

**Processamento Digital de Sinais**  
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**Lista de exercícios 1C – Sinais e sistemas digitais (DTFT)**

**P3.3** Determine analytically the DTFT of each of the following sequences. Plot the magnitude and angle of  $X(e^{j\omega})$  over  $0 \leq \omega \leq \pi$ .

1.  $x(n) = 2(0.5)^n u(n+2)$ .
2.  $x(n) = (0.6)^{|n|} [u(n+10) - u(n-11)]$ .
3.  $x(n) = n(0.9)^n u(n+3)$ .
4.  $x(n) = (n+3)(0.8)^{n-1} u(n-2)$ .
5.  $x(n) = 4(-0.7)^n \cos(0.25\pi n)u(n)$ .

**P3.11** For each of the linear, shift-invariant systems described by the impulse response, determine the frequency response function  $H(e^{j\omega})$ . Plot the magnitude response  $|H(e^{j\omega})|$  and the phase response  $\angle H(e^{j\omega})$  over the interval  $[-\pi, \pi]$ .

1.  $h(n) = (0.9)^{|n|}$
2.  $h(n) = \text{sinc}(0.2n)[u(n+20) - u(n-20)]$ , where  $\text{sinc } 0 = 1$ .
3.  $h(n) = \text{sinc}(0.2n)[u(n) - u(n-40)]$
4.  $h(n) = [(0.5)^n + (0.4)^n]u(n)$
5.  $h(n) = (0.5)^{|n|} \cos(0.1\pi n)$

**P3.13** Let  $x(n) = 3 \cos(0.5\pi n + 60^\circ) + 2 \sin(0.3\pi n)$  be the input to each of the systems described in Problem P3.11. In each case, determine the output sequence  $y(n)$ .

**P3.18** A linear, shift-invariant system is described by the difference equation

$$y(n) = \sum_{m=0}^3 x(n-2m) - \sum_{\ell=1}^3 (0.81)^\ell y(n-2\ell)$$

Determine the steady-state response of the system to the following inputs:

1.  $x(n) = 5 + 10(-1)^n$
2.  $x(n) = 1 + \cos(0.5\pi n + \pi/2)$
3.  $x(n) = 2 \sin(\pi n/4) + 3 \cos(3\pi n/4)$
4.  $x(n) = \sum_{k=0}^5 (k+1) \cos(\pi k n/4)$
5.  $x(n) = \cos(\pi n)$

In each case, generate  $x(n)$ ,  $0 \leq n \leq 200$ , and process it through the **filter** function to obtain  $y(n)$ . Compare your  $y(n)$  with the steady-state responses in each case.