Homework 9

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Setting Seed

```
set.seed(06072001)
```

Problem 1

```
#a
setwd('/Users/santhoshrajendran/Documents/3rd Year 1st Sem HW Files/STAT 3080')
data1 <- read.csv("Data1.csv")</pre>
corr1 <- cor(data1$V1, data1$V2)</pre>
corr1
## [1] 0.524066
#b
pairedt <- function(df){</pre>
  samp <- df[sample(nrow(df), 13), ]</pre>
  test <- t.test(samp$V1, samp$V2, mu=0, alternative="two.sided", paired=TRUE)</pre>
  pval <- test$p.value</pre>
  pval < 0.05
paired1 <- sum(replicate(10000, pairedt(data1)) == TRUE) / 10000</pre>
paired1
## [1] 0.0474
#c
```

```
twosamp <- function(df){</pre>
  samp <- df[sample(nrow(df), 13), ]</pre>
  test <- t.test(samp$V1, samp$V2, mu=0, alternative="two.sided")</pre>
  pval <- test$p.value</pre>
  pval < 0.05
}
twosamp1 <- sum(replicate(10000, twosamp(data1)) == TRUE) / 10000</pre>
twosamp1
## [1] 0.0075
Problem 2
#a
data2<-read.csv("Data2.csv")</pre>
corr2 <- cor(data2$V1, data2$V2)</pre>
corr2
## [1] -0.52036
#b
paired2 <- sum(replicate(10000, pairedt(data2)) == TRUE) / 10000</pre>
paired2
## [1] 0.0533
#c
twosamp2 <- sum(replicate(10000, twosamp(data2)) == TRUE) / 10000</pre>
twosamp2
## [1] 0.107
```

Problem 3

```
#a
data3 <- read.csv("data3.csv")</pre>
corr3 <- cor(data3$V1, data3$V2)</pre>
corr3
## [1] 0.002426237
#b
paired3 <- sum(replicate(10000, pairedt(data3)) == TRUE) / 10000</pre>
paired3
## [1] 0.0511
#c
twosamp3 <- sum(replicate(10000, twosamp(data3)) == TRUE) / 10000
twosamp3
## [1] 0.0511
Problem 4
```

```
correlation <- c(corr1, corr2, corr3)</pre>
pairedtest <- c(paired1, paired2, paired3)</pre>
twosampletest <- c(twosamp1, twosamp2, twosamp3)</pre>
data.frame(correlation, pairedtest, twosampletest)
      correlation pairedtest twosampletest
##
## 1
      0.524066001
                                      0.0075
                       0.0474
## 2 -0.520360008
                       0.0533
                                      0.1070
## 3 0.002426237
                       0.0511
                                      0.0511
```

One observation that can be made is the relationship between correlation and the Type 1 error probability for a two sample t test; with more negative correlation values, a larger probability for a Type 1 Error occurs. Another observation is that the Type 1 error for the paired t test was not affected by the sign before the correlation value. The probability values for the paired test stayed consistent around .05.

Problem 5

```
#a
data5 <- read.csv("data4.csv")</pre>
corr5 <- cor(data5$V1, data5$V2)</pre>
corr5
## [1] 0.5906402
#b
paired5 <- sum(replicate(10000, pairedt(data5)) == TRUE) / 10000</pre>
paired5
## [1] 0.0468
#c
twosamp5 <- sum(replicate(10000, twosamp(data5)) == TRUE) / 10000</pre>
twosamp5
## [1] 0.0139
Problem 6
#a
data6 <- read.csv("data5.csv")</pre>
corr6 <- cor(data6$V1, data6$V2)</pre>
corr6
## [1] -0.5721193
#b
paired6 <- sum(replicate(10000, pairedt(data6)) == TRUE) / 10000</pre>
paired6
## [1] 0.0717
#c
twosamp6 <- sum(replicate(10000, twosamp(data6)) == TRUE) / 10000</pre>
twosamp6
## [1] 0.115
```

Problem 7

```
#a

data7 <- read.csv("data6.csv")
corr7 <- cor(data7$V1, data7$V2)
corr7

## [1] -0.007297158

#b

paired7 <- sum(replicate(10000, pairedt(data7)) == TRUE) / 10000
paired7

## [1] 0.0386

#c

twosamp7 <- sum(replicate(10000, twosamp(data7)) == TRUE) / 10000
twosamp7

## [1] 0.0292</pre>
```

Problem 8

```
correlation <- c(corr5, corr6, corr7)</pre>
pairedtest <- c(paired5, paired6, paired7)</pre>
twosampletest <- c(twosamp5, twosamp6, twosamp7)</pre>
data.frame(correlation, pairedtest, twosampletest)
##
      correlation pairedtest twosampletest
## 1
      0.590640226
                                      0.0139
                       0.0468
## 2 -0.572119341
                       0.0717
                                      0.1150
## 3 -0.007297158
                       0.0386
                                      0.0292
```

One conclusion that can be noted is the increasing probability of a Type 1 error for two sample t tests when correlation values reach progressively more negative values. For paired t tests, the probability of a Type 1 error increases when correlation values change from \sim -.007 to \sim -.572 but not from \sim 0.591 to -0.007.