Week 3 Review: Risk and the Evaluation of Alternatives

◆ Example: Europa Solvent Industries

Europa Solvent Industries: Business Context

- Europa Solvent Industries (ESI) has a contract to supply one of its receives a daily payment of 10000€ per ton customers with 35 tons of a chemical solvent each day, for which it
- particular day the actual production may fall below or above this value is tuned to produce 35 tons of solvent each day on average, on any technological reasons, is somewhat unreliable. While its production line ESI operates a solvent production line whose processing speed, due to
- with a mean of 35 tons and a standard deviation of 7 tons Analysis of the past data shows that the daily output of the production line, P, can be approximated as a normally distributed random variable

Europa Solvent Industries: Business Context

- ESI's daily production cost is 9500€ per ton of solvent
- per ton (i.e., at a loss as compared to ESI's production cost) extra solvent it produces to a discount retail chain at a price of 9000€ If ESI's daily production exceeds 35 tons, the company must sell the
- and it must also pay the customer a penalty of 2000€ for each ton all of its daily production to its customer at the price of 10000€ per ton, In the case that the daily production falls short of 35 tons, ESI will sell ESI will pay the penalty of (35-32.5)*2000€ = 5000€ below 35. For example, if the daily production happens to be 32.5 tons,

Europa Solvent Industries: Questions

- Suppose that, on a particular day, the daily production P turns out to be 31 tons of solvent. What is the total profit ESI will make on that day?
- Consider a day when the company's daily production turns out be to 37 tons of solvent. What is the total profit ESI will make on that day?
- daily profit value V as a function of its daily production P Write down an algebraic expression that calculates the company's total
- Simulate (using n=100 simulation runs and seed = 123) the distribution to answer the following questions: of the total daily profit that ESI makes, V, and use the simulation results
- What is estimate of the expected value of the total daily profit?
- What is the estimate of the standard deviation of the total daily

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the penalty cost of 2000€ for each ton under 35. sell all of it to the customer at the price of 10000€ per ton, and b) will incur Answer: since the production on that day fell short of 35 tons, ESI will a)

ESI's regular revenue on that day is 10000€*31 = 310000€

ESI's production cost on that day is 9500€*31 = 294500€

ESI's penalty cost on that day is 2000€ *(35-31) = 8000€

ESI's total profit on that day is 310000€ - 294500€ - 8000€ = 7500€

Consider a day when the company's daily production turns out be to 37 tons of solvent. What is the total daily profit ESI will make on that day?

tons to the discount chain for 9000€ per ton. 35 tons to the customer at the price of 10000€ per ton, and b) will sell 2 Answer: since the production on that day exceeds 35 tons, ESI will a) sell

ESI's regular revenue on that day is 10000€*35 = 350000€

ESI's discount revenue on that day is 9000€*(37-35) = 18000€

ESI's production cost on that day is 9500€*37 = 351500€

ESI's total profit on that day is 350000€ + 18000€ - 351500€ = 16500€

Write down an algebraic expression that calculates the company's daily profit value V as a function of its daily production P

Answer:

How we calculate ESI's total daily profit depends on whether its daily production is below 35 or at or above that value

In the case that P<35, ESI

- a) incurs production cost of 9500*P,
- <u></u> sells all of its production at the price of 10000€ per ton, obtaining revenue of 10000*P and
- c) incurs penalty cost of 2000*(35-P)

=500*P-2000*(35-P)=500*P-70000+2000*P=2500*P-70000In total, for *P*<35, ESI's total daily profit is 10000**P*-9500**P*-2000*(35-*P*)

In the case that $P \ge 35$, ESI

- a) incurs production cost of 9500*P, and
- <u></u> sells the first 35 tons of its production at the price of 10000€ per ton, and revenue of 10000*35+9000*(P-35) the remaining *P*-35 tons at the discount price of 9000€ per ton, obtaining

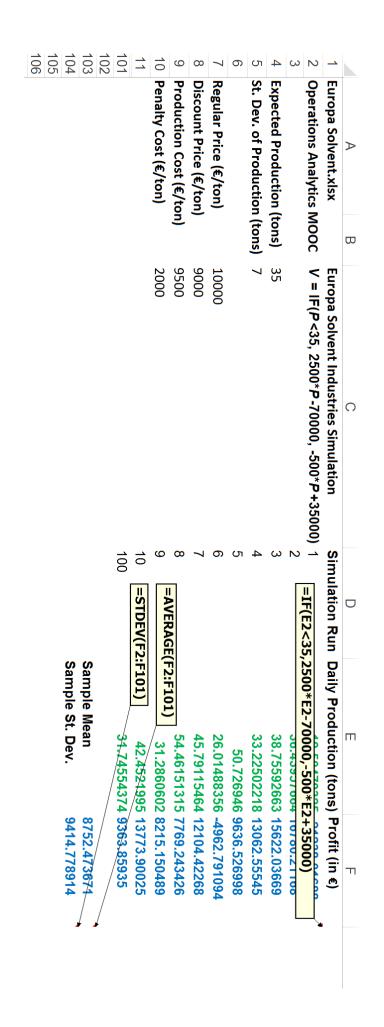
= -500*P + 35000In total, for $P \ge 35$, ESI's total daily profit is $10000^*35 + 9000^*(P-35) - 9500^*P$

Combining the two cases, we can write the expression for the total daily protit:

V = IF(P < 35, 2500*P - 70000, -500*P + 35000)

Europa Solvent Industries: Questions

- Simulate (using n=100 simulation runs and seed = 123) the distribution to answer the following questions: of the total daily profit that ESI makes, V, and use the simulation results
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- profit? What is the estimate of the standard deviation of the total daily



♦ See Europa Solvent.xlsx

- Simulate (using n=100 simulation runs and seed = 123) the distribution to answer the following questions: of the total daily profit that ESI makes, V, and use the simulation results
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- What is the estimate of the standard deviation of the total daily profit?

Answer:

estimate of the **expected daily profit is about 8752€**, and estimate of the standard deviation of the daily profit is about 9415€ Based on a simulation with n=100 simulation runs and seed=123, the