the strategy  $\mu_{i;r}^* = \delta_r$  delivers the highest probability that the policy is executed given members' ensuing voting strategies; so, if

 $\mu_{i;r}^* = \delta_r$  is a best response for  $m_i$ , it is also part of her equilibrium information strategy. So to conclude our proof, we wish to show:

$$\int_{0}^{1} \left[ \pi_{i}(q; r) - \pi_{i}(r; r) \right] d\mu(q) - C_{i}(\mu) \leq 0 \qquad \text{for all } \mu \in \Delta_{r}([0, 1])$$
 (4.1)

whenever  $r \geq \tilde{Q}$ .

To this end, define  $\overset{\bullet}{\pi}_i(q_i)$  to be the payoff  $m_i$  expects under an  $m_i$ -dictatorship given her posterior belief  $q_i$ ; i.e.,  $\overset{\bullet}{\pi}_i(q_i) := \max\{0, q_i \times (1 + u_i) - 1\}$ . Since  $\bar{q}_i \geq \overset{\bullet}{Q}$ , Lemma 1 implies that:

did i show
this in the
proof of the
lemma?

$$\int_{0}^{1} \left[ \overset{\star}{\pi}_{i}(q) - \overset{\star}{\pi}_{i}(r) \right] d\mu(q) - C_{i}(\mu) \leq 0 \qquad \text{for all } \mu \in \Delta_{r}([0, 1])$$

$$(4.2)$$

whenever  $r \geq \mathbf{\ddot{Q}}$ . So, we are done once we show:

$$\int_0^1 \tilde{\pi}_i(q; r) d\mu(q) \le 0 \qquad \text{for all } \mu \in \Delta_r([0, 1])$$

$$\tag{4.3}$$

where  $\tilde{\pi}_i(q,r) := [\pi_i(q,r) - \pi_i(r,r)] - [\overset{\bullet}{\pi}_i(q) - \overset{\bullet}{\pi}_i(r)].$ 

To see this, first note that  $\pi_i(q,r) - \overset{\bullet}{\pi}_i(q) \leq \pi_i \left( (1+u_i)^{-1}, r \right) - \overset{\bullet}{\pi}_i \left( (1+u_i)^{-1} \right) = 0$ , so  $\tilde{\pi}_i(q,r)$  is piecewise linear, decreasing below  $q = (1+u_i)^{-1}$ , and increasing above  $q = (1+u_i)^{-1}$ . Therefore,  $\tilde{\pi}_i(.,r)$  is a concave function for any  $r \geq \overset{\bullet}{Q}$ . Combined with the fact that  $\tilde{\pi}_i(r,r) = 0$ , this gives:

$$\int_0^1 \tilde{\pi}_i(q;r) d\mu(q) \le \int_0^1 \tilde{\pi}_i(q;r) d\delta_r(q) = 0 \qquad \text{for all } \mu \in \Delta_r\left([0,1]\right)$$

by Jensen's Inequality.

Claim 3. The dictatorship of the most-demanding member is a dominant voting mechanism.

*Proof.* In the equilibrium the dictatorship of the most-demanding member induces, no committee member acquires private information about the state. Any other voting mechanism must thus result in a weakly higher expected cost of information acquisition for each member.

To conclude the proof, it suffices to show that any fixed voting mechanism achieves:

- (a) a lower probability that the policy is enacted when  $\omega = \omega_1$ , and
- (b) a lower probability that the policy is blocked when  $\omega = \omega_0$

than the dictatorship of the most-demanding member.

Recall (from Lemma 1) that, under this dictatorship, the lobbyist's equilibrium information strategy is the unique distribution  $\overset{\bullet}{\mu}_l$  such that supp  $\overset{\bullet}{\mu}_l = \left\{0, \min\{p, \overset{\bullet}{Q}\}\right\}$ . Therefore, the dictator never blocks the policy unless her interim belief is r=0; i.e.  $\omega=\omega_0$  is revealed. The policy is implemented whenever  $\omega=\omega_1$ .

Note that, due to Claim 2, the probability that the policy is executed following interim beliefs r=0 and  $r=\bar{Q}$  are  $\bar{D}$  and  $\bar{D}$ , respectively. Therefore, if the lobbyist employs the strategy  $\mu_l$  described above, we get:

$$\mathbb{P}_{D, \breve{\mu}_{l}} \left( \text{enact} \mid \omega = \omega_{1} \right) = \bar{D} \qquad \mathbb{P}_{D, \breve{\mu}_{l}} \left( \text{enact} \mid \omega = \omega_{0} \right) = 1 - \mathbb{P}_{\breve{\mu}_{l}} \left( r = 0 \mid \omega_{0} \right) \times (1 - D)$$

The lobbyist's equilibrium information strategy,  $\mu_l^*$ , must weakly increase at least one of these probabilities. Since the probability that the policy is enacted cannot exceed  $\bar{D}$  in either state, we conclude that:

$$\mathbb{P}_{D,\mu_l^*} \left( \text{enact} \mid \omega = \omega_1 \right) \leq \bar{D} \leq 1$$

$$\mathbb{P}_{D,\mu_l^*} \left( \text{enact} \mid \omega = \omega_0 \right) \geq 1 - \mathbb{P}_{\boldsymbol{\mu}_l} \left( r = 0 \mid \omega_0 \right) \times (1 - \underline{D}) \geq 1 - \mathbb{P}_{\boldsymbol{\mu}_l} \left( r = 0 \mid \omega_0 \right)$$

better to
do this in
two "steps"
rather than
"claim"s.

### 5 Discussion