



Instituto Politécnico  
Nacional



# Neurofuzzy Systems

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PRACTICE NN 1. PERCEPTRON VS ADALINE

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Delivery Date: - May 2023

## I. Introduction

In the realm of artificial intelligence and machine learning, neural networks have emerged as a powerful paradigm for solving complex problems. Inspired by the structure and functionality of the human brain, neural networks simulate the behavior of interconnected neurons to process and analyze vast amounts of data. With their ability to learn from experience, adapt, and generalize, neural networks have revolutionized various domains, including image recognition, natural language processing, and pattern classification.

The Perceptron, introduced by Frank Rosenblatt in 1957, can be considered the precursor to modern neural networks. It consists of a single layer of artificial neurons, or perceptrons, interconnected through weighted connections. This simple yet powerful model paved the way for the development of more complex neural network architectures. However, the Perceptron has limitations in handling linearly non-separable data and updating its weights in real-time, leading to the need for further advancements.

Enter Adaline, which stands for Adaptive Linear Neuron. Developed by Bernard Widrow and Tedd Hoff in 1960, Adaline builds upon the foundation laid by the Perceptron. It addresses some of the Perceptron's shortcomings by introducing a more flexible learning rule and the concept of continuous activation. Adaline's breakthrough lies in its ability to handle linearly non-separable data through gradient descent optimization, allowing for fine-tuning of weights and improved convergence.

By understanding the differences between Perceptron and Adaline, we gain insights into the progression of neural networks and the evolving strategies employed to address various challenges. This exploration will equip us with a solid foundation to tackle real-world problems using neural network algorithms and open doors to further advancements in artificial intelligence and machine learning.

## II. Objective

Objective of the Practice:

The objective of this practice is to gain a practical understanding of neural networks by focusing on the Perceptron and Adaline models. Through hands-on exploration and experimentation, the practice aims to achieve the following objectives:

1. Implement Perceptron and Adaline algorithms: Develop a working knowledge of how to implement the Perceptron and Adaline algorithms using appropriate programming tools or frameworks. This will involve understanding the mathematical foundations of these algorithms and translating them into code.
2. Explore architecture and learning rules: Investigate the architectural differences between Perceptron and Adaline, including the number of layers, activation functions, and learning rules. Analyze how these differences affect the models' capabilities, convergence, and generalization.
3. Compare performance on linearly separable and non-separable data: Evaluate the performance of Perceptron and Adaline models on linearly separable and non-separable datasets. Analyze and compare their abilities to correctly classify and converge on the correct decision boundaries for different types of data.
4. Examine convergence and limitations: Study the convergence properties of Perceptron and Adaline models, including their limitations in handling complex or overlapping classes. Identify scenarios where one model outperforms the other and understand the factors contributing to these differences.
5. Gain insights into practical applications: Discuss the real-world applications of Perceptron and

Adaline models, considering their strengths and weaknesses. Explore scenarios where one model may be more suitable than the other based on the characteristics of the problem and available data.

### III. Development

It is asked to implement:

#### A. Perceptron

Implement a perceptron neural network to classify the toys (bears and rabbits). Train the network for different number of epochs:

- 20
- 50
- 100

#### B. Adaline

Implement an Adaline neural network to classify the toys (bear and rabbits). Train the network for different number of epochs:

##### 1. 20

- $\alpha = 1/(4 * \lambda_{\max})$
- $\alpha = 1/(8 * \lambda_{\max})$
- $\alpha = 1/(16 * \lambda_{\max})$

##### 2. 50

- $\alpha = 1/(4 * \lambda_{\max})$
- $\alpha = 1/(8 * \lambda_{\max})$
- $\alpha = 1/(16 * \lambda_{\max})$

##### 3. 100

- $\alpha = 1/(4 * \lambda_{\max})$
- $\alpha = 1/(8 * \lambda_{\max})$
- $\alpha = 1/(16 * \lambda_{\max})$

Then make the comparison of Perceptron vs Adaline. Start with random values of  $W$  and  $B$ , the same for Perceptron and Adaline. Train both networks simultaneously for different number of epochs and different values of  $\alpha$  in Adaline. In one figure subplot for each of the number of epochs (3 graphs):

- Solution of the 2 networks(patterns, limit lines (overlaped in different colour))

- Error perceptron (1 subplot), 3 errors for adaline(1 subplot, in different colours). Add labels and titles to your graphs.

To test the networks:

- Select the best option for alpha and number of epochs
- Ask the user for a input(p)
- Calculate the output for perceptron and adaline
- Display a figure of bear or rabbit

## IV. Results

The first results we got are the subplots of the solutions of both Networks.

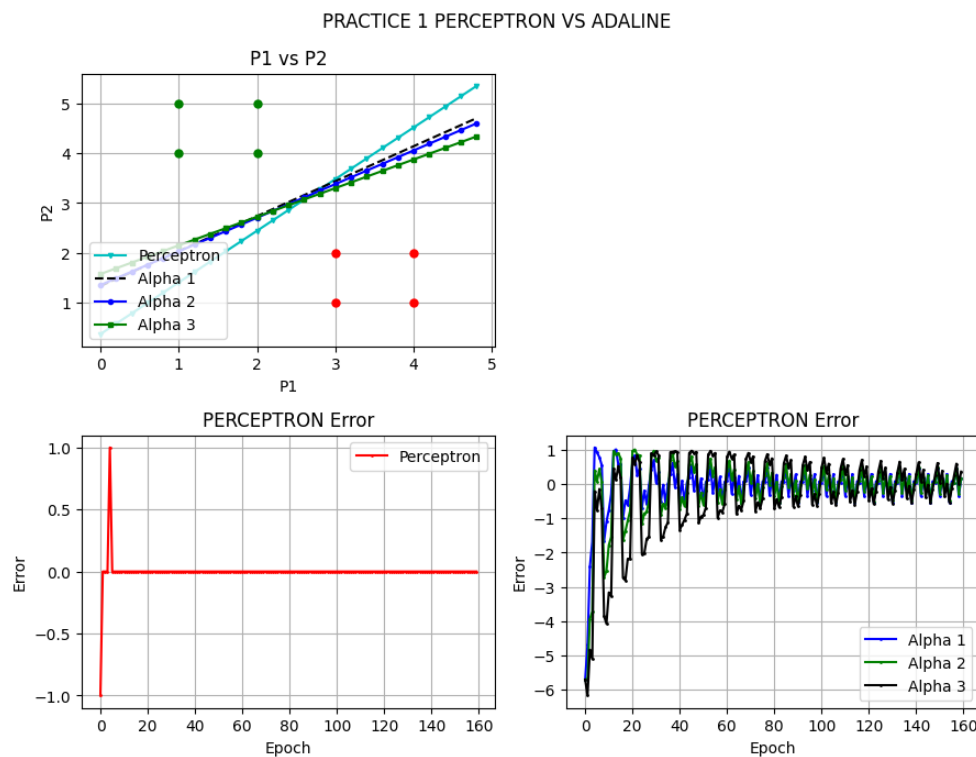


Figure 1: 20 Epochs

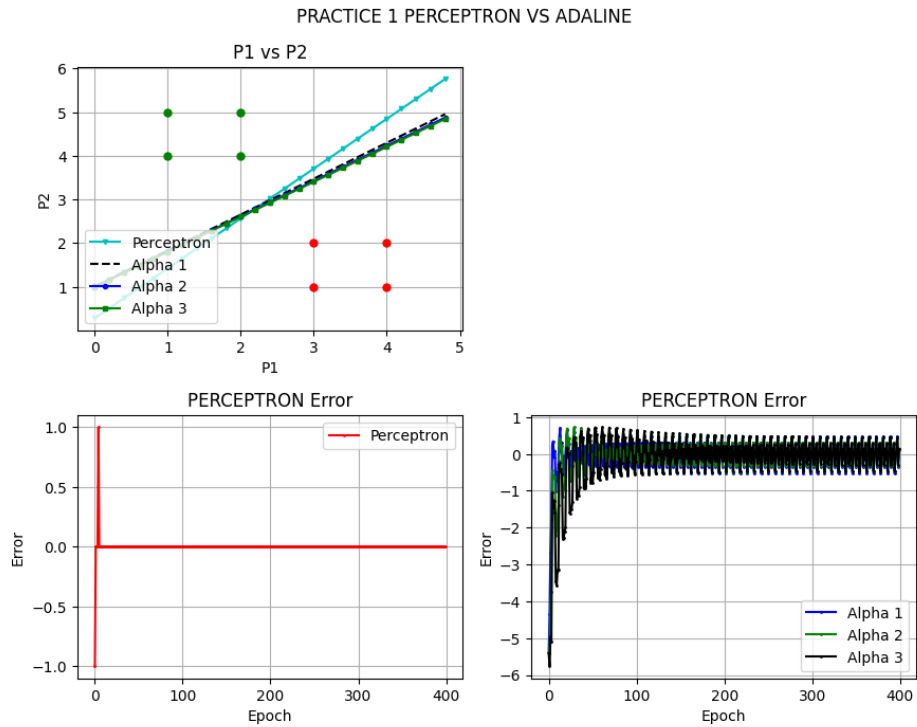


Figure 2: 50 Epochs

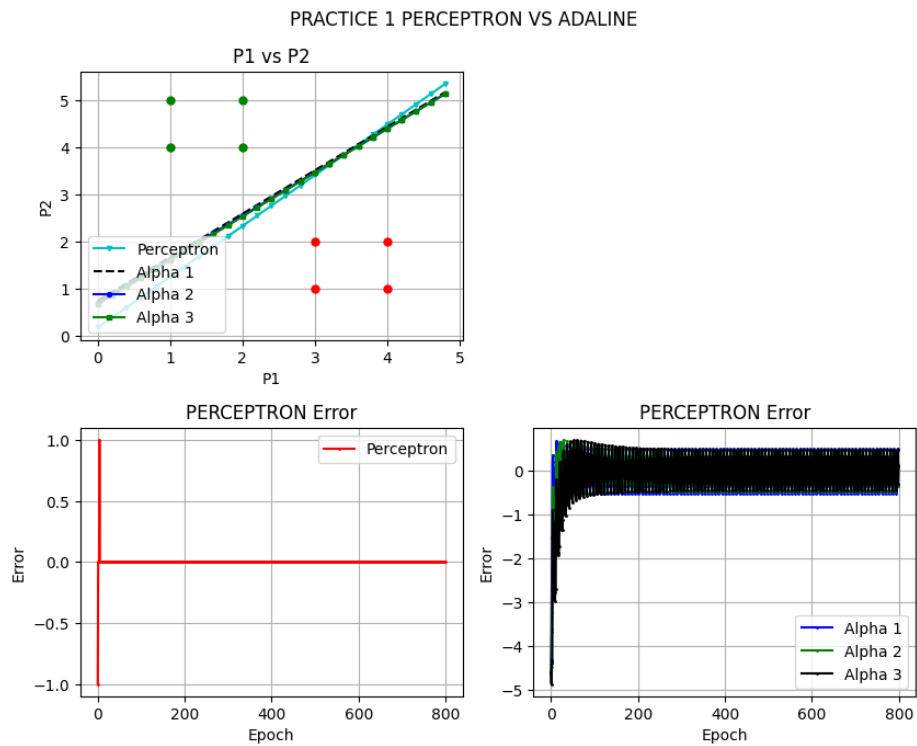
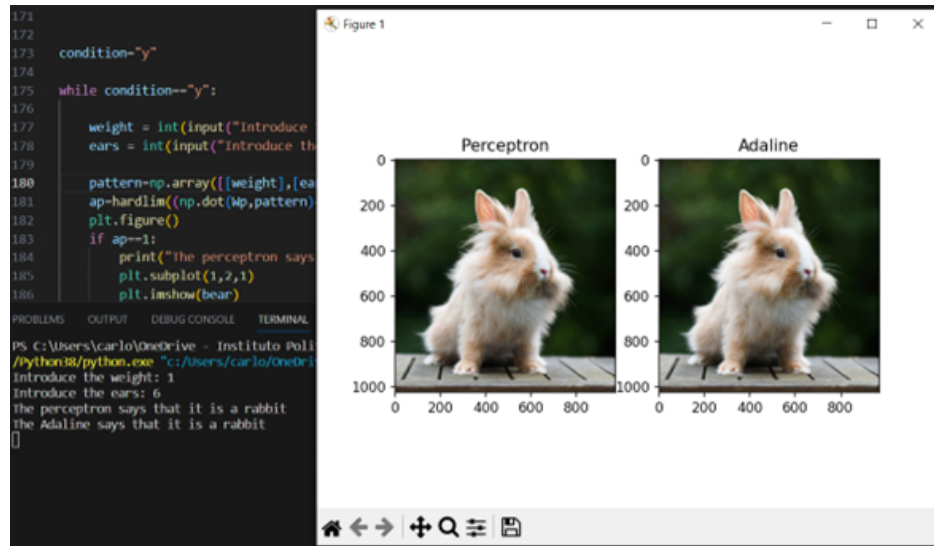


Figure 3: 100 Epoch

As it can be seen, the difference between Perceptron and Adaline is that in perceptron, once it finds a solution, it does not try to find another better solution, that's why the error is almost always 0, in contrast with adaline's error. that it begins in -5 and it tends to turn around 0, but it is always chasing trying to find a better solution.

In this cases, I considered that the best solution was with Adaline and with the second alpha and with 100 epochs. So in the testing we got the next results:



learning rule and decision boundaries.

The perceptron algorithm uses a simple step function as its activation function and employs the perceptron learning rule, which updates the weights based on misclassified samples. It has a linear decision boundary and can only solve linearly separable problems. However, it converges to a solution if the data is linearly separable.

On the other hand, Adaline (Adaptive Linear Neuron) uses a linear activation function and employs the Widrow-Hoff learning rule, also known as the delta rule or least mean squares (LMS) algorithm. Adaline aims to minimize the mean squared error between its predicted outputs and the desired outputs. Unlike the perceptron, Adaline can handle non-linearly separable problems because it uses continuous outputs and computes a weighted sum of inputs rather than a binary output.

Overall, the practice helped to highlight the key differences between the perceptron and Adaline algorithms, such as their learning rules and decision boundaries, and provided a hands-on understanding of their behavior on different types of data.—

## VI. Apenddix

### A. Code

#### 1. Code

```

1 import matplotlib.pyplot as plt
2 import numpy as np
3 import matplotlib.image as mpimg
4
5 def hardlim(x):
6     if (x<0).all():
7         return 0
8     else:
9         return 1
10
11 def purelin(x):
12     return x
13
14
15 # patterns
16 P=np.array([[1,1,2,2,3,3,4,4], [4,5,4,5,1,2,1,2]]) #matrix of patterns
17 Tp=np.array([0,0,0,0,1,1,1,1])
18 Ta=np.array([-1,-1,-1,-1,1,1,1,1])
19
20 [R,N]=P.shape
21 S=1 # number of neurons
22 epoch=100 # number of epochs
23
24 #WEIGHTS AND BIAS FOR PERCEPTRON
25 Wp=np.random.rand(S,R) # matrix of weights
26 bp=np.random.rand(S,1) # matrix of bias
27
28 #WEIGHTS AND BIAS FOR ADALINE
29 Wa1=Wp
30 ba1=bp
31 Wa2=Wp
32 ba2=bp
33 Wa3=Wp
34 ba3=bp

```

```

35
36 R=(1/N)*np.dot(P,P.T)
37 eigen=np.linalg.eigvals(R)
38
39 #Alpha
40 alpha1=1/(4*max(eigen))
41 alpha2=1/(8*max(eigen))
42 alpha3=1/(16*max(eigen))
43
44 #errors list
45 errorp=[]
46 errora1=[]
47 errora2=[]
48 errora3=[]
49
50 it=0
51 ue=[]
52 #Training
53 for i in range(epoch):
54     for j in range(N):
55         ue.append(it)
56         it=it+1
57
58         x=P[:,j]
59
60         #Percetron Training
61         ap=hardlim((np.dot(Wp,x)+bp))
62         e_p=Tp[j]-ap
63         errorp.append(e_p)
64         Wp=Wp+e_p*x
65         bp=bp+e_p
66
67         #Adeline Training 1
68         aa1=purelin((np.dot(Wa1,x)+ba1))
69         e_a1=Ta[j]-aa1
70         errora1.append(e_a1[0][0])
71         Wa1=Wa1+alpha1*e_a1*x
72         ba1=ba1+alpha1*e_a1
73
74         #Adeline Training 2
75         aa2=purelin((np.dot(Wa2,x)+ba2))
76         e_a2=Ta[j]-aa2
77         errora2.append(e_a2[0][0])
78         Wa2=Wa2+alpha2*e_a2*x
79         ba2=ba2+alpha2*e_a2
80
81         #Adeline Training 3
82         aa3=purelin((np.dot(Wa3,x)+ba3))
83         e_a3=Ta[j]-aa3
84         errora3.append(e_a3[0][0])
85         Wa3=Wa3+alpha3*e_a3*x
86         ba3=ba3+alpha3*e_a3
87
88 X = np.arange(0,5,0.2)
89 Y = np.arange(0,5,0.2)
90
91 #-----PLOT PATTERNS
92 a=P.tolist()
93

```



```

94 fig=plt.figure(figsize=(10,10),tight_layout=True)
95 fig.suptitle("PRACTICE 1 PERCEPTRON VS ADALINE")
96 plt.subplot(2,2,1)
97 for i in range(len(a[0])):
98     if i <=3:
99         plt.plot(a[0][i],a[1][i], 'go', markersize=5)
100     else:
101         plt.plot(a[0][i],a[1][i], 'ro', markersize=5)
102
103 #-----LIMIT LINE ALPHA1
104 Wpp=Wp[0].tolist()
105 bpp=bp[0].tolist()
106
107 limlineP=[]
108 for x in X:
109     limlineP.append(-bpp[0]/Wpp[1]-Wpp[0]/Wpp[1]*x)
110 plt.plot(X,limlineP, 'cv-', markersize=3, label='Perceptron')
111
112 #-----LIMIT LINE ALPHA1
113 Wa1p=Wa1[0].tolist()
114 ba1p=ba1[0].tolist()
115
116 limlineA1=[]
117 for x in X:
118     limlineA1.append(-ba1p[0]/Wa1p[1]-Wa1p[0]/Wa1p[1]*x)
119 plt.plot(X,limlineA1, 'k--', markersize=3, label='Alpha 1')
120
121 #-----LIMIT LINE ALPHA2
122 Wa2p=Wa2[0].tolist()
123 ba2p=ba2[0].tolist()
124
125 limlineA2=[]
126 for x in X:
127     limlineA2.append(-ba2p[0]/Wa2p[1]-Wa2p[0]/Wa2p[1]*x)
128 plt.plot(X,limlineA2, 'b-o', markersize=3, label='Alpha 2')
129
130 #-----LIMIT LINE ALPHA3
131 Wa3p=Wa3[0].tolist()
132 ba3p=ba3[0].tolist()
133
134 limlineA3=[]
135 for x in X:
136     limlineA3.append(-ba3p[0]/Wa3p[1]-Wa3p[0]/Wa3p[1]*x)
137 plt.plot(X,limlineA3, 'g-s', markersize=3, label='Alpha 3')
138 plt.xlabel('P1')
139 plt.ylabel('P2')
140 plt.title('P1 vs P2')
141 plt.legend(loc="lower left")
142 plt.grid(True)
143
144 #-----PLOT PERCEPTRON ERROR
145
146 plt.subplot(2,2,3)
147 plt.plot(ue,errorp, 'r-o', markersize=1, label='Perceptron')
148 plt.xlabel('Epoch')
149 plt.ylabel('Error')
150 plt.title('PERCEPTRON Error')
151 plt.legend()
152 plt.grid(True)

```

```

153 #-----PLOT ADALINE ERROR
154
155 plt.subplot(2,2,4)
156 plt.plot(ue,errora1,'b-o',markersize=1,label='Alpha 1')
157 plt.plot(ue,errora2,'g-o',markersize=1,label='Alpha 2')
158 plt.plot(ue,errora3,'k-o',markersize=1,label='Alpha 3')
159 plt.xlabel('Epoch')
160 plt.ylabel('Error')
161 plt.title('PERCEPTRON Error')
162 plt.grid(True)
163
164 #plt.show()
165
166 #-----TESTING
167
168 bear = mpimg.imread('bear.jpg')
169 rabbit = mpimg.imread('rabbit.jpg')
170
171 print(Wp)
172 print(Wa2)
173
174 condition="y"
175
176 while condition=="y":
177
178     weight = int(input("Introduce the weight: "))
179     ears = int(input("Introduce the ears: "))
180
181     pattern=np.array([[weight],[ears]])
182     print(pattern)
183     ap=hardlim((np.dot(Wp,pattern)+bp))
184     plt.figure()
185     if ap==1:
186         print("The perceptron says that it is a bear")
187         plt.subplot(1,2,1)
188         plt.imshow(bear)
189         plt.title("Perceptron")
190     else:
191         print("The perceptron says that it is a rabbit")
192         plt.subplot(1,2,1)
193         plt.imshow(rabbit)
194         plt.title("Perceptron")
195
196     aa=purelin((np.dot(Wa2,pattern)+ba2))
197     if aa>0:
198         print("The Adaline says that it is a bear")
199         plt.subplot(1,2,2)
200         plt.imshow(bear)
201         plt.title("Adaline")
202     else:
203         print("The Adaline says that it is a rabbit")
204         plt.subplot(1,2,2)
205         plt.imshow(rabbit)
206
207     plt.show()
208     condition=input("Do you want to continue? (y/n): ")
209
210 print("BYE!")

```