The ILTP Library in Intuitionistic Linear Logic

October 8, 2018

Abstract

We present the results of the prover https://github.com/carlosolarte/Benchmarking-Linear-Logic for three different encodings of the propositional problems of the ILTP library http://iltp.de as intuitionistic linear logic [1] sequents. We consider the Girard's translations [1] call-by-name and call-by-value as well as the Liang and Miller translation 0/1.

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1 General Information

- Test run on a QEMU Virtual CPU, 2GHz, 64 bits, 2GB of RAM running Ubuntu.
- Timeout: 2min.
- Maude version: 2.7.1 built: Oct 2 2017.

• The search procedure considers proofs using up to 10 times the copy rule (focusing on one of the formulas of the classical context). Since this procedure is not complete, failures cannot be considered as non-provable sequents. For this reason, we reprocessed the problems that returned "failed" with a prover where the copy rule can be used an unboundedly number of times. The sequents marked as fail here can be then considered as non-theorems (since the prover explored all the possibilities).

2 Statistics

2.1 Translation 0/1

	KLE	LCL	SYJ	SYN
Problems	88	2	252	20
Unsolved (timeouts)	13	2	223	13
Solved (Theorems)	75	0	29	7
Non-Theorems	0	0	0	0
Min Time	30	-	26	17
Avg Time	736.66	-	20733.45	320.71
Max Time	19336	-	117105	795

2.2 Call-by-Name

	KLE	LCL	SYJ	SYN
Problems	88	2	252	20
Unsolved (timeouts)	13	2	218	9
Solved (Theorems)	75	0	34	11
Non-Theorems	0	0	0	5
Min Time	23	-	26	24
Avg Time	1172.12	-	9162.94	335.67
Max Time	28552	-	80827	845

2.3 Call-by-Value

	KLE	LCL	SYJ	SYN
Problems	88	2	252	20
Unsolved (timeouts)	12	2	227	9
Solved (Theorems)	75	0	25	7
Non-Theorems	1	0	0	4
Min Time	45	0	30	17
Avg Time	1210.4	-	16127.2	268.86
Max Time	58637	-	112706	769

3 Translation 0/1

3.1 KLE Problems

```
file: KLE/KLE002+1.p (357 ms)
     \overline{a,!(a)\multimap !(b),!(b)\multimap !(c): \cdot \vdash a}
                                                                                                                                                                   \overline{a, b, !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash b}
\frac{a,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash a}{a,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash \vdash !(a)} ! \frac{a,b,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash b}{a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \vdash b} \star
                                                                  a,!(a) \multimap !(b),!(b) \multimap !(c) : !(a) \multimap !(b) \vdash b
                                                                                     a, \overline{!(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash b}
                                                                                                                                                                                                                                                                                                                                               a, c, !(a) \multimap !(\overline{b), !(b)} \multimap !(c) : \cdot \vdash c
                                                                                                                                                                                                                                                                                                                                           \frac{1}{a,!(a) \multimap !(b),!(b) \multimap !(c) : !(c) \vdash c} \star
                                                                                  a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash !(b)
                                                                                                                                                                                                a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \multimap !(c) \vdash c 
D_C
                                                                                                                                                                                                              a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash c
                                                                                                                                                                                                           \frac{1}{(a)\multimap !(b),!(b)\multimap !(c): \cdot \vdash !(a)\multimap c}
                                                                                                                                                                                                      \frac{1}{!(a)\multimap !(b),!(b)\multimap !(c): \cdot \vdash !(!(a)\multimap c)}!
                                                                                                                                                                                             \cdot : !(!(a) \multimap !(b)), !(!(b) \multimap !(c)) \vdash !(!(a) \multimap c)
  file: KLE/KLE003+1.p (283 ms)
                                                                                                                                                                                                                                                                                                                            a, b, c, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \vdash c
                                                                                                                                              a, b, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \cdot \vdash b
                                                                                                                                          \frac{a, b, !(a) - !(!(b) - !(c)), !(b) - !(c) : + \vdash !(b)}{a, b, !(a) - !(!(b) - !(c)), !(b) - !(c) : + \vdash !(b)} \cdot \frac{a, b, !(a) - !(!(b) - !(c)), !(b) - !(c) : !(c) + \vdash c}{a, b, !(a) - !(b) - !(c), !(b) - !(c) : !(c) + c}
                                                                                                                                                                                                                      \frac{a, b, !(a) - !(!(b) - o !(c)), !(b) - o !(c) : \ !(b) - o !(c) \vdash c}{D_C}
                                                                                                                                                                                                                                      a, b, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \cdot \vdash c
   \overline{a,b,!(a)\multimap !(!(b)\multimap !(c)): \ \cdot \vdash a}
                                                                                                                                                                                                                                      a, b, !(a) \multimap !(!(b) \multimap !(c)) : !(!(b) \multimap !(c)) \vdash c
\overline{a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(a)}
                                                                                                      \frac{a, b, !(a) - \circ !(!(b) - \circ !(c)) : \ !(a) - \circ !(!(b) - \circ !(c)) \vdash c}{D_{C}}
                                                                                                                                          a,b,!(a)\multimap !(!(b)\multimap !(c)): \ \cdot \vdash c
                                                                                                                                  \overline{b,!(a)\multimap !(!(b)\multimap !(c)): \cdot \vdash !(a)\multimap c}
                                                                                                                             \overline{b,!(a)} \rightarrow !(!(b) \rightarrow !(c)) : \cdot \vdash !(!(a) \rightarrow c)!
                                                                                                                     \frac{!(a)\multimap !(!(b)\multimap !(c)): \cdot \vdash !(b)\multimap !(!(a)\multimap c)}{}
                                                                                                                \frac{!(a)\multimap !(!(b)\multimap !(c)): \ \cdot \vdash !(!(b)\multimap !(!(a)\multimap c))}{}
                                                                                                             \frac{}{ \cdot : \ !(!(a) \multimap !(!(b) \multimap !(c))) \vdash !(!(b) \multimap !(!(a) \multimap c)) } 
  file: KLE/KLE004+1.p (233 ms)
                                                                                                                                          \frac{\overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash b}}{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash !(b)} \; ! \; \overline{a,b,c,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \; \star \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(l) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(b) \multimap !(c) : \cdot \vdash c} \\ \overline{a,b,!(a) \multimap !(c) : 
                                                                                                                                                                                                                      \frac{(c)_{1}, (c)_{1}}{a, b, !(a) - 0 !(!(b) - 0 !(c)), !(b) - 0 !(c) : !(b) - 0 !(c) \vdash c}{D_{C}}
   a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash a
                                                                                                                                                                                                                                        a, b, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \cdot \vdash c
                                                                                                                                                                                                                                      \frac{a, b, !(a) - o!(!(b) - o!(c)) : !(!(b) - o!(c)) \vdash c}{a, b, !(a) - o!(c)} *
a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(a)
                                                                                                      \frac{a, b, !(a) - \circ !(!(b) - \circ !(c)) : \ !(a) - \circ !(!(b) - \circ !(c)) \vdash c}{D_C}
                                                                                                                                         a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash c
                                                                                                                     \frac{!(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(!(a) \& !(b)) \multimap c}{!(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(!(a) \& !(b)) \multimap c}
                                                                                                                 \frac{1}{!(a) \multimap !(!(b) \multimap !(c)) :} \cdot \vdash !(!(!(a) \& !(b)) \multimap c) !
                                                                                                             \frac{}{\cdot : \ !(!(a) \multimap !(!(b) \multimap !(c))) \vdash !(!(!(a) \& !(b)) \multimap c)}
    file: KLE/KLE005+1.p (567 ms)
```

```
\overline{a, b, !(!(a \& b))} \multimap !(c) : \cdot \vdash a \quad a, b, !(!(a \& b)) \multimap !(c) : \cdot \vdash b
                               a, b, !(!(a \& b)) \multimap !(c) : \cdot \vdash a \& b
                            a, b, !(!(a \& b)) \multimap !(c) : \vdash !(a \& b)!
                                                                                                                                                        \frac{\overline{a,b,c,!(!(a \& b)) \multimap !(c) : \cdot \vdash c}}{a,b,!(!(a \& b)) \multimap !(c) : \cdot !(c) \vdash c} \ \star
                          a, b, !(!(a \& b)) \multimap !(c) : \cdot \vdash !(!(a \& b))!
                                                                         (c): ((a \& b)) \multimap ((c)) : (((a \& b)) \multimap ((c)) \vdash c
(b)
                                                                                         a, b, !(!(a \& b)) \multimap !(c) : \cdot \vdash c
                                                                                       \overline{a,!(!(a \& b)) \multimap !(c) : \cdot \vdash !(b) \multimap c}
                                                                              \frac{a,!(!(a \& b)) \multimap !(c) : \cdot \vdash !(!(b) \multimap c)}{!(!(a \& b)) \multimap !(c) : \cdot \vdash !(a) \multimap !(!(b) \multimap c)} *
                                                                           \frac{(((a \& b)) - ((c) : \cdot \vdash (((a) - \circ (((b) - \circ c)))))}{!(!(a \& b)) - \circ !(c) : \cdot \vdash !(!(a) - \circ !(!(b) - \circ c)))}!
                                                                         \cdot : !(!(!(a \& b)) \multimap !(c)) \vdash !(!(a) \multimap !(!(b) \multimap c))
 file: KLE/KLE006+1.p (322 ms)
  a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash a
                                                                             a, b, !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash b
a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash !(a) ! a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \vdash b
                               a,!(a) \multimap !(b),!(b) \multimap !(c) : !(a) \multimap !(b) \vdash b
D_C
                                         a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash b
                                                                                                                                                                 a, c, !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash c
                                       \overline{a,!(a)\multimap !(b),!(b)\multimap !(c): \cdot \vdash !(b)}
                                                                                                                                                                a,!(a) \multimap !(b),!(b) \multimap !(c) : !(c) \vdash c
                                                                                             a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \multimap !(c) \vdash c
                                                                                                       a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash c
                                                                                                  \frac{!(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(a) \multimap c}{!}
                                                                                                \overline{!(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(!(a) \multimap c)}
                                                                                          \frac{1}{!(a) \multimap !(b) : \cdot \vdash !(!(b) \multimap !(c)) \multimap !(!(a) \multimap c)} \star
                                                                                        \frac{!(a) \multimap !(b) : \neg \vdash !(!(!(b) \multimap !(c)) \multimap !(!(a) \multimap c))}{!(a) \multimap !(b) : \neg \vdash !(!(!(b) \multimap !(c)) \multimap !(!(a) \multimap c))}
                                                                                       \frac{}{\cdot : !(!(a) \multimap !(b)) \vdash !(!(!(b) \multimap !(c)) \multimap !(!(a) \multimap c))} 
file: KLE/KLE007+1.p (289 ms)
  c, !(a) \multimap !(b), !(c) \multimap \overline{!(a) : \cdot \vdash c}
                                                                             a, c, !(a) \multimap !(b), !(c) \multimap !(a) : \cdot \vdash a
\frac{c,!(a) - \circ !(b),!(c) - \circ !(a) : \cdot \vdash !(c)}{c,!(a) - \circ !(b),!(c) - \circ !(a) : \cdot \vdash !(c)} \cdot \frac{c,!(a) - \circ !(b),!(c) - \circ !(a) : \cdot !(a) \vdash a}{c,!(a) - \circ !(b),!(c) - \circ !(a) : \cdot !(a) \vdash a}
                               c,!(a) \multimap !(b),!(c) \multimap !(a) : !(c) \multimap !(a) \vdash a
D_C
                                         c,!(a) \multimap !(b),!(c) \multimap !(a) : \cdot \vdash a
                                                                                                                                                                  \overline{b,c,!(a)} \multimap !(b),!(c) \multimap !(a) : \cdot \vdash \overline{b}
                                        \overline{c,!(a)\multimap!(b),!(c)\multimap!(a):\cdot\vdash!(a)}
                                                                                                                                                                 c,!(a) \multimap !(b),!(c) \multimap !(a) : !(b) \vdash b
                                                                                             c,!(a) \multimap !(b),!(c) \multimap !(a) : !(a) \multimap !(b) \vdash b
                                                                                                       c,!(a) \multimap !(b),!(c) \multimap !(a) : \cdot \vdash b
                                                                                                  \frac{!(a)\multimap !(b),!(c)\multimap !(a): \cdot \vdash !(c)\multimap b}{}
                                                                                               \frac{1}{!(a)\multimap !(b),!(c)\multimap !(a): \cdot \vdash !(!(c)\multimap b)}!
                                                                                           \frac{!(a) \multimap !(b) : \cdot \vdash !(!(c) \multimap !(a)) \multimap !(!(c) \multimap b)}{!}
                                                                                        \frac{!(a) \multimap !(b) : \cdot \vdash !(!(!(c) \multimap !(a)) \multimap !(!(c) \multimap b))}{!(a) \multimap !(b) : \cdot \vdash !(!(!(c) \multimap !(a)) \multimap !(!(c) \multimap b))}
                                                                                       \frac{}{\cdot : !(!(a) \multimap !(b)) \vdash !(!(!(c) \multimap !(a)) \multimap !(!(c) \multimap b))}
```

file: KLE/KLE008+1.p (226 ms)

```
\frac{\overline{a,c,!(a)\multimap!(b): \cdot \vdash a}}{a,c,!(a)\multimap!(b): \cdot \vdash !(a)} \; ! \; \frac{\overline{a,b,c,!(a)\multimap!(b): \cdot \vdash b}}{a,c,!(a)\multimap!(b): \; !(b)\vdash b} \; \star
                                                         \frac{a, c, !(a) \multimap !(b) : !(a) \multimap !(b) \vdash b}{a, c, !(a) \multimap !(b) : \cdot \vdash b} D_C
                                                                                                                                                                                                                                                                                                                        \overline{a,c,!(a)\multimap !(b):} \vdash c
                                                                                                                                                \frac{a, c, !(a) \multimap !(b) : \cdot \vdash b \& c}{a, c, !(a) \multimap !(b) : \cdot \vdash !(b \& c)} !
\frac{!(a) \multimap !(b) : \cdot \vdash !(!(a) \& !(c)) \multimap !(b \& c)}{!(a) \multimap !(b) : \cdot \vdash !(!(!(a) \& !(c)) \multimap !(b \& c))} *
                                                                                                                                           : !(!(a) \multimap !(b)) \vdash !(!(!(a) \& !(c)) \multimap !(b \& c))
  file: KLE/KLE009+1.p (266 ms)
                                                                                                                                                            \overline{a,b,c,!(a)\multimap !(b): \cdot \vdash c} \quad \overline{a,b,c,!(a)}\multimap !(b): \cdot \vdash b
                                                                                                                                                                                                            \frac{a, b, c, !(a) \multimap !(b) : \cdot \vdash c \& b}{a, b, c, !(a) \multimap !(b) : \cdot \vdash !(c \& b)} !
a, c, !(a) \multimap !(b) : !(b) \vdash !(c \& b)
\frac{\overline{a, c, !(a) \multimap !(b) : \cdot \vdash a}}{a, c, !(a) \multimap !(b) : \cdot \vdash !(a)} !
                                                                                    a, c, !(a) \multimap !(b) : !(a) \multimap !(b) \vdash !(c \& b)
D_C
                                                                   \frac{a, c, !(a) \multimap !(b) : \cdot \vdash !(c \& b)}{a, c, !(a) \multimap !(b) : \cdot \vdash !(c \& b)} D_{C}
\frac{!(a) \multimap !(b) : \cdot \vdash !(!(c) \& !(a)) \multimap !(c \& b)}{!(a) \multimap !(b) : \cdot \vdash !(!(!(c) \& !(a)) \multimap !(c \& b))} !
\cdot : !(!(a) \multimap !(b)) \vdash !(!(!(c) \& !(a)) \multimap !(c \& b))
  file: KLE/KLE010+1.p (511 ms)
                                                                                                            | Companies | Comp
   file: KLE/KLE011+1.p (300 ms)
                                                                                                                                                                                                                                                                                                           a, b, !(c) \oplus !(a), !(a) \multimap !(b) : \cdot \vdash b
                                                                                                                                                                                                                                                                                                       \overline{a, b, !(c) \oplus !(a), !(a) \multimap !(b) : \cdot \vdash !(b)}
                                                                                                                                                                a,!(c) \oplus !(a),!(a) \multimap !(b) : \cdot \vdash a
                                                                                                                                                                                                                                                                                             \overline{a, b, !(c) \oplus !(a), !(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)}
                                                                                                                                                                                                                                                                                           a,!(c) \oplus !(a),!(a) \multimap !(b) : !(b) \vdash !(c) \oplus !(b)
               c, !(c) \oplus !(a), !(a) \multimap !(b) : \cdot \vdash c
                                                                                                                                                            a,!(c) \oplus !(a),!(a) \multimap !(b) : \cdot \vdash !(a)
            \overline{c,!(c)\oplus!(a),!(a)\multimap!(b):\ \cdot\vdash!(c)}
                                                                                                                                                                                                               a,!(c) \oplus !(a),!(a) \multimap !(b) : \ !(a) \multimap !(b) \vdash !(c) \oplus !(b)
  c, !(c) \oplus !(a), !(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)
                                                                                                    !(c) \oplus !(a), !(a) - \circ !(b) : !(c) \oplus !(a) \vdash !(c) \oplus !(b) \atop D_C
                                                                                                                    !(c) \oplus !(a), !(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)
                                                                                                            \overline{!(a)\multimap !(b): \ \cdot \vdash !(!(c)\oplus !(a))\multimap !(c)\oplus !(b)}
                                                                                                       \frac{!(a) \multimap !(b) : \cdot \vdash !(!(!(c) \oplus !(a)) \multimap !(c) \oplus !(b))}{!(a) \multimap !(b) : \cdot \vdash !(!(!(c) \oplus !(a)) \multimap !(c) \oplus !(b))}
                                                                                                   \vdots !(!(a) \multimap !(b)) \vdash !(!(!(c) \oplus !(a)) \multimap !(c) \oplus !(b))
```

file: KLE/KLE012+1.p (213 ms)

```
a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash a
\frac{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(a)}{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(a)} ! \frac{a,!(a) \multimap !(\mathbf{0}) : \cdot !(\mathbf{0}) \vdash b}{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash b} \star
                                              \overline{a,!(a)\multimap !(\mathbf{0}): !(a)\multimap !(\mathbf{0})\vdash b}
                                                                       \overline{a,!(a)\multimap !(\mathbf{0}): \cdot \vdash b}
                                                           \frac{!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(a) \multimap b}{} \quad \star
                                               \frac{\frac{!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(!(a) \multimap b)}{!}!}{\cdot : !(!(a) \multimap !(\mathbf{0})) \vdash !(!(a) \multimap b)} \star
 file: KLE/KLE013+1.p (timeout!)
 file: KLE/KLE014+1.p (44 ms)
\frac{\frac{b: \cdot \vdash !(a) \multimap b}{b: \cdot \vdash !(!(a) \multimap b)}^{\star}}{\vdots : !(b) \vdash !(!(a) \multimap b)}
 file: KLE/KLE015+1.p (timeout!)
  file: KLE/KLE016+1.p (251 ms)
                                                                         a, b, !(a) \multimap !(!(b) \multimap !(\mathbf{0})), !(b) \multimap !(\mathbf{0}) : \cdot \vdash b
                                                                      \frac{a, 0, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) \cdots (b) \cdots (b)}{a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) \cdots \vdash !(b)} ! \frac{a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) \cdots !(0) \cdots (b)}{a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) \cdots !(b) \cdots (b)} 
                                                                                                              \overline{a,b,!(a)\multimap !(!(b)\multimap !(\mathbf{0})): \ \cdot \vdash a}
                                                                                                                       a, b, !(a) \multimap !(!(b) \multimap !(\mathbf{0})), !(b) \multimap !(\mathbf{0}) : \cdot \vdash \mathbf{0}
 \overline{a,b,!(a)\multimap !(!(b)\multimap !(\mathbf{0})): \cdot \vdash !(a)}
                                                                                                                      \frac{a, b, !(a) - !(!(b) - !(\mathbf{0})) : !(a) - !(!(b) - !(\mathbf{0})) \vdash \mathbf{0}}{D_C}
                                                                      a, b, !(a) \multimap !(!(b) \multimap !(\mathbf{0})) : \cdot \vdash \mathbf{0}
                                                                   \overline{b,!(a)\multimap !(!(b)\multimap !(\mathbf{0})): \cdot \vdash !(a)\multimap \mathbf{0}}
                                                                 b,!(a) \multimap !(!(b) \multimap !(\mathbf{0})) : \cdot \vdash !(!(a) \multimap \mathbf{0}) !
                                                         \frac{\frac{!(a) \multimap !(!(b) \multimap !(0)) : \ \vdash !(b) \multimap !(!(a) \multimap 0)}{!(a) \multimap !(!(b) \multimap !(0)) : \ \vdash !(!(b) \multimap !(!(a) \multimap 0))}}{!(a) \multimap !(!(b) \multimap !(0)) : \ \vdash !(!(b) \multimap !(!(a) \multimap 0))}
                                                         \frac{}{\cdot : \ !(!(a) \multimap !(!(b) \multimap !(\mathbf{0}))) \vdash !(!(b) \multimap !(!(a) \multimap \mathbf{0}))} 
  file: KLE/KLE017+1.p (timeout!)
  file: KLE/KLE018+1.p (499 ms)
```

file: KLE/KLE019+1.p (329 ms)

```
\frac{\overline{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}}{\underbrace{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)}} : \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : !(b) \vdash b}} \star \underbrace{\frac{\overline{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)}}}_{\underbrace{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)}} : \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)}} : \underbrace{\frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}}_{\underbrace{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}_{\underbrace{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}} : \underbrace{\frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}}_{\underbrace{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}_{\underbrace{b,!(a) \multimap !(b),!(b) \multimap
                                                    a,!(a) \multimap !(b),!(\underline{b}) \multimap !(a) : !(a) \multimap !(b) \vdash \underline{b}
D_C
                                                                                                                                                                                                                                                                                                                             b,!(a) \multimap !(b),!(\underline{b}) \multimap !(a) : !(b) \multimap !(a) \vdash \underline{a}
D_C
                                                                   a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b
                                                                                                                                                                                                                                                                                                                                             b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a
                                                             \overline{!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash !(a)\multimap b}
                                                                                                                                                                                                                                                                                                                                       !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(b) \multimap a
                                                          \frac{!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(!(a)\multimap b)}{}
                                                                                                                                                                                                                                                                                                                                   \frac{!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(!(b)\multimap a)}{}
                                                                                                                                                                       !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(a) \multimap b) \& !(!(b) \multimap a)
                                                                                                                                                                    \frac{1}{!(a) \multimap !(b), !(b) \multimap !(a) :} \vdash !(!(!(a) \multimap b) \& !(!(b) \multimap a)) !
                                                                                                                                                           : !(!(a) \multimap !(b)), !(!(b) \multimap !(a)) \vdash !(!(!(a) \multimap b) \& !(!(b) \multimap a))
   file: KLE/KLE020+1.p (250 ms)
\frac{\overline{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)} ! \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot !(b) \vdash b} \star
                                                                                                          a, !(a) \multimap !(b), !(b) \multimap !(a) : !(a) \multimap !(b) \vdash b
                                                                                                                           \frac{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}{!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a) \multimap b} \star
                                                                                                         \frac{\frac{!(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(a) \multimap b)}{!(!(!(a) \multimap !(b)) \& !(!(b) \multimap !(a))) \vdash !(!(a) \multimap b)} *
 file: KLE/KLE021+1.p (235 ms)
\frac{\overline{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)} \; ! \quad \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \; !(a) \vdash a} \; \star
                                                                                                        b,!(a) \multimap !(b),!(b) \multimap !(a) : !(b) \multimap !(a) \vdash a
                                                                                                                                            b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a
                                                                                                                  \frac{!(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(b) \multimap a}{!(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(b) \multimap a)} !
                                                                                    \cdot : !(!(!(a) \multimap !(b)) \& !(!(b) \multimap !(a))) \vdash !(!(b) \multimap a) 
 file: KLE/KLE022+1.p (239 ms)
\frac{\overline{a,!(a)\multimap !(b),!(b)\multimap !(a): \, \cdot \vdash a}}{a,!(a)\multimap !(b),!(b)\multimap !(a): \, \cdot \vdash !(a)} \; ! \quad \overline{\frac{a,b,!(a)\multimap !(b),!(b)\multimap !(a): \, \cdot \vdash b}{a,!(a)\multimap !(b),!(b)\multimap !(a): \, !(b)\vdash b}} \; \star
                                                                                                        \frac{a,!(a) \multimap !(b),!(b) \multimap !(a) : !(a) \multimap !(b) \vdash b}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b} D_C
                                                                                                     : !(a), !(!(!(a) \multimap !(b)) \& !(!(b) \multimap !(a))) \vdash b
```

file: KLE/KLE023+1.p (253 ms)

```
\frac{\overline{b,!(a)\multimap!(b),!(b)\multimap!(a): \cdot \vdash b}}{b,!(a)\multimap!(b),!(b)\multimap!(a): \cdot \vdash !(b)} \quad ! \quad \frac{\overline{a,b,!(a)\multimap!(b),!(b)\multimap!(a): \cdot \vdash a}}{b,!(a)\multimap!(b),!(b)\multimap!(a): \cdot \vdash a} \quad \star
                                                            \frac{b,!(a) \multimap !(b),!(b) \multimap !(a) : !(b) \multimap !(a) \vdash a}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a} D_C
                                                         \overline{ : : !(b), !(!(!(a) \multimap !(b)) \& !(!(b) \multimap !(a))) \vdash a }
file: KLE/KLE024+1.p (45 ms)

\frac{a : \cdot \vdash a}{\cdot : \cdot \vdash !(a) \multimap a} \star \frac{a : \cdot \vdash a}{\cdot : \cdot \vdash !(a) \multimap a} 

\vdots \cdot \vdash !(!(a) \multimap a) ! \frac{\cdot : \cdot \vdash !(a) \multimap a}{\cdot : \cdot \vdash !(!(a) \multimap a)}

                              \cdot : \cdot \vdash !(!(a) \multimap a) \& !(!(a) \multimap a)
                                             \cdot \vdash !(!(!(a) \multimap a) \& !(!(a) \multimap a))
 file: KLE/KLE025+1.p (314 ms)
                                                                                                                                                       \frac{\overline{a,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash a}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash !(a)} \ ! \ \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash b}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \ !(b) \vdash b}
  \overline{b,!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash b}
                                                                         \overline{a,b,!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash a}
\frac{b,!(a) \multimap !(b),!(b) \multimap !(a) : \, \cdot \vdash b}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \, \cdot \vdash !(b)} \; ! \; \frac{a, b, :(a) \multimap :(b), :(b) \multimap :(a) \cdot \quad \cdot \quad a}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \, !(a) \vdash a} \; \star \\ \underset{\frown}{} \; \bullet
                              b,!(a) \xrightarrow{-\circ !(b),!(b) \xrightarrow{-\circ !(a) : !(b) \xrightarrow{-\circ !(a) \vdash a}} D_C
                                                                                                                                                                                      \frac{a,!(a) - 0!(b),!(b) - 0!(a) : !(a) - 0!(b) \vdash b}{a,!(a) - 0!(b),!(b) - 0!(a) : \cdot \vdash b} D_C
\frac{[(a) - 0!(b),!(b) - 0!(a) : \cdot \vdash !(a) - 0]}{[(a) - 0!(b),!(b) - 0!(a) : \cdot \vdash !(a) - 0]} \star
                                    b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a
\star \star
                                   \frac{}{!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(b)\multimap a}
                                 \underline{!(a) \multimap !(b), !(b) \multimap !(a)} : \cdot \vdash !(!(b) \multimap a) !
                                                                                                                                                                                          \overline{!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(!(a)\multimap b)}
                                                                                                \frac{!(a) \multimap !(b), !(b) \multimap !(a) : \ \vdash !(!(b) \multimap a) \& !(!(a) \multimap b)}{!(a) \multimap !(b), !(b) \multimap !(a) : \ \vdash !(!(b) \multimap a) \& !(!(a) \multimap b)} 
                                                                                              \frac{!(a) \multimap !(b), !(b) \multimap !(a) : \ \cdot \vdash !(!(!(b) \multimap a) \& !(!(a) \multimap b))}{!(a) \multimap !(b), !(b) \multimap !(a) : \ \cdot \vdash !(!(!(b) \multimap a) \& !(!(a) \multimap b))}
                                                                                     \frac{}{ \cdot : \ !(!(!(a) \multimap !(b)) \& !(!(b) \multimap !(a))) \vdash !(!(!(b) \multimap a) \& !(!(a) \multimap b))} \overset{\star}{} 
 file: KLE/KLE026+1.p (615 ms)
  file: KLE/KLE027+1.p (4392 ms)
 file: KLE/KLE028+1.p (468 ms)
```

```
file: KLE/KLE029+1.p (788 ms)
      file: KLE/KLE032+1.p (425 ms)
      file: KLE/KLE033+1.p (904 ms)
      file: KLE/KLE034+1.p (405 ms)
                                                                                                                                                                                                                                                                                   !(a) \multimap !(b) \vdash b
!(a) \multimap !(b) \vdash b
!(a) \multimap !(b) \vdash b
                                                                                                                                                                                                                                                                         \begin{array}{c} (a) : \vdash b & a, c, (a) \multimap (b), (b) \multimap (a) : \vdash b \& c \\ \hline a, c, ((a) \multimap (b), (b) \multimap (a) : \vdash b \& c \\ \hline a, c, ((a) \multimap (b), (b) \multimap (a) : \vdash (b \& c) \\ \hline ((a) \multimap (b), (b) \multimap (a) : \vdash ((a) \& (c)) \multimap ((b \& c) \\ \end{array} \right)^{\star} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \begin{array}{c} b, c, !(a) \multimap !(b), !(b) \multimap !(a) : \, \vdash a \& c \\ b, c, !(a) \multimap !(b), !(b) \multimap !(a) : \, \vdash a \& c \\ b, c, !(a) \multimap !(b), !(b) \multimap !(a) : \, \vdash !(a \& c) \\ \end{array} \\ \begin{array}{c} !(a) \multimap !(b), !(b) \multimap !(a) : \, \vdash !(b) \& !(c)) \multimap !(a \& c) \\ \end{array} \\ \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \begin{array}{c} (a) = (b) \cdot (b \cdot k \cdot c) \cdot (1 \cdot k \cdot c)
         file: KLE/KLE035+1.p (391 ms)
                                                                                                                                                                                                                                                                                                                                                       \begin{array}{l} a,b,c,!(a) \multimap !(b),!(b) \multimap !(a): \ \vdash c \& b \\ \hline a,b,c,!(a) \multimap !(b),!(b) \multimap !(a): \ \vdash !(c \& b) \\ \hline a,c,!(a) \multimap !(b),!(b) \multimap !(a): \ !(b) \vdash !(c \& b) \end{array} \\ \star
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              \frac{a,b,c,!(a) \multimap !(b),!(b) \multimap !(a): \ \vdash c \& a}{a,b,c,!(a) \multimap !(b),!(b) \multimap !(a): \ \vdash !(c \& a)} \stackrel{!}{\underset{b,c,!(a) \multimap !(b),!(b) \multimap !(a): \ !(a) \vdash !(c \& a)}{}} \times \\
\frac{\overline{a,c,!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash a}}{\overline{a,c,!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash !(a)}}
                                                                                                                                                                                     \begin{array}{l} (a) - 0!(b), !(b) - 0!(a) : !(a) - 0!(b) \vdash !(c \& b) \\ a, c, !(a) - 0!(b), !(b) - 0!(a) : \cdot \vdash !(c \& b) \\ \hline o!(b), !(b) - 0!(a) : \cdot \vdash !(c \& b) \\ \hline o!(b), !(b) - 0!(a) : \cdot \vdash !(l(c \& l(a)) - 0!(c \& b) \\ \end{array} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         \begin{array}{lll} b, c, !(a) - 0!(b), !(b) - 0!(a) : !(b) - 0!(a) ! !(c \& a) \\ b, c, !(a) - 0!(b), !(b) - 0!(a) : \cdot + !(c \& a) \\ b, c, !(a) - 0!(b), !(b) - 0!(a) : \cdot + !(c \& a) \\ \end{array} \begin{array}{lll} D_C \\ \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(!(c) \& !(b)) \multimap !(c \& a))
                                                                                                                                           !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(!(c) \& !(a)) \multimap !(c \& b))
                                                                                                                                                                                                                                                                                                                                                                                          \frac{!(a) - 0!(b).!(b) - 0!(a) : \cdot + !(!(!(c) \& !(a)) - 0!(c \& b)) \& !(!(!(c) \& !(b)) - 0!(c \& a))}{!(a) - 0!(b).!(b) - 0!(a) : \cdot + !(!(!(!(c) \& !(a)) - 0!(c \& b)) \& !(!(!(c) \& !(b)) - 0!(c \& a)))} ! \\ - : : !(!(!(a) - 0!(b)) \& !(!(b) - 0!(a))) + !(!(!(!(c) \& !(a)) - 0!(c \& b)) \& !(!(!(c) \& !(b)) - 0!(c \& a)))} * 
      file: KLE/KLE036+1.p (3524 ms)
      file: KLE/KLE037+1.p (728 ms)
```

9

```
file: KLE/KLE038+1.p (1953 ms)
 file: KLE/KLE039+1.p (135 ms)
                                                                                                                                                                                                           \frac{a,b,c: \cdot \vdash a}{a,b,c: \cdot \vdash a \& b}
                                                                             a, b, c: \cdot \vdash b \quad a, b, c: \cdot \vdash c
                                                                                              a, b, c: \cdot \vdash b \& c
                                                                                                                                                                                                                          \overline{a,b,c: \cdot \vdash !(a \& b)}!
                                                                                 \overline{a,b,c: \cdot \vdash !(b \& c)}
                  \overline{a,b,c: \cdot \vdash a}
                                               a,b,c: \cdot \vdash a \& !(b \& c)
                                                                                                                                                                                                                                                           a,b,c: \cdot \vdash !(a \& b) \& c
                                          a, b, c: \cdot \vdash !(a \& !(b \& c))
                                                                                                                                                                                                                                                       a, b, c : \cdot \vdash !(!(a \& b) \& c)
      \frac{}{\cdot : \cdot \vdash !(!(a) \& !(!(b) \& !(c))) \multimap !(!(a \& b) \& c)} 
\overline{\cdot : \cdot \vdash !(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c)))}!
                                                                                                                                                                                                       \cdots \vdash !(!(!(a) \& !(!(b) \& !(c))) \multimap !(!(a \& b) \& c))
               \cdot : \; \cdot \vdash !(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c))) \& !(!(!(a) \& !(!(b) \& !(c))) \multimap !(!(a \& b) \& c)))
            \frac{}{\cdot : \cdot \vdash !(!(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c))) \& !(!(!(a) \& !(!(b) \& !(c))) \multimap !(!(a \& b) \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(!(a) \& !(b)) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(b) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(b) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(!(b) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(b) \& !(c)) \multimap !(a \& !(b \& c)))} \overset{!}{\cdot : \cdot \vdash !(!(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(b) \& !(c))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(b) \& !(b) \& !(b) \& !(b))} \overset{!}{\cdot : \cdot \vdash !(b \& !(b) \& !(
file: KLE/KLE040+1.p (1356 ms)
file: KLE/KLE041+1.p (105 ms)
                                                                                                                                                                                                                                   \frac{\overline{a,b: \cdot \vdash a} \quad \overline{a,b: \cdot \vdash b}}{\frac{a,b: \cdot \vdash a \& b}{a,b: \cdot \vdash !(a \& b)}} \quad \star
                        \frac{\overline{a,b}: \cdot \vdash \overline{b} \quad \overline{a,b}: \cdot \vdash \overline{a}}{\underline{a,b}: \cdot \vdash \overline{b} \& \overline{a}}
                                          \overline{a,b: \cdot \vdash !(b \& a)}
 \frac{\frac{(a,b) + (a,b)}{(a,b) + (a,b)}}{\frac{(a,b) + (a,b)}{(a,b) + (a,b)}} * \frac{\frac{(a,b) + (a,b)}{(a,b)}}{\frac{(a,b) + (a,b)}{(a,b)}} !
                     \overline{\cdot : \cdot \vdash !(!(!(!(a) \& !(b)) \multimap !(b \& a)) \& !(!(!(b) \& !(a)) \multimap !(a \& b)))}
file: KLE/KLE042+1.p (323 ms)
```

```
a,!(a) \oplus !(b) : \cdot \vdash a
                                                               \overline{b,!(a)\oplus!(b):\cdot\vdash b}
    \frac{a,!(a)\oplus !(b): \cdot \vdash !(a)}{a,!(a)\oplus !(b): \cdot \vdash !(a)} !
                                                             b, !(a) \oplus !(b) : \cdot \vdash !(b)
                                                                                                                     \overline{b,!(b)\oplus!(a):\cdot\vdash!(b)}
\frac{1}{a,!(a)\oplus !(b): \ \cdot \vdash !(b)\oplus !(a)} \oplus_1 \frac{1}{b,!(a)\oplus !(b): \ \cdot \vdash !(b)\oplus !(a)}
                                                                                                                b,!(b)\oplus!(a): \cdot \vdash !(a)\oplus!(b) \oplus 1
                      !(a) \oplus !(b) : \ !(a) \oplus !(b) \vdash !(b) \oplus !(a)
                                                                                                                                      !(b) \oplus !(a): \ !(b) \oplus !(a) \vdash !(a) \oplus !(b)
                              !(a) \oplus !(b) : \cdot \vdash !(b) \oplus !(a)
                                                                                                                                              !(b) \oplus !(a) : \cdot \vdash !(a) \oplus !(b)
                         \frac{}{\cdot : \cdot \vdash !(!(a) \oplus !(b)) \multimap !(b) \oplus !(a)} 
                                                                                                                                          \overline{ \cdot : \cdot \vdash !(!(b) \oplus !(a)) \multimap !(a) \oplus !(b) } 
                       \cdot : \cdot \vdash !(!(!(a) \oplus !(b)) \multimap !(b) \oplus !(a)) \& !(!(!(b) \oplus !(a)) \multimap !(a) \oplus !(b))
                                                     \vdots \cdot \vdash !(!(!(!(a) \oplus !(b)) \multimap !(b) \oplus !(a)) \& !(!(!(b) \oplus !(a)) \multimap !(a) \oplus !(b))) 
 file: KLE/KLE043+1.p (451 ms)
 file: KLE/KLE044+1.p (786 ms)
 file: KLE/KLE045+1.p (83 ms)
                                                                                                                               \frac{\overline{a: \cdot \vdash a} \quad \overline{a: \cdot \vdash a}}{\frac{a: \cdot \vdash a \& a}{a: \cdot \vdash ! (a \& a)}!} \star
                                  a : \cdot \vdash a
\frac{ \vdots \cdot \vdash !(!(a) \& !(a)) \multimap a}{ \vdots \cdot \vdash !(!(a) \& !(a)) \multimap a} * \underbrace{ \vdots \cdot \vdash !(a) \multimap !(a \& a)}_{ \vdots \cdot \vdash !(!(a) \multimap !(a \& a))}
           \frac{\cdot : \cdot \vdash !(!(!(a) \& !(a)) \multimap a) \& !(!(a) \multimap !(a \& a))}{\cdot : \cdot \vdash !(!(!(!(a) \& !(a)) \multimap a) \& !(!(a) \multimap !(a \& a)))} !
file: KLE/KLE046+1.p (94 ms)
```

11

```
\overline{a,!(a)\oplus !(a): \ \cdot \vdash a} \quad \overline{a,!(a)} \oplus !(a): \ \cdot \vdash a \quad \star

\frac{\oplus !(a) : \cdot \vdash a \quad a, !(a) \overline{\oplus !(a) : \cdot \vdash a}}{\overset{!(a) \oplus !(a) : \cdot \vdash a}{\vdots \cdot \vdash !(a) \oplus !(a) : \cdot \vdash a}} \times \frac{\overline{a : \cdot \vdash a}}{a : \cdot \vdash !(a)} ! \\
\frac{\overset{!(a) \oplus !(a) : \cdot \vdash a}{\vdots \cdot \vdash !(!(a) \oplus !(a)) \multimap a}}{\overset{!(a) \oplus !(a) \oplus !(a)}{\vdots \cdot \vdash !(!(a) \oplus !(a)) \multimap a}} ! \\
\frac{\overset{!(a) \oplus !(a) : \cdot \vdash a}{\vdots \cdot \vdash !(a) \oplus !(a)} }{\overset{!(a) \oplus !(a) \oplus !(a)}{\vdots \cdot \vdash !(!(a) \oplus !(a))}} ! \\
\frac{\overset{!(a) \oplus !(a) : \cdot \vdash a}{\vdots \cdot \vdash !(a) \oplus !(a)} }{\overset{!(a) \oplus !(a) \oplus !(a)}{\vdots \cdot \vdash !(a) \oplus !(a)}} ! \\
\frac{\cdot : \cdot \vdash !(!(a) \oplus !(a)) \multimap a}{\vdots \cdot \vdash !(!(a) \oplus !(a)) \multimap a} ! \\
\frac{\cdot : \cdot \vdash !(!(a) \oplus !(a)) \multimap a}{\vdots \cdot \vdash !(a) \oplus !(a)} !

                                                                                                                                                                                                                                          \frac{}{\cdot : \cdot \vdash !(!(!(!(a) \oplus !(a)) \multimap a) \& !(!(a) \multimap !(a) \oplus !(a)))} 
       file: KLE/KLE047+1.p (96 ms)
\frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash a} \stackrel{!}{\underbrace{a: \cdot \vdash a}} \stackrel{!}{\underbrace{a: \cdot \vdash a}} \stackrel{!}{\underbrace{a: \cdot \vdash a}} \stackrel{!}{\underbrace{a: \cdot \vdash a}} \stackrel{!}{\underbrace{a: \cdot \vdash a \otimes !(a) \oplus !(b)}} \stackrel{!}{\underbrace{a: \cdot \vdash !(a \otimes !(a) \oplus !(b))}} \stackrel{!}{\underbrace{a: \cdot \vdash !(a) \oplus !(a) \oplus !(b)}} \stackrel{!}{\underbrace{a: \cdot \vdash !(a) \oplus !(a) \oplus !(b)}} \stackrel{!}{\underbrace{a: \cdot \vdash !(a) \oplus !(a) \oplus !(b)}} \stackrel{!}{\underbrace{a: \cdot \vdash !(a) \oplus !(a) \oplus !(a) \oplus !(a) \oplus !(a)}}} \stackrel{!}{\underbrace{a: \cdot \vdash !(a) \oplus !(a) \oplus !(a) \oplus !(a)}} \stackrel{!}{\underbrace{a: \cdot \vdash \vdash !(a) \oplus !(a) \oplus !(a) \oplus !(a)}}} \stackrel{
                                                                     \cdot : \cdot \vdash !(!(!(a) \& !(!(a) \oplus !(b))) \multimap a) \& !(!(a) \multimap !(a \& !(a) \oplus !(b)))
                                                     \cdot : \cdot \vdash !(!(!(!(a) \& !(!(a) \oplus !(b))) \multimap a) \& !(!(a) \multimap !(a \& !(a) \oplus !(b)))) 
         file: KLE/KLE048+1.p (102 ms)
   \overline{a,!(a)\oplus !(!(a)\ \&\ !(b)):\ \cdot\vdash\underline{a}}\quad \underline{a,b,!(a)\oplus !(!(a)\ \&\ !(b)):\ \cdot\vdash a}\quad \star
                                                                                                \frac{\frac{\exists : (!(a) \& !(b)) : \cdot \vdash a \quad a, b, !(a) \oplus !(!(a) \& !(b)) : \cdot \vdash a}{!(a) \oplus !(!(a) \& !(b)) : \cdot \vdash a}}{\frac{!(a) \oplus !(!(a) \& !(b)) : \cdot \vdash a}{!(a) \oplus !(!(a) \& !(b)) : \cdot \vdash a}} \\ \frac{\frac{!(a) \oplus !(!(a) \& !(b)) : \cdot \vdash a}{!(a) \oplus !(!(a) \& !(b)) : \cdot \vdash a}}{\cdot : \cdot \vdash !(!(a) \oplus !(!(a) \& !(b))) \to a} \\ \frac{\frac{\cdot : \cdot \vdash !(a) \oplus !(!(a) \& !(a) \otimes !(b))}{!(a) \oplus !(!(a) \& !(b))} \oplus 1}{\cdot : \cdot \vdash !(!(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(!(a) \oplus !(!(a) \& !(b))) \to a}{\cdot : \cdot \vdash !(!(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(!(a) \oplus !(!(a \& b)))}{\cdot : \cdot \vdash !(!(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(!(a) \oplus !(!(a \& b)))}{\cdot : \cdot \vdash !(!(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b)))}{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b)))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a \& b))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a \& b))} \\ \frac{\cdot : \cdot \vdash !(a) \oplus !(!(a \& b))}{\cdot : \cdot \vdash !(a \& b))} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot : \cdot \vdash !(a \& b)} \\ \frac{\cdot : \cdot \vdash !(a \& b)}{\cdot :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \frac{a: \cdot \vdash a}{a: \cdot \vdash !(a)} !
                                                                                                                                                                                                                                                                                  \overline{\cdot : \cdot \vdash !(!(!(!(a) \oplus !(!(a) \& !(b))) \multimap a) \& !(!(a) \multimap !(a) \oplus !(!(a \& b))))}
       file: KLE/KLE049+1.p (131 ms)
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12

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\frac{\overline{a,!(a) \multimap !(b) : \cdot \vdash a}}{\underbrace{a,!(a) \multimap !(b) : \cdot \vdash !(a)}} ! \frac{\overline{a,b,!(a) \multimap !(b) : \cdot \vdash b}}{a,!(a) \multimap !(b) : \cdot !(b) \vdash b} \star \\ \frac{\underline{a,!(a) \multimap !(b) : \cdot \vdash !(a)}}{\underbrace{a,!(a) \multimap !(b) : \cdot \vdash b}} D_C \\ \frac{\underline{a,!(a) \multimap !(b) : \cdot \vdash b}}{\underline{a: \cdot \vdash !(!(a) \multimap !(b)) \multimap b}} \star \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap !(b)) \multimap b}}{\underline{a: \cdot \vdash !(!(!(a) \multimap !(b)) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}}{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}}{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}}{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}}{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}}{\underline{a: \cdot \vdash !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}}{\underline{a: \cdot \vdash !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(b) \multimap !(!(a) \multimap b))}}{\underline{a: \cdot \vdash !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b))}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(!(a) \multimap b)}}{\underline{a: \cdot \vdash !(!(a) \multimap b)}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) \multimap b}}{\underline{a: \cdot \vdash !(a) \multimap b}} ! \\ \frac{\underline{a: \cdot \vdash !(a) 
                                                                                                                                                                                    \frac{a: \cdot \vdash !(!(!(a) \multimap !(b)) \multimap b) \& !(!(b) \multimap !(!(a) \multimap b))}{a: \cdot \vdash !(!(!(!(a) \multimap !(b)) \multimap b) \& !(!(b) \multimap !(!(a) \multimap b)))} !
                                                                                                                                                                           \cdot : !(a) \vdash !(!(!(!(a) \multimap !(b)) \multimap b) \& !(!(b) \multimap !(!(a) \multimap b)))
     file: KLE/KLE050+1.p (88 ms)
 \frac{\overline{a,b:\cdot\vdash b}}{b:\cdot\vdash!(a)\multimap b} \star \\ \frac{\overline{b,!(a)\multimap!(b):\cdot\vdash b}}{b:\cdot\vdash!(!(a)\multimap!(b))\multimap b} \star \\ \frac{\overline{b:\cdot\vdash!(!(a)\multimap b)}}{b:\cdot\vdash!(!(a)\multimap!(b))\multimap b} ! \\ \frac{\overline{b:\cdot\vdash!(!(a)\multimap b)}}{b:\cdot\vdash!(!(a)\multimap b)} !
                                     \frac{b: \cdot \vdash !(!(!(a) \multimap !(b)) \multimap b) \& !(!(b) \multimap !(!(a) \multimap b))}{b: \cdot \vdash !(!(!(!(a) \multimap !(b)) \multimap b) \& !(!(b) \multimap !(!(a) \multimap b)))} !
                       : !(b) \vdash !(!(!(!(a) \multimap !(b)) \multimap b) \& !(!(b) \multimap !(!(a) \multimap b))
        file: KLE/KLE051+1.p (319 ms)
          a,!(a) \multimap !(b),!(a) \multimap !(\mathbf{0}) : \cdot \vdash a
                                                                                                                                                                                                                                                                                                                                                                                                                                                             a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash a
   \frac{a,!(a) \multimap !(b),!(a) \multimap !(b) : + a}{a,!(a) \multimap !(b),!(a) \multimap !(b) : + !(a)} ! \frac{a,!(a) \multimap !(b),!(a) \multimap !(b) : !(b) \vdash b}{a,!(a) \multimap !(b) : !(b) \vdash b} *
                                                                                          a, !(a) \multimap !(b), !(a) \multimap !(\mathbf{0}) : !(a) \multimap !(\mathbf{0}) \vdash \mathbf{0}
D_C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           \frac{a,!(a) \multimap !(\mathbf{0}) : \ !(a) \multimap !(\mathbf{0}) \vdash b}{a,!(a) \multimap !(\mathbf{0}) : \ \vdash b} \ D_C
                                                                                                                  a,!(a) \multimap !(b),!(a) \multimap !(\mathbf{0}) : \cdot \vdash \mathbf{0}
                                                                                                         \frac{!(a)\multimap !(b),!(a)\multimap !(\mathbf{0}): \cdot \vdash !(a)\multimap \mathbf{0}}{!(a)\multimap !(b),!(a)\multimap !(b): \cdot \vdash !(a)\multimap \mathbf{0}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           \frac{!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(a) \multimap b}{}
                                                                                                   \frac{!(a) \multimap !(b), !(a) \multimap !(\mathbf{0}) : \ \vdash !(!(a) \multimap \mathbf{0})}{!(a) \multimap !(b), !(a) \multimap !(b) : \ \vdash !(!(a) \multimap \mathbf{0})}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \frac{1}{!(a)\multimap !(\mathbf{0}): \cdot \vdash !(!(a)\multimap b)} !
```

file: KLE/KLE052+1.p (414 ms)

 $\frac{!(a)\multimap !(\mathbf{0}): \cdot \vdash !(!(a)\multimap !(b))\multimap !(!(a)\multimap \mathbf{0})}{}$

 $\frac{!(a) \multimap !(\mathbf{0}) : \ \cdot \vdash !(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap \mathbf{0}))}{!(a) \multimap !(b)}$

 $\frac{!(a) \multimap !(0) : \, \, \vdash !(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap 0)) \, \& \, !(!(!(a) \multimap !(0)) \multimap !(!(a) \multimap b))}{!(a) \multimap !(0) : \, \, \vdash !(!(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap 0)) \, \& \, !(!(!(a) \multimap !(0)) \multimap !(!(a) \multimap b)))} \; !}{: \; \, !(!(a) \multimap !(0)) \vdash !(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap 0)) \, \& \, !(!(!(a) \multimap !(0)) \multimap !(!(a) \multimap b)))} \; \star$

 $\frac{!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(!(a) \multimap !(\mathbf{0})) \multimap !(!(a) \multimap b)}{}$

 $!(a) \multimap !(0) : \cdot \vdash !(!(!(a) \multimap !(0)) \multimap !(!(a) \multimap b))$

```
file: KLE/KLE053+1.p (93 ms)
                                                                              \overline{a,b: \cdot \vdash a} \quad \overline{a,b: \cdot \vdash b}
                                                                                     \frac{a,b: \cdot \vdash a \& b}{a,b: \cdot \vdash !(a \& b)} !
                    \overline{a,b: \cdot \vdash a}
\frac{\overline{b: \cdot \vdash !(!(a) \& !(b)) \multimap a}}{\underline{b: \cdot \vdash !(!(!(a) \& !(b)) \multimap a)}} * \frac{\overline{b: \cdot \vdash !(a) \multimap !(a \& b)}}{\underline{b: \cdot \vdash !(!(a) \multimap !(a \& b))}} *
          b: \cdot \vdash !(!(!(a) \& !(b)) \multimap a) \& !(!(a) \multimap !(a \& b))
       \frac{b: \cdot \vdash !(!(!(!(a) \& !(b)) \multimap a) \& !(!(a) \multimap !(a \& b)))}{!} !
    \frac{}{\cdot : !(b) \vdash !(!(!(!(a) \& !(b)) \multimap a) \& !(!(a) \multimap !(a \& b)))}
 file: KLE/KLE054+1.p (94 ms)
```

$$\frac{\frac{\overline{b} : \cdot \vdash b}{b : \cdot \vdash !(b)} !}{\frac{\overline{b} : \cdot \vdash !(b)}{b : \cdot \vdash !(b)} !} \times \frac{\frac{\overline{b} : \cdot \vdash b}{b : \cdot \vdash !(b)} !}{\frac{\overline{b} : \cdot \vdash !(a) \oplus !(b)}{b : \cdot \vdash !(a) \oplus !(b)}} \times \frac{\overline{b} : \cdot \vdash !(!(a) \oplus !(b)) \multimap b}{\frac{\overline{b} : \cdot \vdash !(!(!(a) \oplus !(b)) \multimap b)} !} \times \frac{\overline{b} : \cdot \vdash !(!(!(a) \oplus !(b)) \multimap b)}{\frac{\overline{b} : \cdot \vdash !(!(!(a) \oplus !(b)) \multimap b) \& !(!(b) \multimap !(a) \oplus !(b))}}{\frac{\overline{b} : \cdot \vdash !(!(!(!(a) \oplus !(b)) \multimap b) \& !(!(b) \multimap !(a) \oplus !(b)))} !}{\cdot : \cdot !(b) \vdash !(!(!(!(a) \oplus !(b)) \multimap b) \& !(!(b) \multimap !(a) \oplus !(b)))}} \times$$

file: KLE/KLE055+1.p (265 ms)

```
\frac{\overline{b,!(b)} \multimap !(\mathbf{0}) : \cdot \vdash b}{b,!(b) \multimap !(\mathbf{0}) : \cdot \vdash !(b)} ! \frac{b,!(b) \multimap !(\mathbf{0}) : !(\mathbf{0}) \vdash !(a \& b)}{b,!(b) \multimap !(\mathbf{0}) : !(\mathbf{0}) \vdash !(a \& b)}
                                                                                                                    b,!(b) \multimap !(\mathbf{0}) : !(b) \multimap !(\mathbf{0}) \vdash !(a \& b) \\ D_C
                                                                                                                             \frac{b,!(b) \multimap !(\mathbf{0}) : \ \cdot \vdash !(a \& b)}{!(b) \multimap !(\mathbf{0}) : \ \cdot \vdash !(b) \multimap !(a \& b)}
   \frac{\overline{a,b,!(b)\multimap !(\mathbf{0}): \cdot \vdash b}}{!(b)\multimap !(\mathbf{0}): \cdot \vdash !(!(a) \& !(b))\multimap b} \ \star
!(b) \multimap !(\mathbf{0}) : \vdash !(!(!(a) \& !(b)) \multimap b)
                                                                                                                          !(b) \multimap !(\mathbf{0}) : \cdot \vdash !(!(b) \multimap !(a \& b))
                                  !(b) \multimap !(\mathbf{0}) : \cdot \vdash !(!(!(a) \& !(b)) \multimap b) \& !(!(b) \multimap !(a \& b))
                                \frac{!(b) \multimap !(\mathbf{0}) : \ \cdot \vdash !(!(!(!(a) \& !(b)) \multimap b) \& !(!(b) \multimap !(a \& b)))}{!(b) \multimap !(a \& b))}
                             \cdot : !(!(b) \multimap !(\mathbf{0})) \vdash !(!(!(!(a) \& !(b)) \multimap b) \& !(!(b) \multimap !(a \& b)))
 file: KLE/KLE056+1.p (306 ms)
                                                        \overline{b,!(a)\oplus!(b),!(b)\multimap!(\mathbf{0}):\cdot\vdash b}
                                                      \frac{b,!(a)\oplus!(b),!(b)\multimap!(0): +!(b)}{b,!(a)\oplus!(b),!(b)\multimap!(0): !(0)\vdash a} *
                                                                             \underline{b,!(a)\oplus!(b),!(b)\multimap!(\mathbf{0}):\ !(b)\multimap!(\mathbf{0})\vdash a} \ D_C
                                                                                                                                                                                             \frac{\overline{a,!(b)\multimap !(\mathbf{0}): \ \cdot \vdash a}}{a,!(b)\multimap !(\mathbf{0}): \ \cdot \vdash !(a)}
                                                                                      b,!(a)\oplus !(b),!(b)\multimap !(\mathbf{0}): \cdot \vdash a
\overline{a,!(a)\oplus!(b),!(b)\multimap!(\mathbf{0}): \cdot \vdash a}
                                     !(a) \oplus !(b), !(b) \multimap !(0) : !(a) \oplus !(b) \vdash a \atop D_C
                                                                                                                                                                                        \frac{a,!(b) \multimap !(\mathbf{0}) : \cdot \vdash !(a) \oplus !(b)}{a,!(b) \multimap !(\mathbf{0}) : \cdot \vdash !(a) \oplus !(b)}
                                             !(a) \oplus !(b), !(b) \multimap !(\mathbf{0}) : \cdot \vdash a
                                                                                                                                                                                     \frac{1}{!(b)\multimap !(\mathbf{0}): \cdot \vdash !(a)\multimap !(a)\oplus !(b)}
                                         !(b) \multimap !(\mathbf{0}) : \cdot \vdash !(!(a) \oplus !(b)) \multimap a
                                       !(b) \multimap !(\mathbf{0}) : \cdot \vdash !(!(!(a) \oplus !(b)) \multimap a)
                                                                                                                                                                                   \frac{!(b)\multimap !(\mathbf{0}): \ \cdot \vdash !(!(a)\multimap !(a)\oplus !(b))}{}
                                                                                           !(b) \multimap !(\mathbf{0}) : \cdot \vdash !(!(!(a) \oplus !(b)) \multimap a) \& !(!(a) \multimap !(a) \oplus !(b))
                                                                                         \overline{!(b)\multimap !(\mathbf{0}): \ \cdot \vdash !(!(!(!(a)\oplus !(b))\multimap a) \& !(!(a)\multimap !(a)\oplus !(b)))}
                                                                                        \frac{}{\cdot : \ !(!(b) \multimap !(\mathbf{0})) \vdash !(!(!(!(a) \oplus !(b)) \multimap a) \& !(!(a) \multimap !(a) \oplus !(b)))} 
 file: KLE/KLE057+1.p (87 ms)
     a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash a
\frac{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(a)}{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(a)} ! \frac{a,!(a) \multimap !(\mathbf{0}) : !(\mathbf{0}) \vdash \mathbf{0}}{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash \mathbf{0}}
                                           a,!(a) \multimap !(\mathbf{0}) : !(a) \multimap !(\mathbf{0}) \vdash \mathbf{0}
                                                                  a,!(a) \multimap \overline{!(\mathbf{0}) : \cdot \vdash \mathbf{0}}
                                                       \frac{a : \cdot \vdash !(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0}}{} \star
                                                  \underline{a: \cdot \vdash !(!(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0})}!
                                   \cdot : \cdot \overline{\vdash !(!(a) \multimap !(!(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0}))} !
 file: KLE/KLE058+1.p (497 ms)
```

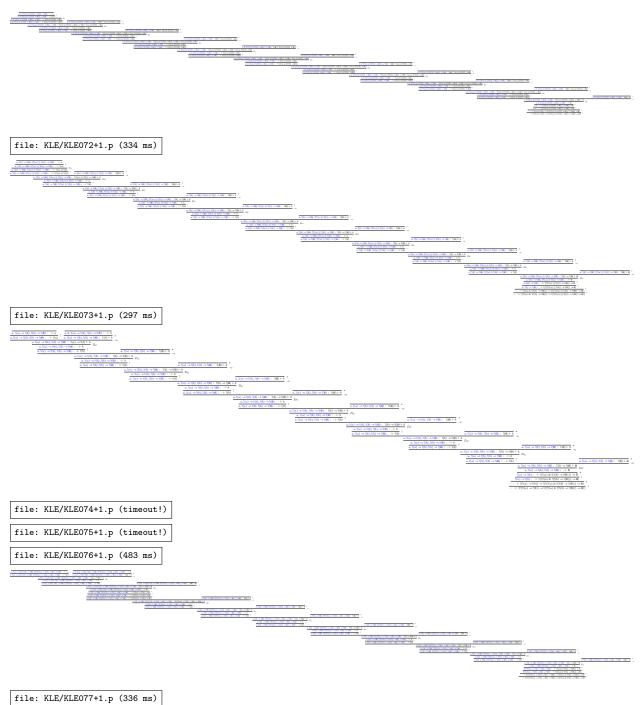
file: KLE/KLE059+1.p (323 ms)

```
\overline{a,!(a)\oplus!(!(a)\multimap!(\mathbf{0})),!(!(!(a)\multimap a))\multimap!(\mathbf{0}): \cdot \vdash a}
      \overline{!(a) \oplus !(!(a) \multimap !(\mathbf{0})), !(!(!(a) \multimap a)) \multimap !(\mathbf{0}) : \cdot \vdash !(a) \multimap a}
   \frac{1}{!(a) \oplus !(!(a) \multimap !(\mathbf{0})), !(!(!(a) \multimap a)) \multimap !(\mathbf{0}) : \ \cdot \vdash !(!(a) \multimap a)} \ !
 \frac{1}{(a)\oplus!(!(a)\multimap!(\mathbf{0})),!(!(!(a)\multimap a))\multimap!(\mathbf{0}): \ \cdot \vdash !(!(!(a)\multimap a))} \ ! \ \overline{(a)\oplus!(!(a)\multimap!(\mathbf{0})),!(!(!(a)\multimap a))\multimap!(\mathbf{0}): \ !(\mathbf{0})\vdash \mathbf{0}} \ ,
                                                      \frac{!(a) \oplus !(!(a) \multimap !(\mathbf{0})), !(!(!(a) \multimap a))}{!(a) \oplus !(!(a) \multimap !(\mathbf{0})), !(!(!(a) \multimap a))} \cdots !(\mathbf{0}) : \ !(!(!(a) \multimap a)) \multimap !(\mathbf{0}) \vdash \mathbf{0}
                                                                           !(a) \oplus !(!(a) \multimap !(\mathbf{0})), !(!(!(a) \multimap a)) \multimap !(\mathbf{0}) : \vdash \mathbf{0}
                                                                     \frac{1}{!(a) \oplus !(!(a) \multimap !(\mathbf{0})) : \ \vdash !(!(!(!(a) \multimap a)) \multimap !(\mathbf{0})) \multimap \mathbf{0}}
                                                         \frac{\frac{!(a) \oplus !(!(a) \ominus !(0)) : \cdot \vdash !(!(!(!(a) \ominus a)) \ominus !(0)) \ominus 0}{!(a) \oplus !(!(a) \ominus !(0)) : \cdot \vdash !(!(!(!(!(a) \ominus a)) \ominus !(0)) \ominus 0)} !}{\cdot : \cdot \vdash !(!(!(a) \oplus !(!(a) \ominus !(0))) \ominus !(!(!(!(!(a) \ominus a)) \ominus !(0)) \ominus 0))} *
  file: KLE/KLE060+1.p (472 ms)
  file: KLE/KLE061+1.p (81 ms)

\frac{\overline{a,!(a)} \multimap !(\mathbf{0}) : \cdot \vdash a}{\underline{a,!(a)} \multimap !(\mathbf{0}) : \cdot \vdash !(a)} ! \frac{\overline{a,!(a)} \multimap !(\mathbf{0}) : !(\mathbf{0}) \vdash \mathbf{0}}{\underline{a,!(a)} \multimap !(\mathbf{0}) : !(a) \multimap !(\mathbf{0}) \vdash \mathbf{0}} \xrightarrow{\underline{a,!(a)} \multimap !(\mathbf{0}) : !(a) \multimap !(\mathbf{0}) \vdash \mathbf{0}} D_{C}

                                                                         a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash \mathbf{0}
                                         \overline{\cdot : \cdot \vdash !(!(!(a) \& !(!(a) \multimap !(\mathbf{0}))) \multimap \mathbf{0})}
   file: KLE/KLE062+1.p (1351 ms)
   file: KLE/KLE063+1.p (328 ms)
  file: KLE/KLE064+1.p (328 ms)
```

```
file: KLE/KLE065+1.p (31 ms)
                                                                                   a,!(b) \oplus !(!(b) \multimap !(\mathbf{0})) : \cdot \vdash a
              \cdot : \cdot \vdash !(!(a) \& !(!(b) \oplus !(!(b) \multimap !(\mathbf{0})))) \multimap a
         : \cdot \vdash !(!(!(a) \& !(!(b) \oplus !(!(b) \multimap !(\mathbf{0})))) \multimap a)
   file: KLE/KLE066+1.p (149 ms)
                                                                                                     b,!(a) \oplus !(!(b) \& !(!(b) \multimap !(\mathbf{0}))),!(b) \multimap !(\mathbf{0}) : \cdot \vdash a
                                                                                                                           \neg \circ !(\mathbf{0}))) : !(\underline{a}) \oplus !(!(\underline{b}) \& !(!(\underline{b}) \multimap !(\mathbf{0}))) \vdash \underline{a} D_C
                                                                                                                                                                                                                                                                                                                                                                                                                             \vdash !(a) \oplus !(!(b \& !(!(b) \multimap \mathbf{0}))) 
\oplus_1
                                                                                                         !(a) \oplus !(!(b) \& !(!(b) \multimap !(\mathbf{0}))) : \cdot \vdash a
                                                                                                    : \overline{ \cdot \vdash !(!(a) \oplus !(!(b) \& !(!(b) \multimap !(\mathbf{0})))) \multimap a} \ ^{\star} 
                                                                                                                                                                                                  : \; \cdot \vdash !(!(!(a) \oplus !(!(b) \& !(!(b) \multimap !(\mathbf{0})))) \multimap a) \& !(!(a) \multimap !(a) \oplus !(!(b \& !(!(b) \multimap \mathbf{0})))) \\
                                                                                                                                                                                              : \cdot \vdash !(!(!(!(a) \oplus !(!(b) \& !(!(b) \multimap !(\mathbf{0})))) \multimap a) \& !(!(a) \multimap !(a) \oplus !(!(b \& !(!(b) \multimap \mathbf{0}))))) 
  file: KLE/KLE067+1.p (147 ms)
    \overline{a, b, !(b) \multimap !(\mathbf{0}) : \cdot \vdash b}
\underbrace{a, b, !(b) \multimap !(0) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{a, b, !(b) \multimap !(0) : \, !(0) \vdash !(b \& !(!(b) \multimap \mathbf{0}))}_{} \, * \, \underbrace{b, !(b) \multimap !(0) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{b, !(b) \multimap !(0) : \, !(0) \vdash !(a \& !(b \& !(!(b) \multimap \mathbf{0})))}_{} \, \underbrace{b, !(b) \multimap !(0) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{b, !(b) \multimap !(0) : \, !(b) \vdash !(a \& !(b \& !(!(b) \multimap \mathbf{0})))}_{} \, \underbrace{b, !(b) \multimap !(0) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{b, !(b) \multimap !(0) : \, !(b) \vdash !(a \& !(b \& !(!(b) \multimap \mathbf{0})))}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, ! \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \cdot \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b) : \, \vdash !(b)}_{} \, \underbrace{b, !(b) \multimap !(b) : \, \vdash !(b)}_{} 
                                    \frac{b,!(b) \multimap !(\mathbf{0}) : \ !(b) \multimap !(\mathbf{0}) \vdash !(a \& !(b \& !(!(b) \multimap \mathbf{0})))}{b,!(b) \multimap !(\mathbf{0}) : \ \vdash !(a \& !(b \& !(!(b) \multimap \mathbf{0})))} \ D_C 
                                                   a, b, !(b) \multimap !(\mathbf{0}) : \cdot \vdash !(b \& !(!(b) \multimap \mathbf{0}))
                 \frac{}{\cdot : \cdot \vdash !(!(!(b) \& !(!(b) \multimap !(\mathbf{0}))) \multimap !(a \& !(b \& !(!(b) \multimap \mathbf{0}))))} \stackrel{!}{} 
                                                    \cdot : \ \cdot \vdash !(!(!(a) \ \& \ !(!(b) \ \& \ !(!(b) - \circ \ !(\mathbf{0})))) \ - \cdot !(b \ \& \ !(!(b) - \circ \ 0))) \ \& \ !(!(!(b) \ \& \ !(!(b) - \circ \ !(\mathbf{0}))) \ - \cdot !(a \ \& \ !(b \ \& \ !(!(b) - \circ \ 0))))
                                                 \overline{\cdot : \cdot \vdash !(!(!(!(a) \& !(!(b) \& !(!(b) \multimap !(\mathbf{0})))) \multimap !(b \& !(!(b) \multimap \mathbf{0}))) \& !(!(!(b) \& !(!(b) \multimap !(\mathbf{0}))) \multimap !(a \& !(b \& !(!(b) \multimap \mathbf{0}))))}}
  file: KLE/KLE068+1.p (timeout!)
  file: KLE/KLE069+1.p (timeout!)
    file: KLE/KLE070+1.p (355 ms)
  file: KLE/KLE071+1.p (294 ms)
```



```
file: KLE/KLE078+1.p (timeout!)
 file: KLE/KLE079+1.p (431 ms)
 file: KLE/KLE080+1.p (124 ms)
                                                                                                            \overline{a,b,!(a)\multimap !(!(b)\multimap !(\mathbf{0})),!(b)\multimap !(\mathbf{0}): \cdot \vdash b}
                                                                                                        \frac{a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) : \cdot \vdash b}{a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) : \cdot \vdash !(b)} ! \xrightarrow[a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) : !(b) \multimap !(0) : !(b) \multimap !(b) \multimap !(b) \\ \xrightarrow[a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) : !(b) \multimap !(0) \vdash b} D_{C}
                                                                                                                                                                                \frac{a, b, !(a) \multimap !(!(b) \multimap !(0)), !(b) \multimap !(0) : \vdash \mathbf{0}}{a, b, !(a) \multimap !(!(b) \multimap !(0)) : !(!(b) \multimap !(0)) \vdash \mathbf{0}}
 \overline{a,b,!(a)\multimap !(!(b)\multimap !(\mathbf{0})): \cdot \vdash a}
\overline{a,b,!(a)\multimap !(!(b)\multimap !(\mathbf{0})):\ \cdot \vdash !(a)}
                                                                             \begin{array}{c} a, b, !(a) & \circ !(!(b) - \circ !(0)) : \ !(a) - \circ !(!(b) - \circ !(0)) \vdash \mathbf{0} \\ \end{array}
                                                                                                        a, b, !(a) \multimap !(!(b) \multimap !(\mathbf{0})) : \cdot \vdash \mathbf{0}
                                                                                                  a, b: \cdot \vdash !(!(a) \multimap !(!(b) \multimap !(\mathbf{0}))) \multimap \mathbf{0}
                                                                         \frac{\frac{a,b: \cdot \vdash !(!(!(a) \circ !(!(b) \circ !(0))) \circ o)}{a,b: \cdot \vdash !(!(!(a) \circ !(!(b) \circ !(0))) \circ o)} !}{\cdot : \cdot \vdash !(!(a) \& !(b)) \circ !(!(!(a) \circ !(!(b) \circ !(0))) \circ o)} *}{\cdot : \cdot \vdash !(!(!(a) \& !(b)) \circ !(!(!(a) \circ !(!(b) \circ !(0))) \circ o))} !
 file: KLE/KLE081+1.p (290 ms)
```

file: KLE/KLE082+1.p (374 ms)



file: KLE/KLE088+1.p (timeout!)

3.2 LCL Problems

file: LCL/LCL181+1.p (timeout!)

file: LCL/LCL230+1.p (timeout!)

3.3 SYJ Problems

file: SYJ/SYJ101+1.p (26 ms)

 $\frac{\overline{a:\cdot\vdash a}}{\cdot:\ !(a)\vdash a}\ \star$

file: SYJ/SYJ102+1.p (86 ms)

$$\frac{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash a}{\underbrace{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash !(a)} ! \underbrace{a,!(a) \multimap !(\mathbf{0}) : \cdot !(\mathbf{0}) \vdash \mathbf{0}}_{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash \mathbf{0}} \star \underbrace{\frac{a,!(a) \multimap !(\mathbf{0}) : \cdot \vdash \mathbf{0}}_{a:\cdot \vdash !(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0}}_{\star} + \underbrace{\frac{a,!(a) \multimap !(!(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0}}_{\star} : \cdot \vdash !(!(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0})}_{\cdot : \cdot !(a) \vdash !(!(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0})} *}_{\cdot : \cdot !(a) \vdash !(!(!(a) \multimap !(\mathbf{0})) \multimap \mathbf{0})} \star$$

file: SYJ/SYJ103+1.p (timeout!)

file: SYJ/SYJ104+1.p (226 ms)

file: SYJ/SYJ105+1.002.p (349 ms)



file: SYJ/SYJ105+1.003.p (timeout!)

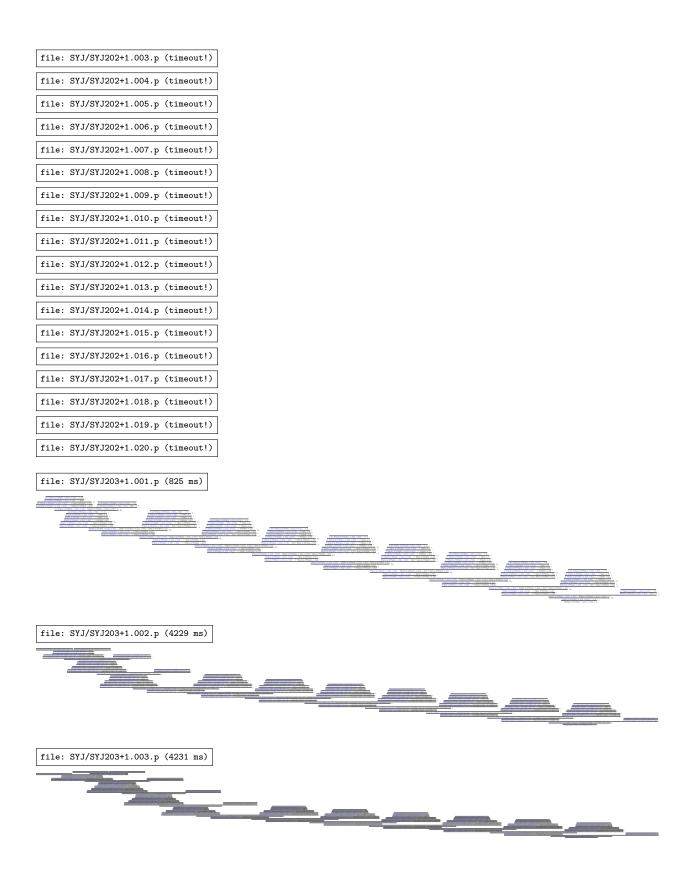
file: SYJ/SYJ105+1.004.p (timeout!)

file: SYJ/SYJ106+1.p (1814 ms)

```
file: SYJ/SYJ107+1.001.p (841 ms)
file: SYJ/SYJ107+1.002.p (117105 ms)
file: SYJ/SYJ107+1.003.p (timeout!)
file: SYJ/SYJ107+1.004.p (timeout!)
file: SYJ/SYJ201+1.002.p (timeout!)
file: SYJ/SYJ201+1.003.p (timeout!)
file: SYJ/SYJ201+1.004.p (timeout!)
file: SYJ/SYJ201+1.005.p (timeout!)
file: SYJ/SYJ201+1.006.p (timeout!)
file: SYJ/SYJ201+1.007.p (timeout!)
file: SYJ/SYJ201+1.008.p (timeout!)
file: SYJ/SYJ201+1.009.p (timeout!)
file: SYJ/SYJ201+1.010.p (timeout!)
file: SYJ/SYJ201+1.011.p (timeout!)
file: SYJ/SYJ201+1.012.p (timeout!)
 file: SYJ/SYJ201+1.013.p (timeout!)
file: SYJ/SYJ201+1.014.p (timeout!)
file: SYJ/SYJ201+1.015.p (timeout!)
file: SYJ/SYJ201+1.016.p (timeout!)
file: SYJ/SYJ201+1.017.p (timeout!)
file: SYJ/SYJ201+1.018.p (timeout!)
file: SYJ/SYJ201+1.019.p (timeout!)
file: SYJ/SYJ201+1.020.p (timeout!)
file: SYJ/SYJ202+1.001.p (39 ms)
        \textcolor{red}{o11},\textcolor{red}{o21}: \hspace{0.1cm} \cdot \vdash o11
       \overline{o11}, \overline{o21}: \cdot \vdash !(o11)

\overbrace{o11, o21: \cdot \vdash !(o11) \oplus !(o21)}^{\prime} \oplus_{1}

\cdot : !(o11), !(o21) \vdash !(o11) \oplus !(o21)
file: SYJ/SYJ202+1.002.p (timeout!)
```



```
file: SYJ/SYJ203+1.004.p (5212 ms)
  file: SYJ/SYJ203+1.005.p (7042 ms)
  file: SYJ/SYJ203+1.010.p (timeout!)
  file: SYJ/SYJ203+1.011.p (timeout!)
  file: SYJ/SYJ203+1.012.p (timeout!)
  file: SYJ/SYJ203+1.013.p (timeout!)
  file: SYJ/SYJ203+1.014.p (timeout!)
  file: SYJ/SYJ203+1.015.p (timeout!)
  file: SYJ/SYJ203+1.016.p (timeout!)
  file: SYJ/SYJ203+1.017.p (timeout!)
  file: SYJ/SYJ203+1.018.p (timeout!)
  file: SYJ/SYJ203+1.019.p (timeout!)
   file: SYJ/SYJ203+1.020.p (timeout!)
  file: SYJ/SYJ204+1.001.p (123 ms)
                                                                                                                                                                                                                                                                           \overline{p0, p1, !(p1) \multimap !(p0), !(p1) \multimap !(!(p1) \multimap !(p0)) : \ \cdot \vdash p0}
                                                                                                                    \overline{p1,!(p1) \multimap !(p0),!(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash p1}
                                                                                                                  \frac{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_1) - 0, (p_0)) + p_1}{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_1) - 0, (p_0)) + p_1} + \frac{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_1) - 0, (p_0)) + p_1}{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_1) - 0, (p_0)) + p_2} + \frac{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_1) - 0, (p_0)) + p_2}{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_0) - 0, (p_0)) + p_2} + \frac{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_0) - 0, (p_0)) + p_2}{p_1, (p_1) - 0, (p_0), (p_1) - 0, ((p_0) - 0, (p_0)) + p_2} + \frac{p_1, (p_1) - 0, (p_0), (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, (p_1) - 0, (p_0)} + \frac{p_1, (p_1) - 0, (p_0)}{p_1, 
                                                                                                                                                                                   \frac{p1,!(p1) \multimap !(p0),!(p1) \multimap !(!(p1) \multimap !(p0)) : \ !(p1) \multimap !(p0) \vdash p0}{D_C} D_C
  \overline{p1,!(p1) \multimap !(!(p1) \multimap !(p0)) : \ \cdot \vdash p1}
                                                                                                                                                                                                    p1,!(p1) \multimap !(p0),!(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash p0
                                                                                                                                                                                                   \frac{1}{p_1,!(p_1) \multimap !(!(p_1) \multimap !(p_0)) : !(!(p_1) \multimap !(p_0)) \vdash p_0} \times \frac{1}{p_1,!(p_1) \multimap !(p_0)}
p1,!(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash !(p1)
                                                                                      p1, !(p1) \multimap !(!(p1) \multimap !(p0)) : !(p1) \multimap !(!(p1) \multimap !(p0)) \vdash p0
D_C
                                                                                                                    p1,!(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash p0
                                                                                                               \frac{1}{\cdot : \cdot !(p1), !(!(p1) \multimap !(!(p1) \multimap !(p0))) \vdash p0} 
  file: SYJ/SYJ204+1.002.p (607 ms)
  file: SYJ/SYJ204+1.003.p (2025 ms)
  file: SYJ/SYJ204+1.004.p (9486 ms)
```

file: SYJ/SYJ204+1.006.p (timeout!) file: SYJ/SYJ204+1.007.p (timeout!) file: SYJ/SYJ204+1.008.p (timeout!) file: SYJ/SYJ204+1.009.p (timeout!) file: SYJ/SYJ204+1.010.p (timeout!) file: SYJ/SYJ204+1.011.p (timeout!) file: SYJ/SYJ204+1.012.p (timeout!) file: SYJ/SYJ204+1.013.p (timeout!) file: SYJ/SYJ204+1.014.p (timeout!) file: SYJ/SYJ204+1.015.p (timeout!) file: SYJ/SYJ204+1.016.p (timeout!) file: SYJ/SYJ204+1.017.p (timeout!) file: SYJ/SYJ204+1.018.p (timeout!) file: SYJ/SYJ204+1.019.p (timeout!) file: SYJ/SYJ204+1.020.p (timeout!) file: SYJ/SYJ205+1.001.p (31889 ms) file: SYJ/SYJ205+1.002.p (93986 ms) file: SYJ/SYJ205+1.003.p (timeout!) file: SYJ/SYJ205+1.004.p (timeout!) file: SYJ/SYJ205+1.005.p (timeout!) file: SYJ/SYJ205+1.006.p (timeout!) file: SYJ/SYJ205+1.007.p (timeout!) file: SYJ/SYJ205+1.008.p (timeout!) file: SYJ/SYJ205+1.009.p (timeout!) file: SYJ/SYJ205+1.010.p (timeout!) file: SYJ/SYJ205+1.011.p (timeout!) file: SYJ/SYJ205+1.012.p (timeout!) file: SYJ/SYJ205+1.013.p (timeout!) file: SYJ/SYJ205+1.014.p (timeout!)

```
file: SYJ/SYJ205+1.015.p (timeout!)
file: SYJ/SYJ205+1.016.p (timeout!)
file: SYJ/SYJ205+1.017.p (timeout!)
 file: SYJ/SYJ205+1.018.p (timeout!)
 file: SYJ/SYJ205+1.019.p (timeout!)
 file: SYJ/SYJ205+1.020.p (timeout!)
 file: SYJ/SYJ206+1.001.p (49 ms)
\frac{a1: \cdot \vdash a1}{\cdot : \cdot \vdash !(a1) \multimap a1} \star \frac{\overline{a1: \cdot \vdash a1}}{\cdot : \cdot \vdash !(a1) \multimap a1} \cdot \frac{}{\cdot : \cdot \vdash !(a1) \multimap a1}
           \cdot : \cdot \vdash !(!(a1) \multimap a1) \& !(!(a1) \multimap a1)
        \cdot : \cdot \vdash !(!(!(a1) \multimap a1) \& !(!(a1) \multimap a1))
file: SYJ/SYJ206+1.002.p (528 ms)
 file: SYJ/SYJ206+1.003.p (60604 ms)
 file: SYJ/SYJ206+1.004.p (timeout!)
 file: SYJ/SYJ206+1.005.p (timeout!)
 file: SYJ/SYJ206+1.006.p (timeout!)
 file: SYJ/SYJ206+1.007.p (timeout!)
 file: SYJ/SYJ206+1.008.p (timeout!)
 file: SYJ/SYJ206+1.009.p (timeout!)
 file: SYJ/SYJ206+1.010.p (timeout!)
 file: SYJ/SYJ206+1.011.p (timeout!)
 file: SYJ/SYJ206+1.012.p (timeout!)
 file: SYJ/SYJ206+1.013.p (timeout!)
 file: SYJ/SYJ206+1.014.p (timeout!)
 file: SYJ/SYJ206+1.015.p (timeout!)
 file: SYJ/SYJ206+1.016.p (timeout!)
```

- file: SYJ/SYJ206+1.017.p (timeout!)
- file: SYJ/SYJ206+1.018.p (timeout!)
- file: SYJ/SYJ207+1.001.p (timeout!)
- file: SYJ/SYJ207+1.002.p (timeout!)
- file: SYJ/SYJ207+1.003.p (timeout!)
- file: SYJ/SYJ207+1.004.p (timeout!)
- file: SYJ/SYJ207+1.005.p (timeout!)
- file: SYJ/SYJ207+1.006.p (timeout!)
- file: SYJ/SYJ207+1.007.p (timeout!)
- file: SYJ/SYJ207+1.008.p (timeout!)
- file: SYJ/SYJ207+1.009.p (timeout!)
- file: SYJ/SYJ207+1.010.p (timeout!)
- file: SYJ/SYJ207+1.011.p (timeout!)
- file: SYJ/SYJ207+1.012.p (timeout!)
- file: SYJ/SYJ207+1.013.p (timeout!)
- file: SYJ/SYJ207+1.014.p (timeout!)
- file: SYJ/SYJ207+1.015.p (timeout!)
- file: SYJ/SYJ207+1.016.p (timeout!)
- file: SYJ/SYJ207+1.017.p (timeout!)
- ille. 515/515207/1.017.p (timeout:)
- file: SYJ/SYJ207+1.018.p (timeout!)
- file: SYJ/SYJ207+1.019.p (timeout!)
- file: SYJ/SYJ207+1.020.p (timeout!)
- file: SYJ/SYJ208+1.001.p (timeout!)
- file: SYJ/SYJ208+1.002.p (timeout!)
- file: SYJ/SYJ208+1.003.p (timeout!)
- file: SYJ/SYJ208+1.004.p (timeout!)
- file: SYJ/SYJ208+1.005.p (timeout!)
- file: SYJ/SYJ208+1.006.p (timeout!)
- file: SYJ/SYJ208+1.007.p (timeout!)
- file: SYJ/SYJ208+1.008.p (timeout!)
- file: SYJ/SYJ208+1.009.p (timeout!)
- file: SYJ/SYJ208+1.010.p (timeout!)
- file: SYJ/SYJ208+1.011.p (timeout!)
- file: SYJ/SYJ208+1.012.p (timeout!)
- file: SYJ/SYJ208+1.013.p (timeout!)

- file: SYJ/SYJ208+1.014.p (timeout!)
- file: SYJ/SYJ208+1.015.p (timeout!)
- file: SYJ/SYJ208+1.016.p (timeout!)
- file: SYJ/SYJ208+1.017.p (timeout!)
- file: SYJ/SYJ208+1.018.p (timeout!)
- file: SYJ/SYJ209+1.001.p (timeout!)
- file: SYJ/SYJ209+1.002.p (timeout!)
- file: SYJ/SYJ209+1.003.p (timeout!)
- file: SYJ/SYJ209+1.004.p (timeout!)
- file: SYJ/SYJ209+1.005.p (timeout!)
- file: SYJ/SYJ209+1.006.p (timeout!)
- file: SYJ/SYJ209+1.007.p (timeout!)
- file: SYJ/SYJ209+1.008.p (timeout!)
- file: SYJ/SYJ209+1.009.p (timeout!)
- file: SYJ/SYJ209+1.010.p (timeout!)
- file: SYJ/SYJ209+1.011.p (timeout!)
- file: SYJ/SYJ209+1.012.p (timeout!)
- file: SYJ/SYJ209+1.013.p (timeout!)
- file: SYJ/SYJ209+1.014.p (timeout!)
- file: SYJ/SYJ209+1.015.p (timeout!)
- file: SYJ/SYJ209+1.016.p (timeout!)
- file: SYJ/SYJ209+1.017.p (timeout!)
- file: SYJ/SYJ209+1.018.p (timeout!)
- file: SYJ/SYJ209+1.019.p (timeout!)
- file: SYJ/SYJ209+1.020.p (timeout!)
- file: SYJ/SYJ210+1.001.p (timeout!)
- file: SYJ/SYJ210+1.002.p (timeout!)
- file: SYJ/SYJ210+1.003.p (timeout!)
- file: SYJ/SYJ210+1.004.p (timeout!)
- file: SYJ/SYJ210+1.005.p (timeout!)
- file: SYJ/SYJ210+1.006.p (timeout!)
- file: SYJ/SYJ210+1.007.p (timeout!)
- file: SYJ/SYJ210+1.008.p (timeout!)
- file: SYJ/SYJ210+1.009.p (timeout!)
- file: SYJ/SYJ210+1.010.p (timeout!)

file: SYJ/SYJ210+1.011.p (timeout!) file: SYJ/SYJ210+1.012.p (timeout!) file: SYJ/SYJ210+1.013.p (timeout!) file: SYJ/SYJ210+1.014.p (timeout!) file: SYJ/SYJ210+1.015.p (timeout!) file: SYJ/SYJ210+1.016.p (timeout!) file: SYJ/SYJ210+1.017.p (timeout!) file: SYJ/SYJ210+1.018.p (timeout!) file: SYJ/SYJ210+1.019.p (timeout!) file: SYJ/SYJ210+1.020.p (timeout!) file: SYJ/SYJ211+1.001.p (timeout!) file: SYJ/SYJ211+1.002.p (timeout!) file: SYJ/SYJ211+1.003.p (timeout!) file: SYJ/SYJ211+1.004.p (timeout!) file: SYJ/SYJ211+1.005.p (timeout!) file: SYJ/SYJ211+1.006.p (timeout!) file: SYJ/SYJ211+1.007.p (timeout!) file: SYJ/SYJ211+1.008.p (timeout!) file: SYJ/SYJ211+1.009.p (timeout!) file: SYJ/SYJ211+1.010.p (timeout!) file: SYJ/SYJ211+1.011.p (timeout!) file: SYJ/SYJ211+1.012.p (timeout!) file: SYJ/SYJ211+1.013.p (timeout!) file: SYJ/SYJ211+1.014.p (timeout!) file: SYJ/SYJ211+1.015.p (timeout!) file: SYJ/SYJ211+1.016.p (timeout!) file: SYJ/SYJ211+1.017.p (timeout!) file: SYJ/SYJ211+1.018.p (timeout!) file: SYJ/SYJ211+1.019.p (timeout!) file: SYJ/SYJ211+1.020.p (timeout!) file: SYJ/SYJ212+1.001.p (1267 ms) **--**-file: SYJ/SYJ212+1.002.p (timeout!)

file: SYJ/SYJ212+1.003.p (timeout!)

```
file: SYJ/SYJ212+1.004.p (timeout!)

file: SYJ/SYJ212+1.005.p (timeout!)

file: SYJ/SYJ212+1.006.p (timeout!)

file: SYJ/SYJ212+1.007.p (timeout!)

file: SYJ/SYJ212+1.008.p (timeout!)

file: SYJ/SYJ212+1.009.p (timeout!)
```

```
3.4 SYN Problems
file: SYN/SYN001+1.p (301 ms)
                                file: SYN/SYN040+1.p (timeout!)
file: SYN/SYN041+1.p (timeout!)
file: SYN/SYN044+1.p (622 ms)
file: SYN/SYN045+1.p (795 ms)
file: SYN/SYN046+1.p (timeout!)
file: SYN/SYN047+1.p (timeout!)
file: SYN/SYN387+1.p (timeout!)
file: SYN/SYN388+1.p (timeout!)
file: SYN/SYN389+1.p (timeout!)
file: SYN/SYN390+1.p (44 ms)
```

```
\frac{p: \cdot \vdash p}{\cdot : \cdot \vdash !(p) \multimap p} \star \frac{p: \cdot \vdash p}{\cdot : \cdot \vdash !(p) \multimap p} \cdot \frac{p: \cdot \vdash p}{\cdot : \cdot \vdash !(p) \multimap p}
             \cdot: \cdot \vdash !(!(p) \multimap p) \& !(!(p) \multimap p)
         \cdot: \cdot \vdash !(!(!(p) \multimap p) \& !(!(p) \multimap p))
file: SYN/SYN391+1.p (382 ms)
 file: SYN/SYN392+1.p (timeout!)
 file: SYN/SYN393+1.p (timeout!)
 file: SYN/SYN416+1.p (timeout!)
file: SYN/SYN915+1.p (17 ms)
\overline{\cdot : \cdot \vdash 1}
 file: SYN/SYN916+1.p (timeout!)
 file: SYN/SYN977+1.p (timeout!)
 file: SYN/SYN978+1.p (84 ms)
        \frac{\overline{a,b:\cdot\vdash b}}{a,b:\cdot\vdash!(a)\multimap b}\star \frac{\overline{a,b:\cdot\vdash a}}{a,b:\cdot\vdash!(b)\multimap a}\star \frac{\overline{a,b:\cdot\vdash a}}{a,b:\cdot\vdash!(b)\multimap a}
                      a, b: \cdot \vdash !(!(a) \multimap b) \& !(!(b) \multimap a)
                  \overline{a,b: \cdot \vdash !(!(!(a) \multimap b) \& !(!(b) \multimap a))}
  \cdot : \cdot \vdash !(!(a) \& !(b)) \multimap !(!(!(a) \multimap b) \& !(!(b) \multimap a)) 
\cdot : \cdot \vdash !(!(!(a) \& !(b)) \multimap !(!(!(a) \multimap b) \& !(!(b) \multimap a)))
```

4 Call-by-Name

4.1 KLE Problems

```
file: KLE/KLE001+1.p (26 ms)
       a: \overline{\cdot \vdash a}
 \overline{\cdot : \cdot \vdash !(a) \multimap a}
 file: KLE/KLE002+1.p (227 ms)
    a,!(a)\multimap b,!(b)\multimap c:\ \cdot \vdash a
 \frac{a,!(a)\multimap b,!(b)\multimap c: \ \cdot \vdash a}{a,!(a)\multimap b,!(b)\multimap c: \ \underline{\cdot \vdash !(a)}} \ ! \ \frac{a,!(a)\multimap b,!(b)\multimap c: \ b\vdash b}{a,!(a)\multimap b,!(b)\multimap c: \ b\vdash b} \multimap
                                        \frac{a,!(a) \multimap b,!(b) \multimap c : !(a) \multimap b \vdash b}{a,!(a) \multimap b,!(b) \multimap c : \cdot \vdash b} D_C
\frac{a,!(a) \multimap b,!(b) \multimap c : \cdot \vdash !(b)}{a,!(a) \multimap b,!(b) \multimap c : \cdot \vdash !(b)} !
                                                                                                            \frac{a,!(a)\multimap b,!(b)\multimap c: !(b)\multimap c\vdash c}{a,!(a)\multimap b,!(b)\multimap c: \cdot \vdash c} D_C
                                                                                                                 file: KLE/KLE003+1.p (75 ms)
\frac{\overline{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash b}}{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash !(b)} ! \frac{\overline{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash b}}{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash !(b)} ! \frac{\overline{a,b,!(a) \multimap !(b) \multimap c : c \vdash c}}{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash !(b)} \multimap \frac{\overline{a,b,!(a) \multimap !(b) \multimap c \vdash c}}{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash c} \multimap \frac{\overline{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash c}}{a,b,!(a) \multimap !(b) \multimap c : \cdot \vdash c} \circlearrowleft D_C
   file: KLE/KLE004+1.p (77 ms)
\frac{\overline{a,b,!(a)\multimap!(b)\multimap c: \cdot \vdash b}}{a,b,!(a)\multimap!(b)\multimap c: \cdot \vdash !(a)} : \frac{\overline{a,b,!(a)\multimap!(b)\multimap c: \cdot \vdash b}}{a,b,!(a)\multimap!(b)\multimap c: \cdot \vdash !(b)} : \overline{a,b,!(a)\multimap!(b)\multimap c: c\vdash c}
a,b,!(a)\multimap!(b)\multimap c: !(b)\multimap c: \cdot \vdash !(b)
                                                             \frac{a, b, !(a) \multimap !(b) \multimap c : !(a) \multimap !(b) \multimap c \vdash c}{a, b, !(a) \multimap !(b) \multimap c : \cdot \vdash c} D_C
                                                                     \frac{a, b, :(a) \multimap .(c)}{\cdot : \ !(!(a) \multimap !(b) \multimap c) \vdash !(a \& b) \multimap c}
 file: KLE/KLE005+1.p (78 ms)
 \overline{a,b,!(a \& b) \multimap c : \cdot \vdash a} \quad \overline{a,b,!(a \& b) \multimap c : \cdot \vdash b} \quad \star
                                    \frac{a, b, !(a \& b) \multimap c : \cdot \vdash a \& b}{a, b, !(a \& b) \multimap c : \cdot \vdash !(a \& b)} !
                                                                                                                                                                                                   \overline{a,b,!(a \& b) \multimap c : c \vdash c} \quad \multimap
                                                                                                \frac{a, b, !(a \& b) \multimap c : !(a \& b) \multimap c \vdash c}{a, b, !(a \& b) \multimap c : \cdot \vdash c} D_C
                                                                                                 \overline{ \cdot : \ !(!(a \& b) \multimap c) \vdash !(a) \multimap !(b) \multimap c} 
  file: KLE/KLE006+1.p (229 ms)
```

::ie: KEL/KEL000:::p (223 m3)

$$\frac{a,!(a) - b,!(b) - c c : \cdot \vdash a}{a,!(a) - b,!(b) - c c : \cdot \vdash (a)} ! \frac{a,!(a) - b,!(b) - c c : b \vdash b}{a,!(a) - c,!(b) - c c : \cdot \vdash (a)} - c \frac{a,!(a) - c,!(b) - c c : b \vdash b}{a,!(a) - c,!(b) - c c : \cdot \vdash b} D_C \frac{a,!(a) - c,!(b) - c c : \cdot \vdash b}{a,!(a) - c,!(b) - c c : \cdot \vdash b} D_C \frac{a,!(a) - c,!(b) - c c : \cdot \vdash c}{a,!(a) - c,!(b) - c c : \cdot \vdash c} D_C \frac{a,!(a) - c,!(b) - c c : \cdot \vdash c}{a,!(a) - c,!(b) - c c : \cdot \vdash c} D_C \frac{a,!(a) - c,!(b) - c c : \cdot \vdash c}{c,!(a) - c,!(b) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(b) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(b) - c c : \cdot \vdash c}{c,!(a) - c,!(a) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{c,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{a,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{a,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{a,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(c) - c c : \cdot \vdash c}{a,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(a) - c \cdot \vdash c}{a,!(a) - c,!(c) - c c : \cdot \vdash c} \frac{a,!(a) - c,!(a) - c \cdot \vdash c}{a,!(a) - c,!(a) - c : \cdot \vdash c} \frac{a,!(a) - c,!(a) - c \cdot \vdash c}{a,!(a) - c,!(a) - c : \cdot \vdash c} \frac{a,!(a) - c,!(a) - c \cdot \vdash c}{a,!(a) - c,!(a) - c : \cdot \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c : \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c : \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c : \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c : \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c : \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c : \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c : \vdash c} \frac{a,!(a) - c,!(a) - c : \vdash c}{a,!(a) - c,!(a) - c$$

```
| Total | Tota
  file: KLE/KLE011+1.p (388 ms)
                                                                                                                                                                                                           \frac{\overline{a,!(c) \oplus !(a),!(a) \multimap b : \cdot \vdash a}}{\underbrace{a,!(c) \oplus !(a),!(a) \multimap b : \cdot \vdash !(a)}_{a,!(c) \oplus !(a),!(a) \multimap b : b \vdash b} | D_C 
 \frac{\underbrace{a,!(c) \oplus !(a),!(a) \multimap b : !(a) \multimap b \vdash b}_{a,!(c) \oplus !(a),!(a) \multimap b : \cdot \vdash b} | D_C 
 \frac{\underbrace{a,!(c) \oplus !(a),!(a) \multimap b : \cdot \vdash b}_{a,!(c) \oplus !(a),!(a) \multimap b : \cdot \vdash !(b)} !}_{a,!(c) \oplus !(a),!(a) \multimap b : \cdot \vdash !(c) \oplus !(b)} \oplus_{\star} 
\frac{\overline{c,!(c)\oplus !(a),!(a)\multimap b: \cdot \vdash c}}{\overline{c,!(c)\oplus !(a),!(a)\multimap b: \cdot \vdash !(c)}} \stackrel{!}{\underbrace{c,!(c)\oplus !(a),!(a)\multimap b: \cdot \vdash !(c)\oplus !(b)}} \oplus_{1}
                                                                                                                    \frac{!(c) \oplus !(a), !(a) \multimap b : \ \cdot \vdash !(c) \oplus !(b)}{\cdot : \ !(!(a) \multimap b) \vdash !(!(c) \oplus !(a)) \multimap !(c) \oplus !(b)} \star
 file: KLE/KLE012+1.p (68 ms)
             a,!(a) \multimap \mathbf{0} : \cdot \vdash a
\frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)}{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)} ! \frac{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash b}{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash b}
                                                                                             a, !(a) \multimap \mathbf{0} : !(a) \multimap \mathbf{0} \vdash b
                                                                                                                                           a,!(a) \multimap \mathbf{0} : \cdot \vdash b
                                                                                                    \overline{ \cdot : \quad !(!(a) \multimap \mathbf{0}) \vdash !(a) \multimap b} 
   file: KLE/KLE013+1.p (timeout!)
   file: KLE/KLE014+1.p (27 ms)
\frac{\overline{a,b: \cdot \vdash b}}{\cdot : \ !(b) \vdash !(a) \multimap b} \ \star
  file: KLE/KLE015+1.p (timeout!)
 file: KLE/KLE016+1.p (89 ms)
\frac{\overline{a,b,!(a)\multimap!(b)\multimap\mathbf{0}:\,\cdot\vdash b}}{a,b,!(a)\multimap!(b)\multimap\mathbf{0}:\,\cdot\vdash!(a)}\;!\;\;\frac{\overline{a,b,!(a)\multimap!(b)\multimap\mathbf{0}:\,\cdot\vdash b}}{a,b,!(a)\multimap!(b)\multimap\mathbf{0}:\,\cdot\vdash!(b)}\;!\;\;\overline{a,b,!(a)\multimap!(b)\multimap\mathbf{0}:\,\mathbf{0}:\,\mathbf{0}\vdash\mathbf{0}}\;\;\overset{\star}{\circ}
                                                                                                        \frac{a, b, !(a) \multimap !(b) \multimap \mathbf{0} : \ !(a) \multimap !(b) \multimap \mathbf{0} \vdash \mathbf{0}}{a, b, !(a) \multimap !(b) \multimap \mathbf{0} : \ \vdash \mathbf{0}} D_C
\frac{a, b, !(a) \multimap !(b) \multimap \mathbf{0} : \ \vdash \mathbf{0}}{\cdot : \ !(!(a) \multimap !(b) \multimap \mathbf{0}) \vdash !(b) \multimap !(a) \multimap \mathbf{0}} \star
```

```
file: KLE/KLE017+1.p (timeout!)
  file: KLE/KLE018+1.p (399 ms)
  file: KLE/KLE019+1.p (261 ms)
\frac{\overline{a,!(a)\multimap b,!(b)\multimap a: \cdot \vdash a}}{\underbrace{a,!(a)\multimap b,!(b)\multimap a: \cdot \vdash !(a)}} \overset{!}{\underbrace{a,!(a)\multimap b,!(b)\multimap a: b\vdash b}} D_C \\ \frac{\overline{a,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}}{\underbrace{a,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}} D_C
\frac{\overline{b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}}{\underbrace{b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}} D_C
\frac{\overline{b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}}{\underbrace{b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}} D_C
\frac{\overline{b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}}{\underbrace{b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b}} D_C
                                                                                    \cdot : !(!(a) \multimap b), !(!(b) \multimap a) \vdash !(a) \multimap b \& !(b) \multimap a
 file: KLE/KLE020+1.p (212 ms)
\frac{a,!(a)\multimap b,!(b)\multimap a:\ \cdot\vdash a}{a,!(a)\multimap b,!(b)\multimap a:\ \cdot\vdash !(a)} \ ! \ \frac{a,!(a)\multimap b,!(b)\multimap a:\ b\vdash b}{a,!(a)\multimap b,!(b)\multimap a:\ b\vdash b}
                                                   \frac{a,!(a) \multimap b,!(b) \multimap a : !(a) \multimap b \vdash b}{a,!(a) \multimap b,!(b) \multimap a : \cdot \vdash b} D_C
\vdots !(!(a) \multimap b \& !(b) \multimap a) \vdash !(a) \multimap b
 file: KLE/KLE021+1.p (228 ms)
     b,!(a) \multimap b,!(b) \multimap a : \cdot \vdash b
\frac{b,!(a)\multimap b,!(b)\multimap a: \cdots \smile b}{b,!(a)\multimap b,!(b)\multimap a: \cdots \smile b} \; ! \quad \frac{b,!(a)\multimap b,!(b)\multimap a: a\vdash a}{b,!(a)\multimap b,!(b)\multimap a: a\vdash a} \quad \multimap
                                                      b, !(a) \multimap b, !(b) \multimap a : !(b) \multimap a \vdash a
D_C
                                                                b,!(a) \multimap b,!(b) \multimap a : \cdot \vdash a
```

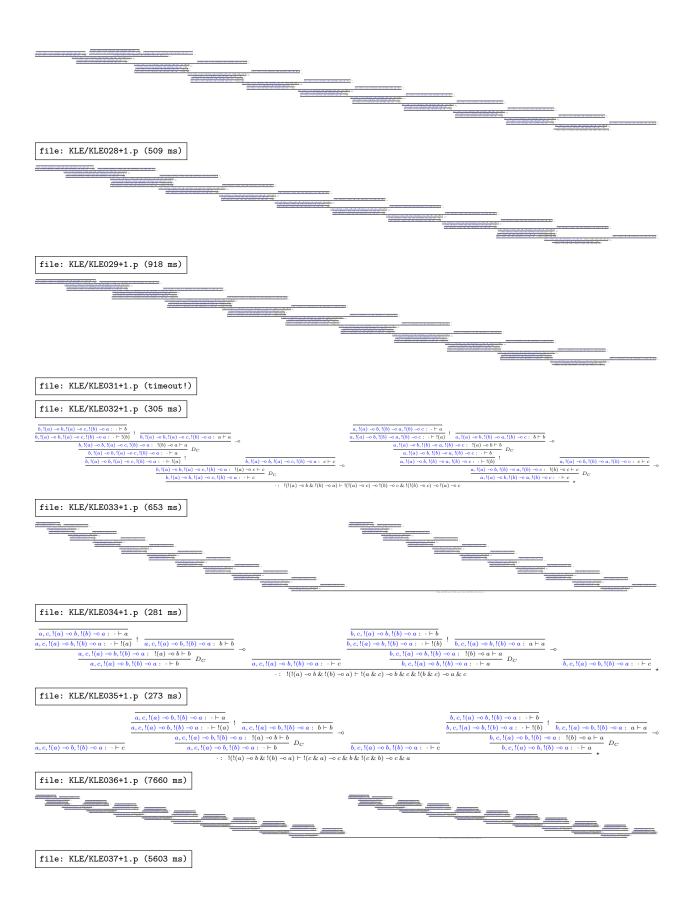
file: KLE/KLE022+1.p (198 ms)

 $\frac{}{\cdot : \ !(!(a) \multimap b \& !(b) \multimap a) \vdash !(b) \multimap a} \quad \star$

```
\overline{a,!(a)} \multimap b,!(b) \multimap a : \cdot \vdash a
\frac{a, !(a) \multimap b, !(b) \multimap a : \cdot \vdash a}{a, !(a) \multimap b, !(b) \multimap a : \cdot \vdash !(a)} ! \frac{a, !(a) \multimap b, !(b) \multimap a : b \vdash b}{a, !(a) \multimap b, !(b) \multimap a : b \vdash b}
                                        a, !(a) \multimap b, !(b) \multimap a : !(a) \multimap b \vdash b

\frac{a,!(a) \multimap b,!(b) \multimap a : \cdot \vdash b}{!(a),!(!(a) \multimap b \& !(b) \multimap a) \vdash b} *

 file: KLE/KLE023+1.p (206 ms)
   b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash b
\frac{b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash !(b)}{b,!(a)\multimap b,!(b)\multimap a: a\vdash a}
                                       b,!(a) \multimap b,!(b) \multimap a : !(b) \multimap a \vdash a
                                                   b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash a
                                         \vdots \quad \overline{!(b),!(!(a)\multimap b \& !(b)\multimap a)\vdash a} \quad \star
 file: KLE/KLE024+1.p (29 ms)
                                                                                     a: \cdot \vdash
                                                                                                                                                                                              m{\star}
                         \cdot \vdash !(a) \multimap a \& !(a) \multimap a
 file: KLE/KLE025+1.p (280 ms)
                                                                                                   \frac{\overline{a,!(a) \multimap b,!(b) \multimap a : \cdot \vdash a}}{\underbrace{a,!(a) \multimap b,!(b) \multimap a : \cdot \vdash !(a)}} \cdot \frac{a,!(a) \multimap b,!(b) \multimap a : b \vdash b}{\underbrace{a,!(a) \multimap b,!(b) \multimap a : !(a) \multimap b \vdash b}}_{a,!(a) \multimap b,!(b) \multimap a : \cdot \vdash b} D_{C}
 b,!(a) \multimap \overline{b,!(b) \multimap a : \cdot \vdash b}
\frac{b,!(a) \multimap b,!(b) \multimap a : \vdash !(b)}{b,!(a) \multimap b,!(b) \multimap a : \vdash !(b)} \stackrel{!}{\underbrace{b,!(a) \multimap b,!(b) \multimap a : a \vdash a}}
                   \frac{(b) \multimap a : \quad r : (b)}{b,!(a) \stackrel{\frown}{\multimap} b,!(b) \multimap a : \quad !(b) \multimap a \vdash a} \quad D_C
                         b,!(a)\multimap b,!(b)\multimap a: \cdot \vdash a
                                                           \cdot : !(!(a) \multimap b \& !(b) \multimap a) \vdash !(b) \multimap a \& !(a) \multimap b
file: KLE/KLE026+1.p (499 ms)
file: KLE/KLE027+1.p (646 ms)
```



```
file: KLE/KLE038+1.p (919 ms)
    file: KLE/KLE039+1.p (33 ms)
 \overline{a,b,c: \cdot \vdash a} \quad \overline{a,b,c: \cdot \vdash b} \quad \overline{a,b,c: \cdot \vdash c} \quad \overline{a,b,c: \cdot \vdash a} \quad \overline{a,b,c: \cdot \vdash b} \quad \overline{a,b,c: \cdot \vdash c}
                                                                                                           \cdot : \cdot \vdash !(a \& b \& c) \multimap a \& b \& c \& !(a \& b \& c) \multimap a \& b \& c
    file: KLE/KLE040+1.p (1384 ms)
  file: KLE/KLE041+1.p (42 ms)
 \overline{a,b: \cdot \vdash b} \quad a,b: \cdot \vdash a \quad a,b: \cdot \vdash a \quad a,b: \cdot \vdash b
                                             \cdot : \cdot \vdash !(a \& b) \multimap b \& a \& !(b \& a) \multimap a \& b
  file: KLE/KLE042+1.p (337 ms)
\frac{\overline{a,!(a)\oplus!(b):\cdot\vdash a}}{a,!(a)\oplus!(b):\cdot\vdash!(a)} \stackrel{!}{=} \frac{\overline{b,!(a)\oplus!(b):\cdot\vdash b}}{b,!(a)\oplus!(b):\cdot\vdash!(b)\oplus!(a)} \stackrel{!}{=} \frac{\overline{b,!(a)\oplus!(b):\cdot\vdash b}}{b,!(a)\oplus!(b):\cdot\vdash!(b)\oplus!(a)} \stackrel{!}{=} \frac{\overline{b,!(b)\oplus!(a):\cdot\vdash b}}{b,!(a)\oplus!(b):\cdot\vdash!(b)\oplus!(a)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash a}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)} \stackrel{!}{=} \frac{\overline{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}}{a,!(b)\oplus!(a):\cdot\vdash!(a)\oplus!(b)}
                                                                                                                                                                                                                                                                                                                                                                                                         \frac{!(b) \oplus !(a) : \ !(b) \oplus !(a) \vdash !(a) \oplus !(b)}{!(a) \oplus !(a) \oplus !(a)} D_C
                                                                 \frac{!(a) \oplus !(b) : \ !(a) \oplus !(b) \vdash !(b) \oplus !(a)}{!(a) \oplus !(b) : \ \vdash !(b) \oplus !(a)} \ D_C 
 \frac{!(b) \oplus !(a) : \ !(b) \oplus !(a) \vdash !(a) \oplus !(b)}{!(b) \oplus !(a) : \ \vdash !(a) \oplus !(b)} 
                                                                                                                                                                       \cdot : \cdot \vdash !(!(a) \oplus !(b)) \multimap !(b) \oplus !(a) \& !(!(b) \oplus !(a)) \multimap !(a) \oplus !(b)
     file: KLE/KLE043+1.p (408 ms)
                                                                                                                                                                                                                                 !(a \& b) \oplus !(a \& c) : \cdot \vdash a

\cdot \vdash !(a \& !(b) \oplus !(c)) \multimap !(a \& b) \oplus !(a \& c) \& !(!(a \& b) \oplus !(a \& c)) \multimap a \& !(b) \oplus !(c)
    file: KLE/KLE044+1.p (496 ms)
                                                                                                                                                                                   !(a) \oplus !(b \& c) : \cdot \vdash !(a) \oplus !(c)

!(!(a) \oplus !(b \& c)) \multimap !(a) \oplus !(b) \& !(a) \oplus !(c) \& !(!(a) \oplus !(b) \& !(a) \oplus !(c)) \multimap !(a) \oplus !(b \& c)
```

file: KLE/KLE045+1.p (26 ms)

file: KLE/KLE050+1.p (36 ms)

```
b,!(a) \multimap b: \cdot \vdash b \quad a,b: \cdot \vdash b
     : !(b) \vdash !(!(a) \multimap b) \multimap b \& !(b) \multimap !(a) \multimap b
   file: KLE/KLE051+1.p (123 ms)
\frac{\overline{a,!(a) \multimap b,!(a) \multimap 0: \vdash a}}{\underbrace{a,!(a) \multimap b,!(a) \multimap 0: \vdash l(a)}} : \underbrace{\frac{\overline{a,!(a) \multimap b,!(a) \multimap 0: \bullet \vdash 0}}{a,!(a) \multimap b,!(a) \multimap 0: \bullet \vdash 0}}_{a,!(a) \multimap b,!(a) \multimap 0: \vdash \vdash 0} \times \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash a}}{a,!(a) \multimap 0: \vdash \vdash !(a)}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash a}}{a,!(a) \multimap 0: \vdash \vdash !(a)}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash a}}{a,!(a) \multimap 0: \vdash \vdash !(a)}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash a}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) \multimap 0: \vdash b}}{a,!(a) \multimap 0: \vdash b}}_{\bullet} : \underbrace{\frac{\overline{a,!(a) 
    file: KLE/KLE052+1.p (331 ms)
     file: KLE/KLE053+1.p (40 ms)
             a,b: \cdot \vdash a \quad a,b: \cdot \vdash a \quad a,b: \cdot \vdash b
                                                                   !(b) \vdash !(a \& b) \multimap a \& !(a) \multimap a \& b
                                                                                                                                                                                                                                                                                                                                                                                                          \frac{\overline{b}: \cdot \vdash \overline{b}}{b: \cdot \vdash !(b)} !
                                                         \frac{}{b,!(a)\oplus !(b): \cdot \vdash b} \quad \frac{}{b: \cdot \vdash !(a)\oplus !(b)} \quad \oplus_{1}
                                                      !(b) \vdash !(!(a) \oplus !(b)) \multimap b \& !(b) \multimap !(a) \oplus !(b)
     file: KLE/KLE055+1.p (94 ms)
```

```
\overline{b,!(b)} \multimap \mathbf{0} : \cdot \vdash b
                                                               \frac{b,!(b)\multimap \mathbf{0}: \cdot \vdash b}{b,!(b)\multimap \mathbf{0}: \cdot \vdash !(b)} \; ! \; \frac{b,!(b)\multimap \mathbf{0}: \; \mathbf{0}\vdash a}{b,!(b)\multimap \mathbf{0}: \; \mathbf{0}\vdash a} \; \star
                                                                                        \frac{b,!(b) \multimap \mathbf{0} : !(b) \multimap \mathbf{0} \vdash a}{b,!(b) \multimap \mathbf{0} : \cdot \vdash a} D_C
                                                                                                                                                                                                        b,!(b) \multimap \mathbf{0}: \cdot \vdash b
a, b, !(b) \multimap \mathbf{0} : \cdot \vdash b
                                                                : !(!(b) \multimap \mathbf{0}) \vdash !(a \& b) \multimap b \& !(b) \multimap a \& b
 file: KLE/KLE056+1.p (297 ms)
                                                                 \overline{b,!(a)\oplus!(b),!(b)\multimap\mathbf{0}:\ \cdot \vdash b}
                                                              \frac{b,!(a) \oplus !(b),!(b) \multimap 0 : \cdot \vdash !(b)}{b,!(a) \oplus !(b),!(b) \multimap 0 : \cdot \vdash !(b)} \cdot \frac{b,!(a) \oplus !(b),!(b) \multimap 0 : 0 \vdash a}{b,!(a) \oplus !(b),!(b) \multimap 0 : \cdot \vdash a} \xrightarrow{b} D_{C}
                                                                                                                                                                                                                \frac{\overline{a,!(b)} \multimap \mathbf{0} : \cdot \vdash a}{a,!(b) \multimap \mathbf{0} : \cdot \vdash !(a)} !
a,!(a)\oplus !(b),!(b)\multimap \mathbf{0}: \cdot \vdash a
                                         \underline{!(a) \oplus !(b)},\underline{!(b) \multimap \mathbf{0} : !(a) \oplus !(b) \vdash a}
                                                   !(a) \oplus !(b), !(b) \multimap \mathbf{0} : \cdot \vdash a
                                                                                                  \cdot : !(!(b) \multimap \mathbf{0}) \vdash !(!(a) \oplus !(b)) \multimap a \& !(a) \multimap !(a) \oplus !(b)
 file: KLE/KLE057+1.p (74 ms)
      a,!(a) \multimap \mathbf{0} : \cdot \vdash a
\frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)}{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)} ! \frac{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash \mathbf{0}}{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash \mathbf{0}} \star
                                                a, !(a) \multimap \mathbf{0} : !(a) \multimap \mathbf{0} \vdash \mathbf{0}
                                                                      a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}
                                       \overline{\cdot : \cdot \vdash !(a) \multimap !(!(a) \multimap \mathbf{0}) \multimap \mathbf{0}}
 file: KLE/KLE058+1.p (568 ms)
  file: KLE/KLE059+1.p (214 ms)
         a,!(a) \oplus !(!(a) \multimap \mathbf{0}),!(!(a) \multimap a) \multimap \mathbf{0} : \cdot \vdash a
  \frac{1(a) \oplus !(!(a) \multimap \mathbf{0}), !(!(a) \multimap a) \multimap \mathbf{0} : \vdash !(a) \multimap a}{(a) \oplus !(!(a) \multimap \mathbf{0}), !(!(a) \multimap a) \multimap \mathbf{0} : \vdash !(a) \multimap a} \star
\frac{(a) \oplus !(!(a) \multimap 0),!(!(a) \multimap a) \multimap 0 : \ \cdot \vdash !(!(a) \multimap a)}{!(a) \oplus !(!(a) \multimap 0),!(!(a) \multimap a) \multimap 0 : \ \cdot \vdash !(!(a) \multimap a)} \ ! \ \frac{!(a) \oplus !(!(a) \multimap 0),!(!(a) \multimap a) \multimap 0 : \ 0 \vdash 0}{!(a) \oplus !(!(a) \multimap 0),!(!(a) \multimap a) \multimap 0 : \ 0 \vdash 0} \ \star
                                                     !(a) \oplus !(!(a) \multimap \mathbf{0}), !(!(a) \multimap a) \multimap \mathbf{0} : !(!(a) \multimap a) \multimap \mathbf{0} \vdash \mathbf{0}
                                                                         !(a) \oplus !(!(a) \multimap \mathbf{0}), !(!(a) \multimap a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}
                                                          \vdots \vdash !(!(a) \oplus !(!(a) \multimap \mathbf{0})) \multimap !(!(!(a) \multimap a) \multimap \mathbf{0}) \multimap \mathbf{0}
 file: KLE/KLE060+1.p (214 ms)
```

```
\frac{a,!(a)\oplus !(!(a)\multimap 0),!(!(a)\multimap a\&!(a)\multimap a)\multimap 0: \vdash a}{\underbrace{!(a)\oplus !(!(a)\multimap 0),!(!(a)\multimap a\&!(a)\multimap 0: \vdash \vdash a}_{!(a)\oplus !(!(a)\multimap 0),!(!(a)\multimap a\&!(a)\multimap a)} : \vdash \underbrace{!(a)\oplus !(!(a)\multimap 0),!(!(a)\multimap a\&!(a)\multimap a)}_{!(a)\oplus !(a)\oplus a} : \vdash \underbrace{!(a)\multimap a\&!(a)\multimap a}_{!(a)\oplus a} : \vdash \underbrace{!(a)\multimap a}_{!(a)\oplus a} : \vdash \underbrace{!(a)\multimap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  10 \oplus !(!(a) \multimap 0), !(!(a) \multimap a \& !(a) \multimap a) \multimap 0 : 0 \vdash 0
                                                                                  \overline{!(a) \oplus !(!(a) \multimap \mathbf{0}), !(!(a) \multimap a \& !(a) \multimap a) \multimap \mathbf{0} : \cdot \vdash !(!(a) \multimap a \& !(a) \multimap a)}
                                                                                                                                                                                                                                     \begin{array}{c} (a) \oplus !(!(a) \rightarrow 0), !(!(a) \rightarrow a) & !(a) \oplus !(!(a) \rightarrow 0), !(!(a) \rightarrow 0), !(!(a) \rightarrow 0), !(!(a) \rightarrow 0), !(!(a) \rightarrow a) \rightarrow 0 \\ \hline (a) \oplus !(!(a) \rightarrow 0), !(!(a) \rightarrow a) \oplus !(a) \rightarrow 0, !(!(a) \rightarrow a) \rightarrow 0 \\ \hline (a) \oplus !(!(a) \rightarrow 0), !(!(a) \rightarrow a) \oplus !(a) \rightarrow 0, !(a) \rightarrow 0 \\ \hline \end{array} 
                                                                                                                                                                                                                                                                        \cdot : \cdot \vdash !(!(a) \oplus !(!(a) \multimap \mathbf{0})) \multimap !(!(!(a) \multimap a \& !(a) \multimap a) \multimap \mathbf{0}) \multimap \mathbf{0}
    file: KLE/KLE061+1.p (70 ms)
                   a,!(a) \multimap \mathbf{0} : \cdot \vdash a
\overline{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)} \quad ! \quad \overline{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash \mathbf{0}}
                                                                                                                                   a, !(a) \multimap \mathbf{0} : !(a) \multimap \mathbf{0} \vdash \mathbf{0}
                                                                                                                                            a,!(a) \multimap \mathbf{0}: \cdot \vdash \mathbf{0}
                                                                                                                                    \cdot : \cdot \vdash !(a \& !(a) \multimap \mathbf{0}) \multimap \mathbf{0}
     file: KLE/KLE062+1.p (392 ms)
      file: KLE/KLE063+1.p (307 ms)
    file: KLE/KLE064+1.p (280 ms)
                 \overline{a,!(!(a)\multimap a)\multimap \mathbf{0},!(!(!(!(a)\multimap a)\multimap \mathbf{0})\multimap \mathbf{0})\multimap \mathbf{0}:\ \cdot\vdash a}
        \overline{!(!(a)\multimap a)\multimap 0,!(!(!(!(a)\multimap a)\multimap 0)\multimap 0)\multimap 0: \cdot \vdash !(a)\multimap a}
   \frac{(!(a) \circ a) \circ 0; (!(!(!(a) \circ a) \circ 0) \circ 0; 0) \circ 0 \circ 0}{!(!(a) \circ a) \circ 0; (!(!(!(a) \circ a) \circ 0) \circ 0) \circ 0} \circ 0 \circ 0 \circ 0 \circ 0} \circ 1
                                                                                                                 \frac{!(!(a) \multimap a) \multimap 0,!(!(!(!(a) \multimap a) \multimap 0) \multimap 0) \multimap 0: \ !(!(a) \multimap a) \multimap 0 \vdash 0}{D_C}
                                                                                                                                         \frac{!(!(!(!(a) \multimap a) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(!(!(a) \multimap a) \multimap \mathbf{0}) \multimap \mathbf{0}}{!}
                                                                                                                                   \overline{|(!(!(!(a)\multimap a)\multimap \mathbf{0})\multimap \mathbf{0})\multimap \mathbf{0}: \cdot \vdash !(!(!(!(a)\multimap a)\multimap \mathbf{0})\multimap \mathbf{0})}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               \overline{|(!(!(!(a)\multimap a)\multimap \mathbf{0})\multimap \mathbf{0}:\ \mathbf{0}\vdash \mathbf{0}}^{\star}
                                                                                                                                                                                                                                                                                  \frac{|(!(!(!(a) \multimap a) \multimap 0) \multimap 0) \multimap 0 : \ |(!(!(!(a) \multimap a) \multimap 0) \multimap 0) \multimap 0 \vdash 0}{|(!(!(!(a) \multimap a) \multimap 0) \multimap 0) \multimap 0} D_{C}
                                                                                                                                                                                                                                                                                                                                            !(!(!(!(a) \multimap a) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}
                                                                                                                                                                                                                                                                                                                                     \overline{ \cdot : \cdot \vdash !(!(!(!(!(a) \multimap a) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0} } 
     file: KLE/KLE065+1.p (23 ms)
```

```
a,!(b)\oplus !(!(b)\multimap \mathbf{0}): \cdot \vdash a
                                                                             \cdot \vdash !(a \& !(b) \oplus !(!(b) \multimap \mathbf{0})) \multimap a
     file: KLE/KLE066+1.p (112 ms)
                                                                                                                                                                                        \overline{b,!(a)\oplus!(b\&!(b)\multimap\mathbf{0}),!(b)\multimap\mathbf{0}:\ \cdot\vdash b}
                                                                                                                                                                                  \frac{b,!(a) \oplus !(b \& !(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : \vdash b}{b,!(a) \oplus !(b \& !(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : \vdash !(b)} ! \frac{b,!(a) \oplus !(b \& !(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : \mathbf{0} \vdash a}{b,!(a) \oplus !(b \& !(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : !(b) \multimap \mathbf{0} \vdash a} \frac{b,!(a) \oplus !(b \& !(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : !(b) \multimap \mathbf{0} \vdash a}{b,!(a) \oplus !(b \& !(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : \vdash a} \mathcal{D}_{C}
\overline{a,!(a)\oplus!(b\&!(b)\multimap\mathbf{0}):\cdot\vdash a}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            \frac{\overline{a:\cdot\vdash a}}{a:\cdot\vdash!(a)} \;\;!
                                                                                                                               \underbrace{!(a) \oplus !(b \& !(b) \multimap \mathbf{0}) : \ !(a) \oplus !(b \& !(b) \multimap \mathbf{0}) \vdash a}_{D_C}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             \frac{a : \cdot \vdash !(a) \oplus !(b \& !(b) \multimap \mathbf{0})}{a : \cdot \vdash !(a) \oplus !(b \& !(b) \multimap \mathbf{0})} \oplus_{1}
                                                                                                                                                                                        !(a) \oplus !(b \& !(b) \multimap \mathbf{0}) : \cdot \vdash a
                                                                                                                                                                                                                                                                                                                                          \cdot: \cdot \vdash !(!(a) \oplus !(b & !(b) \multimap 0)) \multimap a & !(a) \multimap !(a) \oplus !(b & !(b) \multimap 0)
  file: KLE/KLE067+1.p (148 ms)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            \frac{\overbrace{b,!(b) \multimap 0: \cdot \vdash b}^{\begin{subarray}{c} b,!(b) \multimap 0: \cdot \vdash b \\ \hline b,!(b) \multimap 0: \cdot \vdash !(b) \\ \hline \\ \begin{subarray}{c} b,!(b) \multimap 0: !(b) \multimap 0 \vdash 0 \\ \hline \\ \begin{subarray}{c} b,!(b) \multimap 0: \cdot \vdash 0 \\ \hline \\ \begin{subarray}{c} b,!(b) \multimap 0: \cdot \vdash 0 \\ \hline \\ \end{subarray}} \begin{subarray}{c} D_C \\ \hline \end{subarray}
                                                                                                     \frac{a, b, !(b) \multimap 0 : \cdot \vdash b}{\underbrace{a, b, !(b) \multimap 0 : \cdot \vdash [b)}_{} !} \cdot \underbrace{\frac{a, b, !(b) \multimap 0 : 0 \vdash 0}{a, b, !(b) \multimap 0 \vdash 0}}_{DC} \star \underbrace{\frac{b, !(b) \multimap 0 : \cdot \vdash b}{b, !(b) \multimap 0 : \cdot \vdash [b]}}_{\underbrace{b, !(b) \multimap 0 : \cdot \vdash [b]}_{} !} \cdot \underbrace{\frac{b, !(b) \multimap 0 : 0 \vdash a}_{b, !(b) \multimap 0 \vdash 0}}_{\underbrace{b, !(b) \multimap 0 : \cdot \vdash a}}_{\underbrace{b, !(b) \multimap 0 : \cdot \vdash a}}
 a, b, !(b) \multimap \mathbf{0} : \cdot \vdash b
                                                                                                                                                                                                                                             \vdash !(a \& b \& !(b) \multimap \mathbf{0}) \multimap b \& !(b) \multimap \mathbf{0} \& !(b \& !(b) \multimap \mathbf{0}) \multimap a \& b \& !(b) \multimap \mathbf{0}
    file: KLE/KLE068+1.p (timeout!)
      file: KLE/KLE069+1.p (timeout!)
      file: KLE/KLE070+1.p (286 ms)
    file: KLE/KLE071+1.p (256 ms)
                                                                                                                                                                                              file: KLE/KLE072+1.p (280 ms)
```

```
file: KLE/KLE073+1.p (256 ms)
file: KLE/KLE074+1.p (timeout!)
file: KLE/KLE075+1.p (timeout!)
file: KLE/KLE076+1.p (352 ms)
file: KLE/KLE077+1.p (250 ms)
file: KLE/KLE078+1.p (timeout!)
file: KLE/KLE079+1.p (346 ms)
```

```
file: KLE/KLE080+1.p (83 ms)
                                                                                   \frac{\overline{a,b,!(a)\multimap !(b)\multimap \mathbf{0}: \ \cdot \vdash b}}{\underline{a,b,!(a)\multimap !(b)\multimap \mathbf{0}: \ \cdot \vdash !(b)}} \ ! \ \overline{a,b,!(a)\multimap !(b)\multimap \mathbf{0}: \ \mathbf{0}\vdash \mathbf{0}}
  \overline{a,b,!(a)\multimap !(b)\multimap \mathbf{0}: \cdot \vdash a}
\underline{a,b,!(a)\multimap!(b)\multimap\mathbf{0}: \vdash !(a)} !
                                                                                        a, b, !(a) \multimap !(b) \multimap \mathbf{0} : !(b) \multimap \mathbf{0} \vdash \mathbf{0}
                                                \frac{a,b,!(a)\multimap !(b)\multimap \mathbf{0}: \ !(a)\multimap !(b)\multimap \mathbf{0}\vdash \mathbf{0}}{a,b,!(a)\multimap !(b)\multimap \mathbf{0}: \ \vdash \mathbf{0}} D_C
\vdots \vdash !(a \& b)\multimap !(!(a)\multimap !(b)\multimap \mathbf{0})\multimap \mathbf{0}
 file: KLE/KLE081+1.p (294 ms)
 file: KLE/KLE082+1.p (403 ms)
 file: KLE/KLE083+1.p (timeout!)
 file: KLE/KLE085+1.p (timeout!)
 file: KLE/KLE086+1.p (timeout!)
 file: KLE/KLE087+1.p (278 ms)
```



file: KLE/KLE088+1.p (timeout!)

4.2 LCL Problems

file: LCL/LCL181+1.p (timeout!)
file: LCL/LCL230+1.p (timeout!)

4.3 SYJ Problems

file: SYJ/SYJ101+1.p (26 ms)

 $\frac{\overline{a:\cdot\vdash a}}{\cdot:\ !(a)\vdash a}\ \star$

file: SYJ/SYJ102+1.p (66 ms)

$$\frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash a}{\underbrace{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)}} ! \frac{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash \mathbf{0}}{\underbrace{a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}} \stackrel{\star}{-\circ} \frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}{\underbrace{a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}} D_C \\
 \frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}{\cdot : \cdot \vdash (a) \vdash !(!(a) \multimap \mathbf{0}) \multimap \mathbf{0}} \stackrel{\star}{\times}$$

file: SYJ/SYJ103+1.p (timeout!)

file: SYJ/SYJ104+1.p (60 ms)

```
a,!(a) \multimap b: \cdot \vdash a
\frac{a, \cdot (a) \multimap b : \neg a}{a, !(a) \multimap b : \neg b : b \vdash b}
                          a, !(a) \multimap b : !(a) \multimap b \vdash b
                                      a,!(a) \multimap b : \cdot \vdash b
                          \overline{\cdot : \ !(!(a) \multimap b) \vdash !(a) \multimap b}
 file: SYJ/SYJ105+1.002.p (311 ms)
file: SYJ/SYJ105+1.003.p (timeout!)
 file: SYJ/SYJ105+1.004.p (timeout!)
 file: SYJ/SYJ106+1.p (1549 ms)
 file: SYJ/SYJ107+1.001.p (489 ms)
                                             !(!(b) \oplus !(a)) \oplus !(b) : \cdot \vdash !(a) \oplus !(b \& c)
                                                                                  !(!(b)\oplus !(a))\oplus !(b)\vdash !(a)\oplus !(b\ \&\ c) D_C
                                                                       \frac{c,!(!(b)\oplus !(a))\oplus !(b): \cdot \vdash !(a)\oplus !(b\&c)}{\cdot : \cdot !(c),!(!(!(b)\oplus !(a))\oplus !(b))\vdash !(a)\oplus !(b\&c)} \star
file: SYJ/SYJ107+1.002.p (13734 ms)
file: SYJ/SYJ107+1.003.p (timeout!)
file: SYJ/SYJ107+1.004.p (timeout!)
 file: SYJ/SYJ201+1.002.p (timeout!)
 file: SYJ/SYJ201+1.003.p (timeout!)
file: SYJ/SYJ201+1.004.p (timeout!)
```

```
file: SYJ/SYJ201+1.005.p (timeout!)
```

file: SYJ/SYJ201+1.006.p (timeout!)

file: SYJ/SYJ201+1.007.p (timeout!)

file: SYJ/SYJ201+1.008.p (timeout!)

file: SYJ/SYJ201+1.009.p (timeout!)

file: SYJ/SYJ201+1.010.p (timeout!)

file: SYJ/SYJ201+1.011.p (timeout!)

file: SYJ/SYJ201+1.012.p (timeout!)

file: SYJ/SYJ201+1.013.p (timeout!)

file: SYJ/SYJ201+1.014.p (timeout!)

file: SYJ/SYJ201+1.015.p (timeout!)

file: SYJ/SYJ201+1.016.p (timeout!)

file: SYJ/SYJ201+1.017.p (timeout!)

file: SYJ/SYJ201+1.018.p (timeout!)

file: SYJ/SYJ201+1.019.p (timeout!)

file: SYJ/SYJ201+1.020.p (timeout!)

file: SYJ/SYJ202+1.001.p (38 ms)

$$\frac{\overbrace{o11,o21: \cdot \vdash o11}^{o11,o21: \cdot \vdash o11}!}{\underbrace{o11,o21: \cdot \vdash !(o11) \oplus !(o21)}^{\oplus 1}} \xrightarrow{(o11),o21: \cdot \vdash !(o11) \oplus !(o21)}^{\bullet 1}$$

file: SYJ/SYJ202+1.002.p (timeout!)

file: SYJ/SYJ202+1.003.p (timeout!)

file: SYJ/SYJ202+1.004.p (timeout!)

file: SYJ/SYJ202+1.005.p (timeout!)

file: SYJ/SYJ202+1.006.p (timeout!)

file: SYJ/SYJ202+1.007.p (timeout!)
file: SYJ/SYJ202+1.008.p (timeout!)

file: SYJ/SYJ202+1.009.p (timeout!)

file: SYJ/SYJ202+1.010.p (timeout!)

file: SYJ/SYJ202+1.011.p (timeout!)

file: SYJ/SYJ202+1.012.p (timeout!)

file: SYJ/SYJ202+1.013.p (timeout!)

file: SYJ/SYJ202+1.014.p (timeout!)

file: SYJ/SYJ202+1.015.p (timeout!)

file: SYJ/SYJ202+1.016.p (timeout!)

file: SYJ/SYJ202+1.017.p (timeout!)

```
file: SYJ/SYJ202+1.018.p (timeout!)
 file: SYJ/SYJ202+1.019.p (timeout!)
 file: SYJ/SYJ202+1.020.p (timeout!)
file: SYJ/SYJ203+1.001.p (356 ms)
                \overline{p1,!(!(p1)\oplus !(!(p1)\multimap f))\multimap f:\ \cdot \vdash p1}
              \overline{p1,!(!(p1)\oplus !(!(p1)\multimap f))\multimap f:\ \cdot \vdash !(p1)}
 \overline{p1,!(!(p1)\oplus !(!(p1)\multimap f))\multimap f:\ \cdot\vdash !(p1)\oplus !(!(p1)\multimap f)}
p1,!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f : \cdot \vdash !(!(p1) \oplus !(!(p1) \multimap f))
                                                                                                            p1,!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f : f \vdash f
                               \underbrace{p1,!(!(p1)\oplus !(!(p1)\multimap f))}_{} \circ f: \ !(!(p1)\oplus !(!(p1)\multimap f)) \multimap f\vdash f
                                                      p1,!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f : \cdot \vdash f
                                                   \overline{!(!(p1)\oplus !(!(p1)\multimap f))\multimap f:\ \cdot \vdash !(p1)}\multimap f
                                          \frac{\overline{!(!(p1)\oplus !(!(p1)\multimap f))\multimap f:\ \cdot\vdash !(!(p1)\multimap f)}}{!(!(p1)\oplus !(!(p1)\multimap f))\multimap f:\ \cdot\vdash !(p1)\oplus !(!(p1)\multimap f)}
                                        \frac{!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f : \cdot \vdash !(!(p1) \oplus !(!(p1) \multimap f))}{!(!(p1) \oplus !(!(p1) \multimap f))}
                                                                                                                                                                                         \overline{!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f : f \vdash f}
                                                                                         \frac{!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f : \ !(!(p1) \oplus !(!(p1) \multimap f)) \multimap f \vdash f}{\frac{!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f : \ \vdash f}{\cdot : \ !(!(!(p1) \oplus !(!(p1) \multimap f)) \multimap f) \vdash f}} \ \star
 file: SYJ/SYJ203+1.002.p (2330 ms)
file: SYJ/SYJ203+1.003.p (2648 ms)
```

file: SYJ/SYJ203+1.004.p (3158 ms)

```
file: SYJ/SYJ203+1.005.p (4545 ms)
 file: SYJ/SYJ203+1.010.p (timeout!)
 file: SYJ/SYJ203+1.011.p (timeout!)
 file: SYJ/SYJ203+1.012.p (timeout!)
 file: SYJ/SYJ203+1.013.p (timeout!)
 file: SYJ/SYJ203+1.014.p (timeout!)
 file: SYJ/SYJ203+1.015.p (timeout!)
 file: SYJ/SYJ203+1.016.p (timeout!)
 file: SYJ/SYJ203+1.017.p (timeout!)
 file: SYJ/SYJ203+1.018.p (timeout!)
 file: SYJ/SYJ203+1.019.p (timeout!)
 file: SYJ/SYJ203+1.020.p (timeout!)
 file: SYJ/SYJ204+1.001.p (85 ms)
                                                         \frac{\overline{p1,!(p1) \multimap !(p1) \multimap p0 : \cdot \vdash p1}}{p1,!(p1) \multimap !(p1) \multimap p0 : \cdot \vdash !(p1)} \; ! \; \frac{}{p1,!(p1) \multimap !(p1) \multimap p0 : \; p0 \vdash p0}
\frac{\overline{p1,!(p1) \multimap !(p1) \multimap p0 : \cdot \vdash p1}}{p1,!(p1) \multimap !(p1) \multimap p0 : \cdot \vdash !(p1)} \;\;!
                                                            p1,!(p1) \multimap !(p1) \multimap p0 : !(p1) \multimap p0 \vdash p0
                                 \frac{p1,!(p1) \multimap !(p1) \multimap p0 : !(p1) \multimap !(p1) \multimap p0 \vdash p0}{p1,!(p1) \multimap !(p1) \multimap p0 : \cdot \vdash p0 \over \cdot : !(p1),!(!(p1) \multimap !(p1) \multimap p0) \vdash p0} \star D_{C}
 file: SYJ/SYJ204+1.002.p (351 ms)
 file: SYJ/SYJ204+1.003.p (503 ms)
 file: SYJ/SYJ204+1.004.p (984 ms)
```

file: SYJ/SYJ204+1.008.p (timeout!) file: SYJ/SYJ204+1.009.p (timeout!) file: SYJ/SYJ204+1.010.p (timeout!) file: SYJ/SYJ204+1.011.p (timeout!) file: SYJ/SYJ204+1.012.p (timeout!) file: SYJ/SYJ204+1.013.p (timeout!) file: SYJ/SYJ204+1.014.p (timeout!) file: SYJ/SYJ204+1.015.p (timeout!) file: SYJ/SYJ204+1.016.p (timeout!) file: SYJ/SYJ204+1.017.p (timeout!) file: SYJ/SYJ204+1.018.p (timeout!) file: SYJ/SYJ204+1.019.p (timeout!) file: SYJ/SYJ204+1.020.p (timeout!) file: SYJ/SYJ205+1.001.p (2907 ms) file: SYJ/SYJ205+1.002.p (5855 ms) file: SYJ/SYJ205+1.003.p (8888 ms) file: SYJ/SYJ205+1.004.p (18028 ms) file: SYJ/SYJ205+1.005.p (80827 ms) file: SYJ/SYJ205+1.006.p (timeout!) file: SYJ/SYJ205+1.007.p (timeout!) file: SYJ/SYJ205+1.008.p (timeout!) file: SYJ/SYJ205+1.009.p (timeout!) file: SYJ/SYJ205+1.010.p (timeout!) file: SYJ/SYJ205+1.011.p (timeout!) file: SYJ/SYJ205+1.012.p (timeout!)

```
file: SYJ/SYJ205+1.013.p (timeout!)

file: SYJ/SYJ205+1.014.p (timeout!)

file: SYJ/SYJ205+1.015.p (timeout!)

file: SYJ/SYJ205+1.016.p (timeout!)

file: SYJ/SYJ205+1.017.p (timeout!)

file: SYJ/SYJ205+1.018.p (timeout!)

file: SYJ/SYJ205+1.019.p (timeout!)

file: SYJ/SYJ205+1.020.p (timeout!)

file: SYJ/SYJ205+1.020.p (timeout!)
```

 $a1: \cdot \vdash a1 \quad a1: \cdot \vdash a1$

 $\cdot: \cdot \vdash !(a1) \multimap a1 \& !(a1) \multimap a1$

file: SYJ/SYJ206+1.002.p (253 ms)

 $\frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(a) \circ az.(az) \circ az. \mapsto az}{a!(a) \circ az.(a) \circ az. \mapsto az} = \frac{a!(a) \circ az.(az) \circ az. \mapsto az}{a!(a) \circ az.(az) \circ az. \mapsto az} = \frac{a!(a) \circ az.(az) \circ az.(az) \circ az. \mapsto az}{a!(a) \circ az.(az) \circ az. \mapsto az} = \frac{a!(a) \circ az.(az) \circ az.(az) \circ az. \mapsto az}{a!(a) \circ az.(az) \circ az. \mapsto az} = \frac{a!(a) \circ az.(az) \circ az.($

file: SYJ/SYJ206+1.003.p (3374 ms)

file: SYJ/SYJ206+1.004.p (timeout!)
file: SYJ/SYJ206+1.005.p (timeout!)

file: SYJ/SYJ206+1.006.p (timeout!)

file: SYJ/SYJ206+1.007.p (timeout!)

file: SYJ/SYJ206+1.008.p (timeout!)

file: SYJ/SYJ206+1.009.p (timeout!)
file: SYJ/SYJ206+1.010.p (timeout!)

file: SYJ/SYJ206+1.011.p (timeout!)

file: SYJ/SYJ206+1.012.p (timeout!)

file: SYJ/SYJ206+1.013.p (timeout!)

file: SYJ/SYJ206+1.014.p (timeout!)

file: SYJ/SYJ206+1.015.p (timeout!)

file: SYJ/SYJ206+1.016.p (timeout!)

file: SYJ/SYJ206+1.017.p (timeout!)

file: SYJ/SYJ206+1.018.p (timeout!)

file: SYJ/SYJ206+1.019.p (timeout!)

- file: SYJ/SYJ207+1.001.p (timeout!)
- file: SYJ/SYJ207+1.002.p (timeout!)
- file: SYJ/SYJ207+1.003.p (timeout!)
- file: SYJ/SYJ207+1.004.p (timeout!)
- file: SYJ/SYJ207+1.005.p (timeout!)
- file: SYJ/SYJ207+1.006.p (timeout!)
- file: SYJ/SYJ207+1.007.p (timeout!)
- file: SYJ/SYJ207+1.008.p (timeout!)
- file: SYJ/SYJ207+1.009.p (timeout!)
- file: SYJ/SYJ207+1.010.p (timeout!)
- file: SYJ/SYJ207+1.011.p (timeout!)
- file: SYJ/SYJ207+1.012.p (timeout!)
- file: SYJ/SYJ207+1.013.p (timeout!)
- file: SYJ/SYJ207+1.014.p (timeout!)
- file: SYJ/SYJ207+1.015.p (timeout!)
- file: SYJ/SYJ207+1.016.p (timeout!)
- file: SYJ/SYJ207+1.017.p (timeout!)
- file: SYJ/SYJ207+1.018.p (timeout!)
- file: SYJ/SYJ207+1.019.p (timeout!)
- file: SYJ/SYJ207+1.020.p (timeout!)
- file: SYJ/SYJ208+1.001.p (timeout!)
- file: SYJ/SYJ208+1.002.p (timeout!)
- file: SYJ/SYJ208+1.003.p (timeout!)
- file: SYJ/SYJ208+1.004.p (timeout!)
- file: SYJ/SYJ208+1.005.p (timeout!)
- file: SYJ/SYJ208+1.006.p (timeout!)
- file: SYJ/SYJ208+1.007.p (timeout!)
- file: SYJ/SYJ208+1.008.p (timeout!)
- file: SYJ/SYJ208+1.009.p (timeout!)
 file: SYJ/SYJ208+1.010.p (timeout!)
- file: SYJ/SYJ208+1.011.p (timeout!)
- file: SYJ/SYJ208+1.012.p (timeout!)
- file: SYJ/SYJ208+1.013.p (timeout!)
- file: SYJ/SYJ208+1.014.p (timeout!)
- file: SYJ/SYJ208+1.015.p (timeout!)
- file: SYJ/SYJ208+1.016.p (timeout!)

- file: SYJ/SYJ208+1.017.p (timeout!)
- file: SYJ/SYJ208+1.018.p (timeout!)
- file: SYJ/SYJ208+1.019.p (timeout!)
- file: SYJ/SYJ209+1.001.p (timeout!)
- file: SYJ/SYJ209+1.002.p (timeout!)
- file: SYJ/SYJ209+1.003.p (timeout!)
- file: SYJ/SYJ209+1.004.p (timeout!)
- file: SYJ/SYJ209+1.005.p (timeout!)
- file: SYJ/SYJ209+1.006.p (timeout!)
- file: SYJ/SYJ209+1.007.p (timeout!)
- file: SYJ/SYJ209+1.008.p (timeout!)
- iiic. bio/biozoo:i.ooo.p (oimcouo.)
- file: SYJ/SYJ209+1.009.p (timeout!)
- file: SYJ/SYJ209+1.010.p (timeout!)
- file: SYJ/SYJ209+1.011.p (timeout!)
- file: SYJ/SYJ209+1.012.p (timeout!)
- file: SYJ/SYJ209+1.013.p (timeout!)
- file: SYJ/SYJ209+1.014.p (timeout!)
- file: SYJ/SYJ209+1.015.p (timeout!)
- file: SYJ/SYJ209+1.016.p (timeout!)
- file: SYJ/SYJ209+1.017.p (timeout!)
- file: SYJ/SYJ209+1.018.p (timeout!)
- file: SYJ/SYJ209+1.019.p (timeout!)
- file: SYJ/SYJ209+1.020.p (timeout!)
- file: SYJ/SYJ210+1.001.p (timeout!)
- file: SYJ/SYJ210+1.002.p (timeout!)
- file: SYJ/SYJ210+1.003.p (timeout!)
- file: SYJ/SYJ210+1.004.p (timeout!)
- file: SYJ/SYJ210+1.005.p (timeout!)
- file: SYJ/SYJ210+1.006.p (timeout!)
- file: SYJ/SYJ210+1.007.p (timeout!)
- file: SYJ/SYJ210+1.008.p (timeout!)
- file: SYJ/SYJ210+1.009.p (timeout!)
- file: SYJ/SYJ210+1.010.p (timeout!)
- file: SYJ/SYJ210+1.011.p (timeout!)
- file: SYJ/SYJ210+1.012.p (timeout!)

```
file: SYJ/SYJ210+1.013.p (timeout!)
file: SYJ/SYJ210+1.014.p (timeout!)
file: SYJ/SYJ210+1.015.p (timeout!)
file: SYJ/SYJ210+1.016.p (timeout!)
file: SYJ/SYJ210+1.017.p (timeout!)
file: SYJ/SYJ210+1.018.p (timeout!)
file: SYJ/SYJ210+1.019.p (timeout!)
file: SYJ/SYJ210+1.020.p (timeout!)
file: SYJ/SYJ211+1.001.p (timeout!)
file: SYJ/SYJ211+1.002.p (timeout!)
file: SYJ/SYJ211+1.003.p (timeout!)
file: SYJ/SYJ211+1.004.p (timeout!)
file: SYJ/SYJ211+1.005.p (timeout!)
file: SYJ/SYJ211+1.006.p (timeout!)
file: SYJ/SYJ211+1.007.p (timeout!)
file: SYJ/SYJ211+1.008.p (timeout!)
file: SYJ/SYJ211+1.009.p (timeout!)
file: SYJ/SYJ211+1.010.p (timeout!)
file: SYJ/SYJ211+1.011.p (timeout!)
file: SYJ/SYJ211+1.012.p (timeout!)
file: SYJ/SYJ211+1.013.p (timeout!)
file: SYJ/SYJ211+1.014.p (timeout!)
file: SYJ/SYJ211+1.015.p (timeout!)
file: SYJ/SYJ211+1.016.p (timeout!)
file: SYJ/SYJ211+1.017.p (timeout!)
file: SYJ/SYJ211+1.018.p (timeout!)
file: SYJ/SYJ211+1.019.p (timeout!)
file: SYJ/SYJ211+1.020.p (timeout!)
file: SYJ/SYJ212+1.001.p (381 ms)
file: SYJ/SYJ212+1.002.p (timeout!)
file: SYJ/SYJ212+1.003.p (timeout!)
file: SYJ/SYJ212+1.004.p (timeout!)
file: SYJ/SYJ212+1.005.p (timeout!)
```

```
file: SYJ/SYJ212+1.006.p (timeout!)
file: SYJ/SYJ212+1.007.p (timeout!)
file: SYJ/SYJ212+1.008.p (timeout!)
file: SYJ/SYJ212+1.009.p (timeout!)
file: SYJ/SYJ212+1.010.p (timeout!)
```

4.4 SYN Problems

```
file: SYN/SYN001+1.p (73 ms)
\overline{p,!(!(p)\multimap p\ \&\ !(p)\multimap p)\multimap \mathbf{0}:\ \cdot\vdash p}\quad \overline{p,!(!(p)\multimap p\ \&\ !(p)\multimap p)\multimap \mathbf{0}:\ \cdot\vdash p}
                      !(!(p)\multimap p \& !(p)\multimap p)\multimap \mathbf{0}: \cdot \vdash !(p)\multimap p \& !(p)\multimap p
                    \frac{(!(p) \multimap p \& !(p) \multimap p) \multimap \mathbf{0} : \ \cdot \vdash !(!(p) \multimap p \& !(p) \multimap p)}{!}!
                                                                                                                                                                    !(!(p)\multimap p \& !(p)\multimap p)\multimap \mathbf{0}: \mathbf{0}\vdash \mathbf{0}
                                                                  \frac{!(!(p) \multimap p \& !(p) \multimap p) \multimap \mathbf{0} : !(!(p) \multimap p \& !(p) \multimap p) \multimap \mathbf{0} \vdash \mathbf{0}}{!(!(p) \multimap p \& !(p) \multimap p) \multimap \mathbf{0} : \vdash \mathbf{0}} D_{C}
\frac{!(!(p) \multimap p \& !(p) \multimap p) \multimap \mathbf{0} : \vdash \mathbf{0}}{\cdot : \vdash !(!(!(p) \multimap p \& !(p) \multimap p) \multimap \mathbf{0}) \multimap \mathbf{0}} \star
 file: SYN/SYN040+1.p (timeout!)
 file: SYN/SYN041+1.p (timeout!)
 file: SYN/SYN044+1.p (845 ms)
 file: SYN/SYN045+1.p (501 ms)
 file: SYN/SYN046+1.p (timeout!)
 file: SYN/SYN047+1.p (timeout!)
 file: SYN/SYN387+1.p (fail)
19 file: SYN/SYN388+1.p (timeout!)
 file: SYN/SYN389+1.p (timeout!)
 file: SYN/SYN390+1.p (24 ms)
```

```
file: SYN/SYN392+1.p (timeout!)

file: SYN/SYN393+1.p (timeout!)

file: SYN/SYN416+1.p (fail)

20 file: SYN/SYN915+1.p (fail)

18 file: SYN/SYN916+1.p (fail)

21 file: SYN/SYN977+1.p (fail)

25 file: SYN/SYN978+1.p (31 ms)
```

$$\frac{a,b: \cdot \vdash b \quad a,b: \cdot \vdash a}{\cdot : \cdot \vdash !(a \& b) \multimap !(a) \multimap b \& !(b) \multimap a} \quad \star$$

5 Call-by-Value

5.1 KLE Problems

```
\frac{a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash a}{a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash !(a)} ! \frac{a,b,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash b}{a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash b}
                                                                           a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \vdash b
                              a, !(a) \multimap !(b), !(b) \multimap !(c) : \ !(a) \multimap !(b) \vdash b
                                                                                                                                                               a, c, !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash c
                                       a, !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash b
                                                                                                                                                            a, c, !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(c)
                                      a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash !(b)
                                                                                                                                                            a,!(a) \multimap !(b),!(b) \multimap !(c) : !(c) \vdash !(c)
                                                                                          a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \multimap !(c) \vdash !(c)
D_C
                                                                                                   a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash !(c)
                                                                                               !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(a) \multimap !(c)
                                                                                            \frac{1}{(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(!(a) \multimap !(c))} !
                                                                                        \cdot : !(!(a) \multimap !(b)), !(!(b) \multimap !(c)) \vdash !(!(a) \multimap !(c))
 file: KLE/KLE003+1.p (294 ms)
                                                                                                                                                      \overline{a,b,c,!(a)\multimap !(!(b)\multimap !(c)),!(b)\multimap !(c): \ \cdot \vdash c}
                                                                  \overline{a,b,!(a)\multimap !(!(b)\multimap !(c)),!(b)\multimap !(c): \ \cdot \vdash b}
                                                                                                                                                     \overline{a,b,c,!(a)\multimap !(!(b)\multimap !(c)),!(b)\multimap !(c): \ \cdot \vdash !(c)}
                                                                 \underline{a,b,!(a)} \multimap !(!(b) \multimap !(c)),!(b) \multimap !(c) : \cdot \vdash !(b)!
                                                                                                                                                    \overline{a, b, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \ !(c) \vdash !(c)}
                                                                                                    \overline{a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash a}
                                                                                                             a, b, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \cdot \vdash !(c)
\overline{a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(a)}
                                                                                                            a, b, !(a) \multimap !(!(b) \multimap !(c)) : !(!(b) \multimap !(c)) \vdash !(c)
                                               \frac{1}{a,b,!(a)} - 0!(!(b) - 0!(c)) : !(a) - 0!(!(b) - 0!(c)) \vdash !(c) \longrightarrow D_{C}
                                                                a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(c)
                                                            b,!(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(a) \multimap !(c)
                                                          \overline{b,!(a)\multimap!(!(b)\multimap!(c)): \cdot \vdash !(!(a)\multimap!(c))}
                                                      \frac{1}{(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(b) \multimap !(!(a) \multimap !(c))}
                                                    \frac{!(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(!(b) \multimap !(!(a) \multimap !(c)))}{!(a) \multimap !(b) \multimap !(c)}
                                                   \overline{\cdot : !(!(a) \multimap !(!(b) \multimap !(c))) \vdash !(!(b) \multimap !(!(a) \multimap !(c)))} 
 file: KLE/KLE004+1.p (272 ms)
                                                                                                                                                       \overline{a,b,c,!(a)\multimap !(!(b)\multimap !(c)),!(b)\multimap !(c): \cdot \vdash c}
                                                                  a, b, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \cdot \vdash b
                                                                                                                                                    a, b, c, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \cdot \vdash !(c)
                                                                 \frac{a, b, !(a) - \circ !(!(b) - \circ !(c)), !(b) - \circ !(c) : \cdot \vdash !(b)}{a, b, !(a) - \circ !(!(b) - \circ !(c)), !(b) - \circ !(c) : \cdot !(c) \vdash !(c)}
                                                                                                    a, b, !(a) \multimap !(!(b) \multimap !(c)), !(b) \multimap !(c) : \cdot \vdash !(c)
 \overline{a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash a}
                                                                                                            \overline{a, b, !(a) \multimap !(!(b) \multimap !(c)) : \ !(!(b) \multimap !(c)) \vdash !(c)}
\overline{a,b,!(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(a)}
                                               \frac{a, b, !(a) - \circ !(!(b) - \circ !(c)) : !(a) - \circ !(!(b) - \circ !(c)) \vdash !(c)}{D_{G}}
                                                                a, b, !(a) \multimap !(!(b) \multimap !(c)) : \cdot \vdash !(c)
                                                         \frac{}{!(a) \multimap !(!(b) \multimap !(c)) : \ \cdot \vdash !(a) \otimes !(b) \multimap !(c)} \ ^{\star}
                                                       \frac{!(a)\multimap !(!(b)\multimap !(c)): \cdot \vdash !(!(a)\otimes !(b)\multimap !(c))}{}
                                                      : !(!(a) \multimap !(!(b) \multimap !(c))) \vdash !(!(a) \otimes !(b) \multimap !(c)) 
file: KLE/KLE005+1.p (422 ms)
                                                                     \underbrace{a,b,!(a)\otimes!(b)}_{\bullet} - \circ !(c) : \cdot \vdash b
 a, b, !(a) \otimes !(b) \multimap !(c) : \cdot \vdash a
                                                                                                                                                           a, b, c, !(a) \otimes !(b) \multimap !(c) : \cdot \vdash c
                                                                            \overline{a,b,!(a)\otimes!(b)\multimap!(c):\ \cdot\vdash!(b)}
                                                                                                                                                           a, b, c, !(a) \otimes !(b) \multimap !(c) : \cdot \vdash !(c)
\overline{a,b,!(a)\otimes!(b)\multimap!(c):\cdot\vdash!(a)}
                                                                                                                                                          \overline{a, b, !(a) \otimes !(b) \multimap !(c) : \ !(c) \vdash !(c)}
                               a, b, !(a) \otimes !(b) \multimap !(c) : \cdot \vdash !(a) \otimes !(b)
                                                                              \overline{a,b,!(a)\otimes !(b)} \multimap !(c) : !(a)\otimes !(b) \multimap !(c) \vdash !(c)
                                                                                               a, b, !(a) \otimes !(b) \multimap !(c) : \cdot \vdash !(c)
                                                                                          a,!(a)\otimes !(b)\multimap !(c): \cdot \vdash !(b)\multimap !(c)
                                                                                        \frac{a,!(a)\otimes!(b)\multimap!(c): \cdot \vdash !(!(b)\multimap!(c))}{!}
                                                                                   \frac{!(a)\otimes !(b)\multimap !(c): \cdot \vdash !(a)\multimap !(!(b)\multimap !(c))}{!(a)\otimes !(b)\multimap !(c): \cdot \vdash !(a)\multimap !(c)}
                                                                               \frac{!(a) \otimes !(b) \multimap !(c) : \quad \vdash !(!(a) \multimap !(!(b) \multimap !(c)))}{!} !
                                                                             \frac{}{\cdot : !(!(a) \otimes !(b) \multimap !(c)) \vdash !(!(a) \multimap !(!(b) \multimap !(c)))}
```

```
file: KLE/KLE006+1.p (315 ms)
   \overline{a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash a}
                                                                                              \overline{a, b, !(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash b}
\frac{a,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash !(a)}{a,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash !(a)} \cdot \frac{a,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash b}{a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \vdash b}
                                      a,!(a) - 0.!(b),!(b) - 0.!(c) : !(a) - 0.!(b) \vdash b
D_C
                                                                                                                                                                                              \frac{\overline{a,c,!(a)\multimap !(b),!(b)\multimap !(c): \ \cdot \vdash c}}{a,c,!(a)\multimap !(b),!(b)\multimap !(c): \ \cdot \vdash !(c)}
                                               \frac{a,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash b}{a,!(a) \multimap !(b),!(b) \multimap !(c) : \vdash !(b)}
                                                                                                                                                                                             a, !(a) \multimap !(b), !(b) \multimap !(c) : !(c) \vdash !(c)
                                                                                                              a,!(a) \multimap !(b),!(b) \multimap !(c) : !(b) \multimap !(c) \vdash !(c)
D_C
                                                                                                                          a,!(a) \multimap !(b),!(b) \multimap !(c) : \cdot \vdash !(c)
                                                                                                                    \frac{!(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(a) \multimap !(c)}{!(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(a) \multimap !(c)}
                                                                                                                  \overline{!(a) \multimap !(b), !(b) \multimap !(c) : \cdot \vdash !(!(a) \multimap !(c))}
                                                                                                            \overline{!(a) \multimap !(b) : \cdot \vdash !(!(b) \multimap !(c)) \multimap !(!(a) \multimap !(c))}
                                                                                                         \frac{!(a) \multimap !(b) : \ \cdot \vdash !(!(!(b) \multimap !(c)) \multimap !(!(a) \multimap !(c)))}{!(a) \multimap !(b) : \ \cdot \vdash !(!(!(b) \multimap !(c)) \multimap !(!(a) \multimap !(c)))}
                                                                                                      \cdot : !(!(a) \multimap !(b)) \vdash !(!(!(b) \multimap !(c)) \multimap !(!(a) \multimap !(c)))
  file: KLE/KLE007+1.p (341 ms)
   c,!(a) \multimap !(b),!(c) \multimap !(a) : \cdot \vdash c
                                                                                             a, c, !(a) \multimap !(b), !(c) \multimap !(a) : \cdot \vdash a
\frac{1}{c,!(a) \multimap !(b),!(c) \multimap !(a): \ \cdot \vdash !(c)} \cdot \frac{1}{c,!(a) \multimap !(b),!(c) \multimap !(a): \ !(a) \vdash a}
                                      c,!(a) \multimap !(b),!(c) \multimap !(a) : !(c) \multimap !(a) \vdash a 
                                                                                                                                                                                                  \overline{b, c, !(a) \multimap !(b), !(c) \multimap !(a) : \cdot \vdash b}
                                               \frac{c,!(a) \multimap !(b),!(c) \multimap !(a) : \cdot \vdash a}{c,!(a) \multimap !(b),!(c) \multimap !(a) : \cdot \vdash !(a)}
                                                                                                                                                                                               \overline{b,c,!(a)\multimap!(b),!(c)\multimap!(a):\cdot\vdash!(b)}
                                                                                                                                                                                              c, !(a) \multimap !(b), !(c) \multimap !(a) : !(b) \vdash !(b)
                                                                                                              c, !(a) \multimap !(b), !(c) \multimap !(a) : !(a) \multimap !(b) \vdash !(b)
                                                                                                                          c, !(a) \multimap !(b), !(c) \multimap !(a) : \cdot \vdash !(b)
                                                                                                                     \frac{!(a)\multimap !(b),!(c)\multimap !(a): \cdot \vdash !(c)\multimap !(b)}{!}
                                                                                                                 \frac{1}{!(a) \multimap !(b), !(c) \multimap !(a) : \cdot \vdash !(!(c) \multimap !(b))} !
                                                                                                            \frac{!(a) \multimap !(b) : \cdot \vdash !(!(c) \multimap !(a)) \multimap !(!(c) \multimap !(b))}{} 
                                                                                                         \frac{!(a) \multimap !(b) : \ \cdot \vdash !(!(!(c) \multimap !(a)) \multimap !(!(c) \multimap !(b)))}{!(a) \multimap !(b) : \ \cdot \vdash !(!(!(c) \multimap !(a)) \multimap !(!(c) \multimap !(b)))}
                                                                                                       \cdot : !(!(a) \multimap !(b)) \vdash !(!(!(c) \multimap !(a)) \multimap !(!(c) \multimap !(b)))
  file: KLE/KLE008+1.p (266 ms)
\frac{a, c, !(a) \multimap !(b) : \cdot \vdash a}{a, c, !(a) \multimap !(b) : \cdot \vdash !(a)} ! \frac{a, b, c, !(a) \multimap !(b) : \cdot \vdash b}{a, c, !(a) \multimap !(b) : !(b) \vdash b} \star \frac{a, c, !(a) \multimap !(b) : !(a) \multimap !(b) \vdash b}{a, c, !(a) \multimap !(b) : \cdot \vdash b} D_{C}
\frac{a, c, !(a) \multimap !(b) : \cdot \vdash b}{a, c, !(a) \multimap !(b) : \cdot \vdash !(b)} !
                                                                                                                                                                                                  \frac{\overline{a,c,!(a)\multimap!(b):} \vdash c}{a,c,!(a)\multimap!(b):} \vdash c !
                                                                                                           a, c, !(a) \multimap \overline{!(b) : \cdot \vdash !(b) \otimes !(c)}
                                                                                             \frac{!(a) \multimap !(b) : \cdot \vdash !(a) \otimes !(c) \multimap !(b) \otimes !(c)}{!(a) \multimap !(b) : \cdot \vdash !(!(a) \otimes !(c) \multimap !(b) \otimes !(c))} *
```

file: KLE/KLE009+1.p (249 ms)

```
\frac{a, b, c, !(a) \multimap !(b) : \cdot \vdash c}{a, b, c, !(a) \multimap !(b) : \cdot \vdash !(c)} ! \frac{a, b, c, !(a) \multimap !(b) : \cdot \vdash b}{a, b, c, !(a) \multimap !(b) : \cdot \vdash !(b)} ! \\ \frac{a, b, c, !(a) \multimap !(b) : \cdot \vdash !(c) \otimes !(b)}{a, c, !(a) \multimap !(b) : \cdot \vdash !(c) \otimes !(b)} \star \\ \frac{a, b, c, !(a) \multimap !(b) : !(b) \vdash !(c) \otimes !(b)}{a, c, !(a) \multimap !(b) \vdash !(c) \otimes !(b)} - \bigcirc
 \frac{\overline{a, c, !(a) \multimap !(b) : \cdot \vdash a}}{a, c, !(a) \multimap !(b) : \cdot \vdash !(a)} !
                                                                              a, c, !(a) \multimap !(b) : !(a) \multimap !(b) \vdash !(c) \otimes !(b)
                                                                                                     a, c, !(a) \multimap !(b) : \cdot \vdash !(c) \otimes !(b)
                                                                   \frac{\frac{!(a) \multimap !(b) : \ \cdot \vdash !(c) \otimes !(a) \multimap !(c) \otimes !(b)}{!(a) \multimap !(b) : \ \cdot \vdash !(!(c) \otimes !(a) \multimap !(c) \otimes !(b))}}{!(a) \multimap !(b) : \ \cdot \vdash !(!(c) \otimes !(a) \multimap !(c) \otimes !(b))}}^{!} \star
     file: KLE/KLE010+1.p (272 ms)
\frac{a, b, !(a) \multimap !(b) : \cdot \vdash b}{a, b, !(a) \multimap !(b) : \cdot \vdash !(b)} !}{\frac{a, b, !(a) \multimap !(b) : \cdot \vdash !(b)}{a, b, !(a) \multimap !(b) : \cdot \vdash !(b)}}{\frac{a, b, !(a) \multimap !(b) : \cdot \vdash !(b) \oplus !(c)}{a, !(a) \multimap !(b) : !(b) \mapsto !(b) \oplus !(c)}} \underset{a, !(a) \multimap !(b) : \cdot \vdash !(b) \oplus !(c)}{\underbrace{a, !(a) \multimap !(b) : \cdot \vdash !(b) \oplus !(c)}} D_{C} \underbrace{\frac{c, !(a) \multimap !(b) : \cdot \vdash c}{c, !(a) \multimap !(b) : \cdot \vdash !(c)}}_{c, !(a) \multimap !(b) : \cdot \vdash !(b) \oplus !(c)} \underbrace{}_{c}
                                                                                                                                             !(a) \multimap !(b) : \cdot \vdash !(a) \oplus !(c) \multimap !(b) \oplus !(c)
                                                                                                                                         \frac{1}{(a) \multimap !(b) : \cdot \vdash !(!(a) \oplus !(c) \multimap !(b) \oplus !(c))} !
                                                                                                                                    \frac{1}{\cdot : !(!(a) \multimap !(b)) \vdash !(!(a) \oplus !(c) \multimap !(b) \oplus !(c))} \star
   file: KLE/KLE011+1.p (283 ms)
 \frac{\overline{a,b,!(a) \multimap !(b) : \cdot \vdash b}}{a,b,!(a) \multimap !(b) : \cdot \vdash l(b)} ! }{\frac{\overline{a,b,!(a) \multimap !(b) : \cdot \vdash l(b)}}{a,b,!(a) \multimap !(b) : \cdot \vdash !(b)} ! }{\frac{\overline{a,b,!(a) \multimap !(b) : \cdot \vdash !(b)}}{a,b,!(a) \multimap !(b) : \cdot \vdash !(b)} ! }{\frac{\overline{a,b,!(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)}}{a,b,!(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)}} * \\ \frac{\overline{c,!(a) \multimap !(b) : \cdot \vdash !(c)}}{c,!(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)} !}{\frac{\overline{a,!(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)}}{a,!(a) \multimap !(b) : \cdot \vdash !(c) \oplus !(b)}} D_C 
                                                                          \frac{!(a) \multimap !(b) : \ \cdot \vdash !(c) \oplus !(a) \multimap !(c) \oplus !(b)}{!(a) \multimap !(b) : \ \cdot \vdash !(!(c) \oplus !(a) \multimap !(c) \oplus !(b))} !
                                                                       \vdots !(!(a) \multimap !(b)) \vdash !(!(c) \oplus !(a) \multimap !(c) \oplus !(b))
```

file: KLE/KLE012+1.p (233 ms)

```
a,!(a) \multimap \mathbf{0}: \cdot \vdash a
\frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)}{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)} ! \frac{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash !(b)}{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash !(b)}
                                         a, !(a) \multimap \mathbf{0} : !(a) \multimap \mathbf{0} \vdash !(b)
                                                               a,!(a) \multimap \mathbf{0} : \cdot \vdash !(b)
                                                   !(a) \multimap \mathbf{0} : \cdot \vdash !(a) \multimap !(b)
                                            \frac{!(a) \multimap \mathbf{0} : \cdot \vdash !(!(a) \multimap !(b))}{!}
                                                       !(!(a) \multimap \mathbf{0}) \vdash !(!(a) \multimap !(b))
 file: KLE/KLE013+1.p (timeout!)
 file: KLE/KLE014+1.p (46 ms)
         \overline{a,b: \cdot \vdash !(b)}
     \overline{b: \cdot \vdash !(a) \multimap !(b)}
  \overline{{\color{red}b}: \ \cdot \vdash !(!(a) \multimap !(b))}
 \cdot : !(b) \vdash !(!(a) \multimap !(b))
 file: KLE/KLE015+1.p (timeout!)
 file: KLE/KLE016+1.p (298 ms)
                                                                         a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}), !(b) \multimap \mathbf{0} : \cdot \vdash b
                                                                       \overline{a,b,!(a) \multimap !(!(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : \ \cdot \vdash !(b)} \ ! \ \overline{a,b,!(a) \multimap !(!(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} : \ \mathbf{0} \vdash \mathbf{0}}
                                                                                                            a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}), !(b) \multimap \mathbf{0} : !(b) \multimap \mathbf{0} \vdash \mathbf{0}
D_C
                                                                                                                   a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}), !(b) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}
  a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}) : \vdash a
                                                                                                                   \overline{a,b,!(a)\multimap !(!(b)\multimap \mathbf{0}): \ !(!(b)\multimap \mathbf{0})\vdash \mathbf{0}}
a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}) : \cdot \vdash !(a)
                                                  \underbrace{a, b, !(a) \multimap !(!(\underline{b}) \multimap \mathbf{0}) : !(a) \multimap !(!(b) \multimap \mathbf{0}) \vdash \mathbf{0}}_{D_C}
                                                                   a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}) : \cdot \vdash \mathbf{0}
                                                               \overline{b,!(a)\multimap !(!(b)\multimap \mathbf{0}): \cdot \vdash !(a)\multimap \mathbf{0}}
                                                             \overline{b,!(a)} \rightarrow !(!(b) \rightarrow \mathbf{0}) : \cdot \vdash !(!(a) \rightarrow \mathbf{0})
                                                       \frac{!(a) \multimap !(!(b) \multimap \mathbf{0}) : \cdot \vdash !(b) \multimap !(!(a) \multimap \mathbf{0})}{!(a) \multimap !(!(b) \multimap \mathbf{0}) : \cdot \vdash !(b) \multimap !(!(a) \multimap \mathbf{0})}
                                                     \frac{!(a) \multimap !(!(b) \multimap \mathbf{0}) : \cdot \vdash !(!(b) \multimap !(!(a) \multimap \mathbf{0}))}{!(a) \multimap !(!(b) \multimap \mathbf{0}) : \cdot \vdash !(!(b) \multimap !(!(a) \multimap \mathbf{0}))}
                                                   \frac{}{\cdot : !(!(a) \multimap !(!(b) \multimap \mathbf{0})) \vdash !(!(b) \multimap !(!(a) \multimap \mathbf{0}))}
 file: KLE/KLE017+1.p (timeout!)
  file: KLE/KLE018+1.p (495 ms)
```

```
file: KLE/KLE019+1.p (384 ms)
                                                                                                                                                                                                                                                \overline{a,b,!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash a}
                                                                                 \overline{a, b, !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash b}
                                                                               \frac{a,b,!(a)\multimap!(b),!(b)\multimap!(a):}{\bullet} \cdot \vdash !(b)!
                                                                                                                                                                   \frac{\overline{b,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash b}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash !(b)}
  \overline{a,!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash a}
                                                                       ! \frac{1}{a,!(a) - o!(b),!(b) - o!(a) : !(b) \vdash !(b)}{a,!(a) - o!(b),!(b) - o!(a) : !(b) \vdash !(b)}
 a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)
                                a,!(a) \multimap !(b),!(b) \multimap !(a) : !(a) \multimap !(b) \vdash !(b)
D_C
                                         a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)
                                     \overline{!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(a)\multimap !(b)}
                                                                                                                                                                                                          !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(b) \multimap !(a)
                                                                                                                                                                                                       !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(b) \multimap !(a))
                                                                                                   !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a))
                                                                                                  : \ !(!(a) \multimap !(b)), !(!(b) \multimap !(a)) \vdash !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a))
  file: KLE/KLE020+1.p (265 ms)
                                                                                                                                                                   a, b, !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash b
\frac{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)} ! \frac{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash b}{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)} ! \frac{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)} *
                                                                a,!(a) \multimap !(b),!(b) \multimap !(a) : !(a) \multimap !(b) \vdash !(b)
                                                                    \frac{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)}{!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a) \multimap !(b)} \star \frac{!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a) \multimap !(b)}{!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(!(a) \multimap !(b))}!
                                                        \frac{}{\cdot : !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)) \vdash !(!(a) \multimap !(b))} 
  file: KLE/KLE021+1.p (256 ms)
\frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)} ! \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash a}}{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)} ! \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)}}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)} !
                                                               \frac{b,!(a) \multimap !(b),!(b) \multimap !(a) : !(b) \multimap !(a) \vdash !(a)}{b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)} D_C
                                                                    \frac{\frac{!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b) \multimap !(a)}{!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(!(b) \multimap !(a))}}{!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(!(b) \multimap !(a))} *
  file: KLE/KLE022+1.p (238 ms)
\frac{\overline{a,!(a) \multimap !(b),!(b) \multimap !(a) : \, \cdot \vdash a}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \, \cdot \vdash !(a)} \; ! \; \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \, \cdot \vdash b}}{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \, \cdot \vdash !(b)} \; ! \; \overline{a,!(a) \multimap !(b),!(b) \multimap !(a) : \, !(b) \vdash !(b)} \; \star
                                                               \frac{a,!(a) \multimap !(b),!(b) \multimap !(a) : !(a) \multimap !(b) \vdash !(b)}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)} D_{C}
\vdots !(a),!(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)) \vdash !(b)
```

file: KLE/KLE023+1.p (251 ms)

$$\frac{\frac{a,b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash a}{b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash a}!}{\frac{a,b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash a}{b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(a)}!}{\frac{a,b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(a)}{b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(a)}} \\ \frac{\frac{b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot !(b)\multimap !(a)\vdash !(a)}{b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(a)}}{\frac{b,!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(a)}{\cdot : \cdot !(b),!(!(a)\multimap !(b))\otimes !(!(b)\multimap !(a))\vdash !(a)}} D_{C}$$

file: KLE/KLE024+1.p (55 ms)

$$\frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a)} ! \qquad \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a)} ! \qquad \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a)} ! \qquad \times \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a)} ! \qquad \times \frac{\overline{a: \cdot \vdash a}}{\cdots \vdash !(a) \multimap !(a)} ! \qquad \times \frac{\overline{a: \cdot \vdash a}}{\cdots \vdash !(a) \multimap !(a)} ! \qquad \times \cdots \vdash !(!(a) \multimap !(a))} ! \qquad \otimes \cdots \vdash !(!(a) \multimap !(a)) \otimes !(!(a) \multimap !(a))$$

file: KLE/KLE025+1.p (370 ms)

```
\overline{a,b,!(a)} \multimap !(b),!(b) \multimap !(a) : \quad \vdash b
                                                                                                                                                                                  \overline{a,b,!(a)\multimap !(b),!(b)\multimap !(a): \ \cdot \vdash a}
                                                                                                                                                                             a, b, !(a) \multimap !(b), !(b) \multimap !(a) : \vdash !(a)!
                                                                                                                                                                                                                                                                                                                                                                              \frac{\overline{a,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash a}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash !(a)} \ ! \ \frac{\overline{a,b,!(a) \multimap !(b),!(b) \multimap !(a) : \ \cdot \vdash !(b)}}{a,!(a) \multimap !(b),!(b) \multimap !(a) : \ !(b) \vdash !(b)}
    \overline{b,!(a)\multimap!(b),!(b)\multimap!(a):\cdot\vdash b}
\frac{c_{1}, c_{2}, c_{3}, c_{4}, c_{5}, c_{5}
                                                                    b, \underbrace{!(a) \multimap !(b), !(b) \multimap !(a) : \ !(b) \multimap !(a) \vdash !(a)}_{D_C}
                                                                                                                                                                                                                                                                                                                                                                                                                                                     a,!(a) \multimap !(b),!(b) \multimap !(a) : !(a) \multimap !(b) \vdash !(b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        a,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(b)
                                                                                           b,!(a) \multimap !(b),!(b) \multimap !(a) : \cdot \vdash !(a)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \overline{!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(a)\multimap !(b)}
                                                                                  \overline{!(a)\multimap !(b),!(b)\multimap !(a): \cdot \vdash !(b)\multimap !(a)}
                                                                                                                                                                                                                                                                                                                                                                                                                                                               !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(a) \multimap !(b))
                                                                              !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(b) \multimap !(a))
                                                                                                                                                                                                                    !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(b) \multimap !(a)) \otimes !(!(a) \multimap !(b))
                                                                                                                                                                                                                   \overline{ \cdot : \ !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)) \vdash !(!(b) \multimap !(a)) \otimes !(!(a) \multimap !(b)) }
```

file: KLE/KLE026+1.p (798 ms)



file: KLE/KLE028+1.p (565 ms)

```
file: KLE/KLE029+1.p (1204 ms)
 file: KLE/KLE032+1.p (505 ms)
 file: KLE/KLE033+1.p (937 ms)
file: KLE/KLE034+1.p (371 ms)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  !(b) \multimap !(a) \vdash a
D_C
                                                                             \begin{array}{l} ((b),!(b) - \circ !(a) : \ !(a) - \circ !(b) \vdash b \\ a) - \circ !(b),!(b) - \circ !(a) : \ \cdot \vdash b \\ - \circ !(b),!(b) - \circ !(a) : \ \cdot \vdash !(b) \end{array} ! D_C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             \begin{array}{l} a, c, !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(b) \otimes !(c) \\ \hline !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(a) \otimes !(c) \multimap !(b) \otimes !(c) \\ \hline !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(a) \otimes !(c) \multimap !(b) \otimes !(c) \\ \hline !(a) \multimap !(b), !(b) \multimap !(a) : \cdot \vdash !(!(a) \otimes !(c) \multimap !(b) \otimes !(c) \\ \hline \end{array}
                                                                                                                                                                                                                                             \frac{!(a) \multimap !(b),!(b) \multimap !(a) : \, \vdash !(!(a) \otimes !(c) \multimap !(b) \otimes !(c)) \otimes !(!(b) \otimes !(c) \multimap !(a) \otimes !(c))}{\because : !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)) \vdash !(!(a) \otimes !(c) \multimap !(b) \otimes !(c)) \otimes !(!(b) \otimes !(c) \multimap !(a) \otimes !(c))} \\ \star \cdot \frac{!(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)) \vdash !(!(a) \otimes !(c) \multimap !(b) \otimes !(c)) \otimes !(!(b) \otimes !(c) \multimap !(a) \otimes !(c))}{}
  file: KLE/KLE035+1.p (381 ms)
                                                                                                                                                                                                                                            \vdots \quad \vdash !(c) \otimes !(b) \\ !(b) \vdash !(c) \otimes !(b)
                                                                                                                                                                                            \frac{!(a) \multimap !(b),!(b) \multimap !(a): \mapsto !(!(c) \otimes !(a) \multimap !(c) \otimes !(b)) \otimes !(!(c) \otimes !(b) \multimap !(c) \otimes !(a))}{\colon : !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)) \mapsto !(!(c) \otimes !(a) \multimap !(c) \otimes !(b)) \otimes !(!(c) \otimes !(b) \multimap !(c) \otimes !(a))} \xrightarrow{}
 file: KLE/KLE036+1.p (433 ms)
                                                                                                             !(a) \rightarrow !(b) \vdash !(b) \oplus !(c)
!(a) \rightarrow !(b) \vdash !(b) \oplus !(c)
!(a) \rightarrow !(b) \vdash !(b) \oplus !(c)
                                                                                                                                                                                                                                                   \frac{!(a) \multimap !(b),!(b) \multimap !(a) : \ \vdash !(!(a) \oplus !(c) \multimap !(b) \oplus !(c)) \otimes !(!(b) \oplus !(c) \multimap !(a) \oplus !(c))}{ \cdot : \ !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)) \vdash !(!(a) \oplus !(c) \multimap !(b) \oplus !(c)) \otimes !(!(b) \oplus !(c) \multimap !(a) \oplus !(c))} \ \star
```

file: KLE/KLE037+1.p (400 ms)

```
file: KLE/KLE038+1.p (1364 ms)
          file: KLE/KLE039+1.p (100 ms)
                                                                                         \begin{array}{c} \vdots \cdot \vdash a \\ \cdot \vdash !(a) \end{array} : \begin{array}{c} \overline{a,b,c} : \cdot \vdash \overline{b} \\ a,b,c : \cdot \vdash !(b) \end{array} \otimes \begin{array}{c} \overline{a,b,c} : \cdot \vdash \overline{b} \\ a,b,c : \cdot \vdash !(a) \otimes !(b) \end{array} \otimes \begin{array}{c} \overline{a,b,c} : \cdot \vdash \overline{c} \\ a,b,c : \cdot \vdash !(a) \otimes !(b) \otimes !(c) \end{array} \\ \\ \begin{array}{c} \overline{a,b,c} : \cdot \vdash !(a) \otimes !(b) \otimes !(c) \end{array} & \star \\ \hline \vdots \cdot \vdash !(a) \otimes !(b) \otimes !(c) - \circ !(a) \otimes !(b) \otimes !(c) \end{array} \\ \begin{array}{c} \vdots \cdot \vdash !(a) \otimes !(b) \otimes !(c) - \circ !(a) \otimes !(b) \otimes !(c) \end{array} \end{array} 
      \frac{\overline{a,b,c: \cdot \vdash a}}{a,b,c: \cdot \vdash !(a)} ! \frac{\overline{a,b,c: \cdot \vdash b}}{a,b,c: \cdot \vdash !(b)}
                                                                           a, b, c: \cdot \vdash !(a) \otimes !(b)
                                                                                                                                                                                                     \cdot : \cdot \vdash !(!(a) \otimes !(b) \otimes !(c) \multimap !(a) \otimes !(b) \otimes !(c)) \otimes !(!(a) \otimes !(b) \otimes !(c) \multimap !(a) \otimes !(b) \otimes !(c))
            file: KLE/KLE040+1.p (119 ms)
                                                                                                                                                         \begin{array}{c} \vdots \cdot \vdash !(a) \oplus !(b) \oplus !(c) - \circ !(a) \oplus !(b) \oplus !(c) \\ \vdots \cdot \vdash !(!(a) \oplus !(b) \oplus !(c) - \circ !(a) \oplus !(b) \oplus !(c)) \end{array} !
                                                                                                                                                                                                                                                                                                                                    \cdot : \ \cdot \vdash !(!(a) \oplus !(b) \oplus !(c) \multimap !(a) \oplus !(b) \oplus !(c)) \otimes !(!(a) \oplus !(b) \oplus !(c) \multimap !(a) \oplus !(b) \oplus !(c))
          file: KLE/KLE041+1.p (126 ms)
        \frac{\overline{a,b}: \cdot \vdash \overline{b}}{a,b: \cdot \vdash !(b)} ! \frac{\overline{a,b}: \cdot \vdash \overline{a}}{a,b: \cdot \vdash !(a)} ! \frac{\overline{a,b}: \cdot \vdash \overline{a}}{a,b: \cdot \vdash !(a)} ! \frac{\overline{a,b}: \cdot \vdash \overline{b}}{a,b: \cdot \vdash !(b)} ! \frac{\overline{a,b}: \cdot \vdash \overline{b}}{a,b: \cdot \vdash !(b)} ! \frac{\overline{a,b}: \cdot \vdash \overline{b}}{a,b: \cdot \vdash !(a)} ! \frac{\overline{a,b}: \cdot \vdash \overline{b}}{a,b: \cdot \vdash !(b)} ! \frac{\overline{a,b}: \cdot \vdash \overline{b,b}}{a,b: \cdot \vdash !(b)} ! \frac
                                                                               \cdot : \cdot \vdash !(!(a) \otimes !(b) \multimap !(b) \otimes !(a)) \otimes !(!(b) \otimes !(a) \multimap !(a) \otimes !(b))
        file: KLE/KLE042+1.p (134 ms)
\frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a)} \stackrel{!}{=} \frac{\overline{b: \cdot \vdash b}}{b: \cdot \vdash !(b) \oplus !(a)} \stackrel{!}{=} \frac{\overline{b: \cdot \vdash b}}{b: \cdot \vdash !(b) \oplus !(a)} \stackrel{!}{=} \frac{\overline{b: \cdot \vdash b}}{b: \cdot \vdash !(b) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(b)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !(a)} \stackrel{!}{=} \frac{\overline{a: \cdot \vdash a}}{a: \cdot \vdash !(a) \oplus !
                                                                                                                                                                                                       \cdot : \cdot \vdash !(!(a) \oplus !(b) \multimap !(b) \oplus !(a)) \otimes !(!(b) \oplus !(a) \multimap !(a) \oplus !(b))
```

file: KLE/KLE043+1.p (200 ms)

```
\frac{\overline{a,b:\vdash a}}{a,b:\vdash !(a)} \mid \frac{\overline{a,b:\vdash b}}{a,b:\vdash !(a)} \mid \frac{\overline{a,c:\vdash a}}{a,b:\vdash !(a)} \mid \frac{\overline{a,c:\vdash a}}{a,c:\vdash !(a)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(a)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,b:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(a)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(a)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(a)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,c:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(a)} \mid \frac{\overline{a,c:\vdash b}}{a,b:\vdash !(b)} \mid 
                 file: KLE/KLE044+1.p (231 ms)
                    file: KLE/KLE045+1.p (86 ms)
          \frac{\frac{a:\cdot\vdash a}{a:\cdot\vdash a}!}{\frac{a:\cdot\vdash a}{a:\cdot\vdash!(a)}!} \times \frac{\frac{\overline{a:\cdot\vdash a}}{a:\cdot\vdash!(a)}!}{\frac{a:\cdot\vdash!(a)\otimes!(a)\otimes!(a)}{a:\cdot\vdash!(a)\otimes!(a)}} \times \frac{\frac{\overline{a:\cdot\vdash a}}{a:\cdot\vdash!(a)\otimes!(a)}!}{\frac{a:\cdot\vdash!(a)\otimes!(a)\otimes!(a)}{\cdots\vdash!(a)\otimes!(a)\otimes!(a)}} \times \frac{\overline{a:\cdot\vdash a}}{\cdots\vdash!(a)\otimes!(a)\otimes!(a)} \times \frac{\overline{a:\cdot\vdash
                                                                                                                                                                 \cdot : \cdot \vdash !(!(a) \otimes !(a) \multimap !(a)) \otimes !(!(a) \multimap !(a) \otimes !(a))
                 file: KLE/KLE046+1.p (76 ms)
\frac{\overline{a:\cdot\vdash a}}{a:\cdot\vdash a} ! \frac{\overline{a:\cdot\vdash a}}{a:\cdot\vdash !(a)} ! \frac{\overline{a:\cdot\vdash a}}{a:\cdot\vdash !(a)} ! \frac{\overline{a:\cdot\vdash !(a)}}{a:\cdot\vdash !(a)} ! \frac{\overline{a:\cdot\vdash !(a)}}{a:\cdot\vdash !(a)\oplus !(a)} .
\frac{\cdot:\cdot\vdash !(a)\oplus !(a) - \cdot!(a)}{\cdot:\cdot\vdash !(!(a)\oplus !(a) - \cdot!(a))} ! \frac{\cdot:\cdot\vdash !(a) - \cdot!(a)\oplus !(a)}{\cdot:\cdot\vdash !(!(a) - \cdot!(a)\oplus !(a))} ! \frac{\cdot:\cdot\vdash !(!(a) - \cdot!(a)\oplus !(a))}{\cdot:\cdot\vdash !(!(a) - \cdot!(a)\oplus !(a))} .
```

file: KLE/KLE047+1.p (142 ms)

$$\frac{a: \cdot \vdash a}{a: \cdot \vdash (a)} : \frac{a, b: \cdot \vdash a}{a, b: \cdot \vdash (a)} : \frac{a: \cdot \vdash a}{a: \cdot \vdash (a)} : \frac{a: \cdot \vdash (a)}{a: \cdot \vdash (a)} :$$

file: KLE/KLE050+1.p (272 ms)

```
\frac{\overline{a,b:\cdot\vdash b}}{a,b:\cdot\vdash !(b)} \stackrel{!}{\underbrace{b,!(a)\multimap !(b):\cdot\vdash b}} \\ \frac{\overline{b,!(a)\multimap !(b):\cdot\vdash !(b)}}{b,!(a)\multimap !(b):\cdot\vdash !(b)} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \\ \frac{\overline{b:\cdot\vdash !(!(a)\multimap !(b))\multimap !(b)}}{b:\cdot\vdash !(!(a)\multimap !(b))\multimap !(b)} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \\ \frac{\overline{b:\cdot\vdash !(!(!(a)\multimap !(b))\multimap !(b))}}{\underbrace{b:\cdot\vdash !(!(b)\multimap !(!(a)\multimap !(b)))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(b)\multimap !(!(a)\multimap !(b)))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(!(a)\multimap !(b))\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b)))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(!(a)\multimap !(b))\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b)))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b)))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b)))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b)))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \\ \stackrel{!}{\underbrace{b:\cdot\vdash !(!(a)\multimap !(b))}} \stackrel{!}{\underbrace{b:\cdot\vdash !(b)}} 
                               : !(b) \vdash !(!(!(a) \multimap !(b)) \multimap !(b)) \otimes !(!(b) \multimap !(!(a) \multimap !(b)))
     file: KLE/KLE051+1.p (294 ms)
         a,!(a) \multimap \mathbf{0},!(a) \multimap !(b) : \cdot \vdash a
                                                                                                                                                                                                                                                                                                                                                                                                   a,!(a) \multimap \mathbf{0} : \cdot \vdash a
   a,!(a) \multimap 0,!(a) \multimap !(b) : \vdash !(a) ! a,!(a) \multimap 0,!(a) \multimap !(b) : 0 \vdash 0
                                                                                                                                                                                                                                                                                                                                                                                              a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)! a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash !(b)
                                                                             \frac{a,!(a) \multimap 0,!(a) \multimap !(b) : !(a) \multimap 0 \vdash 0}{2} D_C
                                                                                                                                                                                                                                                                                                                                                                                                                                          a,!(a) \stackrel{\frown}{\sim} \mathbf{0} : !(a) \stackrel{\frown}{\sim} \mathbf{0} \vdash !(b) D_C
                                                                                                 a,!(a) \multimap \mathbf{0},!(a) \multimap !(b) : \cdot \vdash \mathbf{0}
                                                                                                                                                                                                                                                                                                                                                                                                                                                             a,!(a) \multimap \mathbf{0} : \cdot \vdash !(b)
                                                                                       \frac{!(a) \multimap \mathbf{0}, !(a) \multimap !(b) : \cdot \vdash !(a) \multimap \mathbf{0}}{!(a) \multimap \mathbf{0}, !(a) \multimap !(b) : \cdot \vdash !(a) \multimap \mathbf{0}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                  !(a) \multimap \mathbf{0} : \cdot \vdash !(a) \multimap !(b)
                                                                                \frac{!(a) \multimap \mathbf{0}, !(a) \multimap !(b) : \cdot \vdash !(!(a) \multimap \mathbf{0})}{!}
                                                                                                                                                                                                                                                                                                                                                                                                                                           \frac{!(a) \multimap \mathbf{0} : \vdash !(!(a) \multimap !(b))}{!}
                                                                                                                                                                                                                                                                                                                                                                                                      \overline{!(a)\multimap \mathbf{0}: \ \cdot \vdash !(!(a)\multimap \mathbf{0})\multimap !(!(a)\multimap !(b))}
                                                                    \frac{!(a) \multimap \mathbf{0} : \cdot \vdash !(!(a) \multimap !(b)) \multimap !(!(a) \multimap \mathbf{0})}{!(a) \multimap \mathbf{0} : \cdot \vdash !(!(a) \multimap !(b)) \multimap !(!(a) \multimap \mathbf{0})}
                                                              \frac{!(a) \multimap \mathbf{0} : \cdot \vdash !(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap \mathbf{0}))}{!(a) \multimap \mathbf{0} : \cdot \vdash !(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap \mathbf{0}))}
                                                                                                                                                                                                                                                                                                                                                                                               !(a) \multimap \mathbf{0} : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap !(!(a) \multimap !(b)))
                                                                                                                                          !(a) \multimap \mathbf{0} : \vdash !(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap \mathbf{0})) \otimes !(!(!(a) \multimap \mathbf{0}) \multimap !(!(a) \multimap !(b)))
                                                                                                                                  \frac{\phantom{a}}{\cdot : \ !(!(a) \multimap \mathbf{0}) \vdash !(!(!(a) \multimap !(b)) \multimap !(!(a) \multimap \mathbf{0})) \otimes !(!(!(a) \multimap \mathbf{0}) \multimap !(!(a) \multimap !(b)))}
       file: KLE/KLE052+1.p (398 ms)
```

file: KLE/KLE053+1.p (89 ms)

$$\frac{a,b: \cdot \vdash a}{a,b: \cdot \vdash (a)} ! \frac{\overline{a,b: \cdot \vdash a}}{a,b: \cdot \vdash (a)} ! \frac{\overline{a,b: \cdot \vdash b}}{a,b: \cdot \vdash (b)} ! \frac{1}{a,b: \cdot \vdash (b)} ! \frac{\overline{a,b: \cdot \vdash b}}{a,b: \cdot \vdash (b)} ! \frac{1}{a,b: \cdot \vdash (b)} ! \frac{\overline{a,b: \cdot \vdash (b)}}{a,b: \cdot \vdash (b)} ! \frac{1}{a,b: \cdot \vdash (b)} ! \frac{\overline{a,b: \cdot \vdash (b)}}{b: \cdot \vdash (a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (a) \otimes !(b) - o!(a) \otimes !(b)}}{b: \cdot \vdash (a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (a) \otimes !(b) - o!(a) \otimes !(b)}}{b: \cdot \vdash (a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (a) \otimes !(b) - o!(a) \otimes !(b)}}{b: \cdot \vdash (a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash b}}{b: \cdot \vdash !(b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash !(b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash !(b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash !(b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash !(b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash !(b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash !(b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b) - o!(a) \otimes !(b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b)}} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash (b)} ! \frac{\overline{b: \cdot \vdash (b)}}{b: \cdot \vdash$$

file: KLE/KLE056+1.p (285 ms)

```
\frac{\overline{b,!(b)}\multimap \mathbf{0}: \ \cdot \vdash \overline{b}}{b,!(b)\multimap \mathbf{0}: \ \cdot \vdash !(b)} \ ! \ \overline{b,!(b)\multimap \mathbf{0}: \ \mathbf{0}\vdash !(a)} \ \star \\ - \circ
                                             \frac{b,!(b) \multimap \mathbf{0} : \ !(b) \multimap \mathbf{0} \vdash !(a)}{b,!(b) \multimap \mathbf{0} : \ \vdash !(a)} \ b
 a,!(b) \multimap \mathbf{0} : \cdot \vdash a
a,!(b) \multimap \mathbf{0} : \cdot \vdash !(a)!
                                                                                                                                        \frac{!(b)\multimap \mathbf{0}: \cdot \vdash !(a)\multimap !(a)\oplus !(b)}{}
                    \frac{!(b) \multimap \mathbf{0} : \cdot \vdash !(a) \oplus !(b) \multimap !(a)}{!(b) \multimap \mathbf{0} : \cdot \vdash !(!(a) \oplus !(b) \multimap !(a))}
                                                         !(b) \multimap \mathbf{0} : \cdot \vdash !(!(a) \oplus !(b) \multimap !(a)) \otimes !(!(a) \multimap !(a) \oplus !(b))
                                                       \frac{}{\cdot : \ !(!(b) \multimap \mathbf{0}) \vdash !(!(a) \oplus !(b) \multimap !(a)) \otimes !(!(a) \multimap !(a) \oplus !(b))} 
file: KLE/KLE057+1.p (105 ms)
     a,!(a) \multimap \mathbf{0} : \cdot \vdash a
\overline{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)} \quad ! \quad \overline{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash \mathbf{0}}
                                    a, !(a) \multimap \mathbf{0} : !(a) \multimap \mathbf{0} \vdash \mathbf{0}
                                                     a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}
                                          \underline{a}: \overline{\cdot \vdash !(!(a) \multimap \mathbf{0}) \multimap \mathbf{0}} 
                                      \underline{a}: \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0}) !
                        \cdot : \overline{\cdot \vdash !(a) \multimap !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})} 
                   \underline{\cdot : \cdot \vdash \underline{!(!(a) \multimap !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0}))}} !
 file: KLE/KLE058+1.p (588 ms)
 file: KLE/KLE059+1.p (385 ms)
 file: KLE/KLE060+1.p (412 ms)
```

```
file: KLE/KLE061+1.p (73 ms)
   a,!(a) \multimap \mathbf{0} : \cdot \vdash a
\overline{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)} \quad ! \quad \overline{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash \mathbf{0}}
                       \overline{a,!(a) \multimap \mathbf{0}} : !(a) \multimap \mathbf{0} \vdash \mathbf{0}
                                  a,!(a) \multimap \mathbf{0} : \cdot \vdash \overline{\mathbf{0}}
                     \overline{\cdot : \cdot \vdash !(a) \otimes !(!(a) \multimap \mathbf{0}) \multimap \mathbf{0}} 
                 \overline{\cdot : \cdot \vdash !(!(a) \otimes !(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})} !
 file: KLE/KLE062+1.p (546 ms)
 file: KLE/KLE063+1.p (346 ms)
```

file: KLE/KLE064+1.p (300 ms)

```
a,!(!(a) \multimap !(a)) \multimap \mathbf{0},!(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0} : \vdash a
       a,!(!(a) \multimap !(a)) \multimap \mathbf{0},!(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(a)
                                                              \frac{!(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0}}{!}
                                                                                                                                                                                                                                                  \frac{1}{!(!(!(!(a)\multimap !(a))\multimap 0)\multimap 0)\multimap 0: 0\vdash 0}
                                                           \frac{1(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0} : \vdash !(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0})}{(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0})}
                                                                                                                           \frac{!(!(!(!(a) \multimap !(a)) \multimap 0) \multimap 0)}{!(!(!(!(a) \multimap !(a)) \multimap 0) \multimap 0) \multimap 0} \cdots \underbrace{!(!(!(!(a) \multimap !(a)) \multimap 0) \multimap 0) \multimap 0}_{D_{G}}
                                                                                                                                                     : \quad \cdot \overline{\vdash !(!(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0})} \quad \star
                                                                                                                                                  : \cdot \vdash !(!(!(!(!(!(a) \multimap !(a)) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0})
  file: KLE/KLE065+1.p (232 ms)
        \frac{\overline{a,b: \cdot \vdash a}}{a,b: \cdot \vdash !(a)} ! \frac{a,!(b) \multimap \mathbf{0}: \cdot \vdash a}{a,!(b) \multimap \mathbf{0}: \cdot \vdash !(a)} !
           \cdot : \cdot \vdash !(a) \otimes !(b) \oplus !(!(b) \multimap \mathbf{0}) \multimap !(a)
                                               !(!(a) \otimes \overline{!(b) \oplus !(!(b) \multimap \mathbf{0}) \multimap !(a))}
  file: KLE/KLE066+1.p (152 ms)
                                               b,!(b) \multimap \mathbf{0} : \cdot \vdash b
          \frac{b,!(b) \multimap 0 : \cdot \vdash b}{b,!(b) \multimap 0 : \cdot \vdash !(b)} ! \frac{b,!(b) \multimap 0 : 0 \vdash !(a)}{b,!(b) \multimap 0 : 0 \vdash !(a)} \star \\ \frac{\vdots \cdot \vdash a}{\cdot \vdash !(a)} ! \frac{b,!(b) \multimap 0 : !(b) \multimap 0 \vdash !(a)}{b,!(b) \multimap 0 : \cdot \vdash !(a)} D_C
\frac{\cdot : \cdot \vdash !(a) \oplus !(b) \otimes !(!(b) \multimap 0) \multimap !(a)}{\cdot : \cdot \vdash !(!(a) \oplus !(b) \otimes !(!(b) \multimap 0) \multimap !(a)} !
\frac{\cdot : \cdot \vdash !(!(a) \oplus !(b) \otimes !(!(b) \multimap 0) \multimap !(a)}{\cdot : \cdot \vdash !(!(a) \oplus !(b) \otimes !(b) \otimes !(b) \otimes !(b) \multimap 0)} \star
\frac{\cdot : \cdot \vdash !(!(a) \oplus !(b) \otimes !(b) \otimes !(b) \otimes !(b) \otimes !(b) \multimap 0)}{\cdot : \cdot \vdash !(!(a) \multimap !(a) \oplus !(b) \otimes !(b) \multimap 0)}
 a: \vdash a!
                                                 \cdot: \cdot \vdash !(!(a) \oplus !(b) \otimes !(!(b) \multimap \mathbf{0}) \multimap !(a)) \otimes !(!(a) \multimap !(a) \oplus !(b) \otimes !(!(b) \multimap \mathbf{0}))
  file: KLE/KLE067+1.p (146 ms)
   a, b, !(b) \multimap \mathbf{0} : \cdot \vdash b
                                                                                                                                                                  b,!(b) \multimap \mathbf{0} : \cdot \vdash b
\frac{a,b,!(b)\multimap 0: \vdash b}{\underbrace{a,b,!(b)\multimap 0: \vdash !(b)}} ! \frac{a,b,!(b)\multimap 0: 0\vdash !(b)\otimes !(!(b)\multimap 0)}{\underbrace{a,b,!(b)\multimap 0: 1(b)\otimes !(!(b)\multimap 0)}} \star \underbrace{\frac{b,!(b)\multimap 0: \vdash !(b)}{b,!(b)\multimap 0: \vdash !(b)}} ! \frac{b,!(b)\multimap 0: 0\vdash !(a)\otimes !(b)\otimes !(!(b)\multimap 0)}{\underbrace{b,!(b)\multimap 0: \vdash !(a)\otimes !(b)\otimes !(!(b)\multimap 0)}} D_C
                                                                                                                                                                           b,!(b) \rightarrow \mathbf{0} : \cdot \vdash !(a) \otimes !(b) \otimes !(!(b) \rightarrow \mathbf{0})
                           a, b, !(b) \multimap \mathbf{0} : \cdot \vdash !(b) \otimes !(!(b) \multimap \mathbf{0})
           \cdot : \cdot \vdash !(!(a) \otimes !(b) \otimes !(!(b) \multimap \mathbf{0}) \multimap !(b) \otimes !(!(b) \multimap \mathbf{0})) \otimes !(!(b) \otimes !(!(b) \multimap \mathbf{0}) \multimap !(a) \otimes !(b) \otimes !(!(b) \multimap \mathbf{0}))
 file: KLE/KLE068+1.p (fail)
 46 file: KLE/KLE069+1.p (timeout!)
  file: KLE/KLE070+1.p (327 ms)
```

```
file: KLE/KLE071+1.p (104 ms)
                          \frac{a,b,!(a)\oplus !(!(b)\multimap \mathbf{0})\multimap \mathbf{0}: \cdot \vdash a}{a,b,!(a)\oplus !(!(b)\multimap \mathbf{0})\multimap \mathbf{0}: \cdot \vdash !(a)} !
\frac{a,b,!(a)\oplus !(!(b)\multimap \mathbf{0})\multimap \mathbf{0}: \cdot \vdash !(a)\oplus !(!(b)\multimap \mathbf{0})}{a,b,!(a)\oplus !(!(b)\multimap \mathbf{0})}\oplus_{1} \frac{a,b,!(a)\oplus !(!(b)\multimap \mathbf{0})\multimap \mathbf{0}: \mathbf{0}\vdash \mathbf{0}}
                                                                      a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} \vdash \mathbf{0}
D_C
                                                                                                    \frac{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}{a, b : \cdot \vdash !(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0}} \star
                                                                        \frac{a,b: \cdot \vdash !(!(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0})}{\cdot : \cdot \vdash !(!(a) \otimes !(b) \multimap !(!(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0})} \cdot \\ \cdot : \cdot \vdash !(!(a) \otimes !(b) \multimap !(!(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0})} \\ \cdot : \cdot \vdash !(!(a) \otimes !(b) \multimap !(!(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap \mathbf{0}))} \cdot !
   file: KLE/KLE072+1.p (327 ms)
   file: KLE/KLE073+1.p (285 ms)
```

```
file: KLE/KLE074+1.p (timeout!)
  file: KLE/KLE075+1.p (timeout!)
  file: KLE/KLE076+1.p (408 ms)
 file: KLE/KLE077+1.p (225 ms)
\frac{\overline{a,!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash a}}{a,!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash !(a)} ! \atop \overline{a,!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash !(a) \oplus !(b)} \oplus_{1} \frac{\overline{a,!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash !(b)}}{a,!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash !(b)} \star_{-\mathbf{0}}
                                               a, !(\underline{a}) \oplus !(\underline{b}) \multimap \mathbf{0} : !(\underline{a}) \oplus !(\underline{b}) \multimap \mathbf{0} \vdash !(\underline{b}) D_C
                                                                          a,!(a)\oplus !(b)\multimap \mathbf{0}: \cdot \vdash !(b)
                                                            \frac{\frac{!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash !(a) \multimap !(b)}{!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash !(!(a) \multimap !(b))} *}{!(a) \oplus !(b) \multimap \mathbf{0} : \cdot \vdash !(!(a) \multimap !(b))}!
                                             \frac{\vdots \cdot \vdash !(!(a) \oplus !(b) \multimap \mathbf{0}) \multimap !(!(a) \multimap !(b))}{\cdot \vdots \cdot \vdash !(!(!(a) \oplus !(b) \multimap \mathbf{0}) \multimap !(!(a) \multimap !(b)))} *
  file: KLE/KLE078+1.p (timeout!)
  file: KLE/KLE079+1.p (359 ms)
```

file: KLE/KLE080+1.p (109 ms)

```
a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}), !(b) \multimap \mathbf{0} : \vdash b
                                                                                                              \frac{}{a,b,!(a) \multimap !(!(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} \colon \cdot \vdash !(b)} \; ! \quad \frac{}{a,b,!(a) \multimap !(!(b) \multimap \mathbf{0}),!(b) \multimap \mathbf{0} \colon \mathbf{0} \vdash \mathbf{0}} 
                                                                                                                                                                      a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}), !(b) \multimap \mathbf{0} : !(b) \multimap \mathbf{0} \vdash \mathbf{0}
                                                                                                                                                                               \frac{a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}), !(b) \multimap \mathbf{0} : \vdash \mathbf{0}}{a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}) : !(!(b) \multimap \mathbf{0}) \vdash \mathbf{0}}
  a, b, !(a) \multimap !(!(b) \multimap \mathbf{0}) : \cdot \vdash a
\overline{a,b,!(a)\multimap !(!(b)\multimap \mathbf{0}): \cdot \vdash !(a)}
                                                                        \begin{array}{c} a,b,!(a) \multimap !(!(b) \multimap \\ \hline a,b,!(a) \multimap !(!(b) \multimap 0) : \ !(a) \multimap !(!(b) \multimap 0) \vdash 0 \\ \hline \frac{a,b,!(a) \multimap !(!(b) \multimap 0) : \ \vdash 0}{a,b: \vdash !(!(a) \multimap !(!(b) \multimap 0)) \multimap 0} \\ \hline \frac{a,b: \vdash !(!(a) \multimap !(!(b) \multimap 0)) \multimap 0}{a,b: \vdash !(!(!(a) \multimap !(!(b) \multimap 0)) \multimap 0)} ! \\ \hline \vdots \vdash \vdash !(a) \otimes !(b) \multimap !(!(!(a) \multimap !(!(b) \multimap 0)) \multimap 0)} \\ \hline \vdots \vdash \vdash !(!(a) \otimes !(b) \multimap !(!(!(a) \multimap !(!(b) \multimap 0)) \multimap 0)) \\ \hline \end{array} 
 file: KLE/KLE081+1.p (330 ms)
 file: KLE/KLE082+1.p (456 ms)
 file: KLE/KLE083+1.p (timeout!)
 file: KLE/KLE084+1.p (timeout!)
 file: KLE/KLE085+1.p (timeout!)
 file: KLE/KLE086+1.p (timeout!)
 file: KLE/KLE087+1.p (234 ms)
```

```
\frac{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash a}{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(a)} !
\frac{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(a) \oplus !(!(b) \multimap \mathbf{0})}{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} \vdash \mathbf{0}} \underbrace{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}_{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash \mathbf{1}} D_{C}
\frac{a, b, !(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(a) \otimes !(b) \multimap \mathbf{0}}{!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(a) \otimes !(b) \multimap \mathbf{0}} \underbrace{\dagger}_{!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0} : \cdot \vdash !(!(a) \otimes !(b) \multimap \mathbf{0})}_{!(a) \oplus !(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0}) \multimap !(!(a) \otimes !(b) \multimap \mathbf{0})} \underbrace{\dagger}_{!(a) \oplus !(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0})}_{!(a) \oplus !(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0})} \underbrace{\dagger}_{!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0}}_{!(a) \oplus !(!(a) \otimes !(b) \multimap \mathbf{0})} \underbrace{\dagger}_{!(a) \oplus !(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0})}_{!(a) \oplus !(b) \multimap \mathbf{0})} \underbrace{\dagger}_{!(a) \oplus !(!(a) \oplus !(!(b) \multimap \mathbf{0}) \multimap \mathbf{0})}_{!(a) \oplus !(b) \multimap \mathbf{0})}_{!(a) \oplus !(b) \multimap \mathbf{0})}
```

file: KLE/KLE088+1.p (timeout!)

5.2 LCL Problems

file: LCL/LCL181+1.p (timeout!)
file: LCL/LCL230+1.p (timeout!)

5.3 SYJ Problems

file: SYJ/SYJ101+1.p (30 ms)

$$\frac{\frac{a: \cdot \vdash a}{a: \cdot \vdash !(a)}!}{\vdots !(a) \vdash !(a)},$$

file: SYJ/SYJ102+1.p (79 ms)

$$\frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash a}{\underbrace{a,!(a) \multimap \mathbf{0} : \cdot \vdash !(a)}} \stackrel{!}{\underbrace{a,!(a) \multimap \mathbf{0} : \mathbf{0} \vdash \mathbf{0}}} \stackrel{\star}{\underbrace{a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}} \stackrel{\star}{\underbrace{a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}} D_C$$

$$\frac{a,!(a) \multimap \mathbf{0} : \cdot \vdash \mathbf{0}}{\underbrace{a: \cdot \vdash !(!(a) \multimap \mathbf{0}) \multimap \mathbf{0}}} \stackrel{\star}{\underbrace{a: \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{!}{\underbrace{a: \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}} \stackrel{\star}{\underbrace{\cdot : \cdot \vdash !(!(!(a) \multimap \mathbf{0}) \multimap \mathbf{0})}}$$

file: SYJ/SYJ104+1.p (249 ms)

```
a, b, !(a) \multimap !(b) : \cdot \vdash b
\frac{\overline{a,!(a) \multimap !(b) : \cdot \vdash a}}{a,!(a) \multimap !(b) : \cdot \vdash !(a)} ! \frac{\overline{a,b,!(a) \multimap !(b) : \cdot \vdash !(b)}}{a,!(a) \multimap !(b) : !(b) \vdash !(b)} *
                                       a,!(a) \multimap !(b) : \underline{!(a) \multimap !(b) \vdash !(b)}
                                                           a, \overline{!(a) \multimap !(b) : \cdot \vdash !(b)}
                                                 \frac{}{!(a)\multimap !(b): \cdot \vdash !(a)\multimap !(b)} \quad \star
                                            \frac{!(a) \multimap !(b) : \cdot \vdash !(!(a) \multimap !(b))}{!}
                                        \frac{\phantom{a}}{\cdot : \ !(!(a) \multimap !(b)) \vdash !(!(a) \multimap !(b))} \quad \star
  file: SYJ/SYJ105+1.002.p (324 ms)
  file: SYJ/SYJ105+1.003.p (timeout!)
  file: SYJ/SYJ105+1.004.p (timeout!)
  file: SYJ/SYJ106+1.p (1858 ms)
 file: SYJ/SYJ107+1.001.p (95 ms)
\frac{\overline{b,c: \cdot \vdash b}}{\underbrace{b,c: \cdot \vdash !(b)}} ! \underbrace{\frac{\overline{b,c: \cdot \vdash c}}{b,c: \cdot \vdash !(c)}}_{b,c: \cdot \vdash !(b) \otimes !(c)} ! \underbrace{\frac{\overline{a,c: \cdot \vdash a}}{a,c: \cdot \vdash !(a)}}_{a,c: \cdot \vdash !(a) \oplus !(b) \otimes !(c)} ! \underbrace{\frac{\overline{b,c: \cdot \vdash b}}{b,c: \cdot \vdash !(b)}}_{b,c: \cdot \vdash !(b) \otimes !(c)} ! \underbrace{\frac{\overline{b,c: \cdot \vdash c}}{b,c: \cdot \vdash !(b)}}_{b,c: \cdot \vdash !(b) \otimes !(c)} ! \underbrace{\frac{\overline{b,c: \cdot \vdash c}}{b,c: \cdot \vdash !(b) \otimes !(c)}}_{b,c: \cdot \vdash !(a) \oplus !(b) \otimes !(c)} !
                                                            \cdot : !(c), !(b) \oplus !(a) \oplus !(b) \vdash !(a) \oplus !(b) \otimes !(c)
```

file: SYJ/SYJ107+1.002.p (374 ms)

```
file: SYJ/SYJ107+1.004.p (timeout!)
file: SYJ/SYJ201+1.002.p (timeout!)
file: SYJ/SYJ201+1.003.p (timeout!)
file: SYJ/SYJ201+1.004.p (timeout!)
file: SYJ/SYJ201+1.005.p (timeout!)
file: SYJ/SYJ201+1.006.p (timeout!)
file: SYJ/SYJ201+1.007.p (timeout!)
file: SYJ/SYJ201+1.008.p (timeout!)
 file: SYJ/SYJ201+1.009.p (timeout!)
file: SYJ/SYJ201+1.010.p (timeout!)
file: SYJ/SYJ201+1.011.p (timeout!)
file: SYJ/SYJ201+1.012.p (timeout!)
 file: SYJ/SYJ201+1.013.p (timeout!)
file: SYJ/SYJ201+1.014.p (timeout!)
file: SYJ/SYJ201+1.015.p (timeout!)
file: SYJ/SYJ201+1.016.p (timeout!)
 file: SYJ/SYJ201+1.017.p (timeout!)
file: SYJ/SYJ201+1.018.p (timeout!)
file: SYJ/SYJ201+1.019.p (timeout!)
file: SYJ/SYJ201+1.020.p (timeout!)
 file: SYJ/SYJ202+1.001.p (38 ms)
        o11, o21 : \cdot \vdash o11
      o11, o21 : \cdot \vdash !(o11)

\overbrace{o11, o21 : \cdot \vdash !(o11) \oplus !(o21)}^{\bullet 1} \oplus_{1}

\cdot : !(o11), !(o21) \vdash !(o11) \oplus !(o21)
file: SYJ/SYJ202+1.002.p (367 ms)
file: SYJ/SYJ202+1.003.p (timeout!)
file: SYJ/SYJ202+1.004.p (timeout!)
file: SYJ/SYJ202+1.005.p (timeout!)
file: SYJ/SYJ202+1.006.p (timeout!)
file: SYJ/SYJ202+1.007.p (timeout!)
 file: SYJ/SYJ202+1.008.p (timeout!)
file: SYJ/SYJ202+1.009.p (timeout!)
```

```
file: SYJ/SYJ202+1.010.p (timeout!)
  file: SYJ/SYJ202+1.011.p (timeout!)
 file: SYJ/SYJ202+1.012.p (timeout!)
 file: SYJ/SYJ202+1.013.p (timeout!)
  file: SYJ/SYJ202+1.014.p (timeout!)
  file: SYJ/SYJ202+1.015.p (timeout!)
  file: SYJ/SYJ202+1.016.p (timeout!)
  file: SYJ/SYJ202+1.017.p (timeout!)
  file: SYJ/SYJ202+1.018.p (timeout!)
  file: SYJ/SYJ202+1.019.p (timeout!)
 file: SYJ/SYJ202+1.020.p (timeout!)
 file: SYJ/SYJ203+1.001.p (307 ms)
\frac{p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash p_1}{p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash p_1}!}{p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash !(p_1)}! \oplus i_1 \frac{\overline{f},p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash \overline{f}}{f,p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash !(f)}}! \star \underbrace{\frac{\overline{f},p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash \overline{f}}{f,p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash !(f)}}_{p_1,!(p_1)\oplus !(p_1)\multimap !(f): \, \, \vdash !(f)}}! \star \underbrace{\frac{\overline{f},p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash \overline{f}}{f,p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash !(f)}}}_{p_1,!(p_1)\oplus !(!(p_1)\multimap !(f))\multimap !(f): \, \, \vdash !(f)}}
                                   \frac{p_1, !(p_1) \oplus !(!(p_1) \multimap !(f)) \multimap !(f) : \ !(p_1) \oplus !(!(p_1) \multimap !(f)) \multimap !(f) \vdash !(f)}{p_1, p_2, p_3, p_4, p_5, p_6} D_C
                                                             p1,!(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) : \cdot \vdash !(f)
                                                         \frac{1}{!(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) : \ \vdash !(p1) \multimap !(f)} \ \star
                                                                                                                                                                                                                 \overline{f,!(p1)\oplus !(!(p1)\multimap !(f))\multimap !(f):\ \cdot \vdash f}
                                                       \frac{1}{(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) : \cdot \vdash !(!(p1) \multimap !(f))} !
                                                                                                                                                                                                               \overline{f,!(p1)\oplus!(!(p1)\multimap!(f))\multimap!(f):\;\cdot\vdash!(f)}
                                                \underbrace{!(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) : \ \cdot \vdash !(p1) \oplus !(!(p1) \boxdot \circ !(f))}_{} \oplus_{1}
                                                                                                                                                                                                              !(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) : !(f) \vdash !(f)
                                                                                                         \frac{!(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) : \ !(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) \vdash !(f)}{\underline{!(p1) \oplus !(!(p1) \multimap !(f)) \multimap !(f) : \ \vdash !(f)}} \ D_{C}
                                                                                                                               file: SYJ/SYJ203+1.002.p (1997 ms)
 file: SYJ/SYJ203+1.003.p (18495 ms)
  file: SYJ/SYJ203+1.004.p (timeout!)
 file: SYJ/SYJ203+1.005.p (timeout!)
 file: SYJ/SYJ203+1.006.p (timeout!)
  file: SYJ/SYJ203+1.007.p (timeout!)
  file: SYJ/SYJ203+1.008.p (timeout!)
```

```
file: SYJ/SYJ203+1.009.p (timeout!)
  file: SYJ/SYJ203+1.010.p (timeout!)
  file: SYJ/SYJ203+1.011.p (timeout!)
  file: SYJ/SYJ203+1.012.p (timeout!)
  file: SYJ/SYJ203+1.013.p (timeout!)
  file: SYJ/SYJ203+1.014.p (timeout!)
  file: SYJ/SYJ203+1.015.p (timeout!)
   file: SYJ/SYJ203+1.016.p (timeout!)
  file: SYJ/SYJ203+1.017.p (timeout!)
  file: SYJ/SYJ203+1.018.p (timeout!)
  file: SYJ/SYJ203+1.019.p (timeout!)
   file: SYJ/SYJ203+1.020.p (timeout!)
   file: SYJ/SYJ204+1.001.p (107 ms)
                                                                                                                                                                                                                                                                             \overline{p0, p1, !(p1) \multimap !(p0), !(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash p0}
                                                                                                                                                                                                                                                                         p0, p1, !(p1) - (p0), !(p1) - !(p1) - !(p0)) : \cdot \vdash !(p0)
                                                                                                                    p1, !(p1) \multimap !(p0), !(p1) \multimap !(!(p1) \multimap !(p0)) : \ \cdot \vdash p1
                                                                                                                                                                                                                                                                        p1, !(p\overline{1}) \multimap !(p0), !(p\overline{1}) \multimap !(!(p\overline{1}) \multimap !(p0)) : \ !(p0) \vdash !(p0)
                                                                                                                  \overline{p_1,!(p_1) \multimap !(p_0),!(p_1) \multimap !(!(p_1) \multimap !(p_0)) : \cdot \vdash !(p_1)}
                                                                                                                                                                                   \begin{array}{c} \circ !(!(p1) - \circ !(p0)) \cdot ! - !(p1) - \circ !
  p1,!(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash p1
                                                                                                                                                                                                   p1,!(p1) \multimap !(p0),!(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash !(p0)
                                                                                                                                                                                                 \overline{p1,!(p1) \multimap !(!(p1) \multimap !(p0)) : \ !(!(p1) \multimap !(p0)) \vdash !(p0)} \ \star
\overline{p1,!(p1) \multimap !(!(p1) \multimap !(p0)) : \cdot \vdash !(p1)}
                                                                                     \frac{1}{p1,!(p1)} \circ !(!(p1) \circ !(p0)) : \ !(p1) \circ !(p1) \circ !(p0)) \vdash !(p0)}{p1,!(p1) \circ !(p1) \circ !(p1)} D_C
                                                                                                                    p1,!(p1) \multimap !(!(p1) \multimap !(p0)) : \ \cdot \vdash !(p0)
                                                                                                               \frac{}{\cdot : \ !(p1), !(!(p1) \multimap !(!(p1) \multimap !(p0))) \vdash !(p0)} 
  file: SYJ/SYJ204+1.002.p (573 ms)
  file: SYJ/SYJ204+1.003.p (2568 ms)
  file: SYJ/SYJ204+1.004.p (13079 ms)
   file: SYJ/SYJ204+1.006.p (timeout!)
   file: SYJ/SYJ204+1.007.p (timeout!)
  file: SYJ/SYJ204+1.008.p (timeout!)
   file: SYJ/SYJ204+1.009.p (timeout!)
   file: SYJ/SYJ204+1.010.p (timeout!)
   file: SYJ/SYJ204+1.011.p (timeout!)
  file: SYJ/SYJ204+1.012.p (timeout!)
  file: SYJ/SYJ204+1.013.p (timeout!)
   file: SYJ/SYJ204+1.014.p (timeout!)
```

file: SYJ/SYJ204+1.015.p (timeout!) file: SYJ/SYJ204+1.016.p (timeout!) file: SYJ/SYJ204+1.017.p (timeout!) file: SYJ/SYJ204+1.018.p (timeout!) file: SYJ/SYJ204+1.019.p (timeout!) file: SYJ/SYJ204+1.020.p (timeout!) file: SYJ/SYJ205+1.001.p (35352 ms) file: SYJ/SYJ205+1.002.p (107317 ms) file: SYJ/SYJ205+1.003.p (timeout!) file: SYJ/SYJ205+1.004.p (timeout!) file: SYJ/SYJ205+1.005.p (timeout!) file: SYJ/SYJ205+1.006.p (timeout!) file: SYJ/SYJ205+1.007.p (timeout!) file: SYJ/SYJ205+1.008.p (timeout!) file: SYJ/SYJ205+1.009.p (timeout!) file: SYJ/SYJ205+1.010.p (timeout!) file: SYJ/SYJ205+1.011.p (timeout!) file: SYJ/SYJ205+1.012.p (timeout!) file: SYJ/SYJ205+1.013.p (timeout!) file: SYJ/SYJ205+1.014.p (timeout!) file: SYJ/SYJ205+1.015.p (timeout!) file: SYJ/SYJ205+1.016.p (timeout!) file: SYJ/SYJ205+1.017.p (timeout!) file: SYJ/SYJ205+1.018.p (timeout!) file: SYJ/SYJ205+1.019.p (timeout!)

file: SYJ/SYJ205+1.020.p (timeout!)
file: SYJ/SYJ206+1.001.p (47 ms)

```
\frac{\overline{a1: \cdot \vdash a1}}{a1: \cdot \vdash !(a1)} ! \frac{\overline{a1: \cdot \vdash a1}}{a1: \cdot \vdash !(a1)} ! \frac{\overline{a1: \cdot \vdash a1}}{a1: \cdot \vdash !(a1)} ! \frac{\cdot : \cdot \vdash !(a1)}{\cdot : \cdot \vdash !(!(a1) \multimap !(a1))} *
           \cdot: \cdot \vdash !(!(a1) \multimap !(a1)) \otimes !(!(a1) \multimap !(a1))
file: SYJ/SYJ206+1.002.p (502 ms)
 file: SYJ/SYJ206+1.003.p (23407 ms)
 file: SYJ/SYJ206+1.004.p (timeout!)
 file: SYJ/SYJ206+1.005.p (timeout!)
 file: SYJ/SYJ206+1.006.p (timeout!)
 file: SYJ/SYJ206+1.007.p (timeout!)
 file: SYJ/SYJ206+1.008.p (timeout!)
 file: SYJ/SYJ206+1.009.p (timeout!)
 file: SYJ/SYJ206+1.010.p (timeout!)
 file: SYJ/SYJ206+1.011.p (timeout!)
 file: SYJ/SYJ206+1.012.p (timeout!)
 file: SYJ/SYJ206+1.013.p (timeout!)
 file: SYJ/SYJ206+1.014.p (timeout!)
 file: SYJ/SYJ206+1.015.p (timeout!)
 file: SYJ/SYJ206+1.016.p (timeout!)
file: SYJ/SYJ206+1.017.p (timeout!)
 file: SYJ/SYJ206+1.018.p (timeout!)
file: SYJ/SYJ207+1.001.p (timeout!)
 file: SYJ/SYJ207+1.002.p (timeout!)
 file: SYJ/SYJ207+1.003.p (timeout!)
 file: SYJ/SYJ207+1.004.p (timeout!)
 file: SYJ/SYJ207+1.005.p (timeout!)
 file: SYJ/SYJ207+1.006.p (timeout!)
```

- file: SYJ/SYJ207+1.007.p (timeout!)
- file: SYJ/SYJ207+1.008.p (timeout!)
- file: SYJ/SYJ207+1.009.p (timeout!)
- file: SYJ/SYJ207+1.010.p (timeout!)
- file: SYJ/SYJ207+1.011.p (timeout!)
- file: SYJ/SYJ207+1.012.p (timeout!)
- file: SYJ/SYJ207+1.013.p (timeout!)
- file: SYJ/SYJ207+1.014.p (timeout!)
- file: SYJ/SYJ207+1.015.p (timeout!)
- file: SYJ/SYJ207+1.016.p (timeout!)
- file: SYJ/SYJ207+1.017.p (timeout!)
- file: SYJ/SYJ207+1.018.p (timeout!)
- file: SYJ/SYJ207+1.019.p (timeout!)
- file: SYJ/SYJ207+1.020.p (timeout!)
- file: SYJ/SYJ208+1.001.p (timeout!)
- file: SYJ/SYJ208+1.002.p (timeout!)
- file: SYJ/SYJ208+1.003.p (timeout!)
- file: SYJ/SYJ208+1.004.p (timeout!)
- file: SYJ/SYJ208+1.005.p (timeout!)
- file: SYJ/SYJ208+1.006.p (timeout!)
 file: SYJ/SYJ208+1.007.p (timeout!)
- file: SYJ/SYJ208+1.008.p (timeout!)
- file: SYJ/SYJ208+1.009.p (timeout!)
- file: SYJ/SYJ208+1.010.p (timeout!)
- file: SYJ/SYJ208+1.011.p (timeout!)
- file: SYJ/SYJ208+1.012.p (timeout!)
- file: SYJ/SYJ208+1.013.p (timeout!)
- file: SYJ/SYJ208+1.014.p (timeout!)
- file: SYJ/SYJ208+1.015.p (timeout!)
- file: SYJ/SYJ208+1.016.p (timeout!)
- file: SYJ/SYJ208+1.017.p (timeout!)
- file: SYJ/SYJ208+1.018.p (timeout!)
- file: SYJ/SYJ208+1.019.p (timeout!)
- file: SYJ/SYJ209+1.001.p (timeout!)
- file: SYJ/SYJ209+1.002.p (timeout!)

- file: SYJ/SYJ209+1.003.p (timeout!)
- file: SYJ/SYJ209+1.004.p (timeout!)
- file: SYJ/SYJ209+1.005.p (timeout!)
- file: SYJ/SYJ209+1.006.p (timeout!)
- file: SYJ/SYJ209+1.007.p (timeout!)
- file: SYJ/SYJ209+1.008.p (timeout!)
- file: SYJ/SYJ209+1.009.p (timeout!)
- file: SYJ/SYJ209+1.010.p (timeout!)
- file: SYJ/SYJ209+1.011.p (timeout!)
- file: SYJ/SYJ209+1.012.p (timeout!)
- file: SYJ/SYJ209+1.013.p (timeout!)
- file: SYJ/SYJ209+1.014.p (timeout!)
- file: SYJ/SYJ209+1.015.p (timeout!)
- file: SYJ/SYJ209+1.016.p (timeout!)
- file: SYJ/SYJ209+1.017.p (timeout!)
- file: SYJ/SYJ209+1.018.p (timeout!)
- file: SYJ/SYJ209+1.019.p (timeout!)
- file: SYJ/SYJ209+1.020.p (timeout!)
- file: SYJ/SYJ210+1.001.p (timeout!)
- file: SYJ/SYJ210+1.002.p (timeout!)
- file: SYJ/SYJ210+1.003.p (timeout!)
- file: SYJ/SYJ210+1.004.p (timeout!)
- file: SYJ/SYJ210+1.005.p (timeout!)
- file: SYJ/SYJ210+1.006.p (timeout!)
- file: SYJ/SYJ210+1.007.p (timeout!)
- file: SYJ/SYJ210+1.008.p (timeout!)
- file: SYJ/SYJ210+1.009.p (timeout!)
- file: SYJ/SYJ210+1.010.p (timeout!)
- file: SYJ/SYJ210+1.011.p (timeout!)
- file: SYJ/SYJ210+1.012.p (timeout!)
- file: SYJ/SYJ210+1.013.p (timeout!)
- file: SYJ/SYJ210+1.014.p (timeout!)
- file: SYJ/SYJ210+1.015.p (timeout!)
- file: SYJ/SYJ210+1.016.p (timeout!)
- file: SYJ/SYJ210+1.017.p (timeout!)
- file: SYJ/SYJ210+1.018.p (timeout!)

file: SYJ/SYJ210+1.019.p (timeout!) file: SYJ/SYJ210+1.020.p (timeout!) file: SYJ/SYJ211+1.001.p (timeout!) file: SYJ/SYJ211+1.002.p (timeout!) file: SYJ/SYJ211+1.003.p (timeout!) file: SYJ/SYJ211+1.004.p (timeout!) file: SYJ/SYJ211+1.005.p (timeout!) file: SYJ/SYJ211+1.006.p (timeout!) file: SYJ/SYJ211+1.007.p (timeout!) file: SYJ/SYJ211+1.008.p (timeout!) file: SYJ/SYJ211+1.009.p (timeout!) file: SYJ/SYJ211+1.010.p (timeout!) file: SYJ/SYJ211+1.011.p (timeout!) file: SYJ/SYJ211+1.012.p (timeout!) file: SYJ/SYJ211+1.013.p (timeout!) file: SYJ/SYJ211+1.014.p (timeout!) file: SYJ/SYJ211+1.015.p (timeout!) file: SYJ/SYJ211+1.016.p (timeout!) file: SYJ/SYJ211+1.017.p (timeout!) file: SYJ/SYJ211+1.018.p (timeout!) file: SYJ/SYJ211+1.019.p (timeout!) file: SYJ/SYJ211+1.020.p (timeout!) file: SYJ/SYJ212+1.001.p (553 ms) Section 1 Section 1 Section 2 Sectio file: SYJ/SYJ212+1.002.p (timeout!) file: SYJ/SYJ212+1.003.p (timeout!) file: SYJ/SYJ212+1.004.p (timeout!) file: SYJ/SYJ212+1.005.p (timeout!) file: SYJ/SYJ212+1.006.p (timeout!) file: SYJ/SYJ212+1.007.p (timeout!) file: SYJ/SYJ212+1.008.p (timeout!)

file: SYJ/SYJ212+1.009.p (timeout!)
file: SYJ/SYJ212+1.010.p (timeout!)

SYN Problems

```
file: SYN/SYN001+1.p (274 ms)
                \overline{p,!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap \mathbf{0}: \cdot \vdash p}
                                                                                                                                                                                                                                    p,!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap \mathbf{0}: \cdot \vdash p
                                                                                                                                                                                                                        \frac{p,!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap \mathbf{0}: \ \cdot \vdash !(p)}{!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap \mathbf{0}: \ \cdot \vdash !(p)\multimap !(p)}
   \frac{p,!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap 0: \cdot \vdash !(p)}{!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap 0: \cdot \vdash !(p)\multimap !(p)}
\frac{!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap 0: \; \cdot \vdash !(!(p)\multimap !(p))}{!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap 0: \; \cdot \vdash !(!(p)\multimap !(p))}
                                                                                                                                                                                                                                                                                                                                                                                                                                          \boxed{!(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap \mathbf{0}:\ \mathbf{0}\vdash \mathbf{0}}
                                                                           !(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))\multimap \mathbf{0}: \ \cdot \vdash !(!(p)\multimap !(p))\otimes !(!(p)\multimap !(p))
                                                                                                                                                                                              \frac{!(!(p) \multimap !(p)) \otimes !(!(p) \multimap !(p)) \multimap 0 : !(!(p) \multimap !(p)) \otimes !(!(p) \multimap !(p)) \multimap 0 \vdash 0}{!(!(p) \multimap !(p)) \otimes !(!(p) \multimap !(p)) \multimap 0 : \vdash 0} \wedge \sum_{i=1}^{k} D_{C}
                                                                                                                                                                                                                                            file: SYN/SYN040+1.p (timeout!)
   file: SYN/SYN041+1.p (timeout!)
   file: SYN/SYN044+1.p (769 ms)
   file: SYN/SYN045+1.p (229 ms)
                                                     \vdots \cdot \vdash !(!(p) \oplus !(q) \otimes !(r) - \circ !(p) \oplus !(q) \otimes !(p) \oplus !(r)) \quad \vdots \quad \vdash !(!(p) \oplus !(q) \otimes !(r) - \circ !(p) \oplus !(q) \otimes !(p) \oplus !(p) \otimes !(p) \oplus !(q) \otimes !(p) \oplus !(p) \oplus !(p) \oplus !(p) \otimes !(p) \otimes
 file: SYN/SYN046+1.p (timeout!)
   file: SYN/SYN047+1.p (timeout!)
  file: SYN/SYN387+1.p (fail)
18 | file: SYN/SYN388+1.p (timeout!)
 file: SYN/SYN389+1.p (timeout!)
   file: SYN/SYN390+1.p (46 ms)
                                                                       p: \cdot \vdash p
                                                                                                                                                                                                                                                                                                                                                                                        p: \cdot \vdash p
                                                    \overline{p: \cdot \vdash !(p)}!
               \frac{\cdot : \overline{\cdot \vdash !(p) \multimap !(p)}}{\cdot \cdot \cdot \vdash !(p) \multimap !(p)} \star
          \frac{\overline{\cdot : \cdot \vdash !(p) \multimap !(p)}}{: \cdot \vdash !(!(p) \multimap !(p))} * \frac{\overline{\cdot : \cdot \vdash !(p) \multimap !(p)}}{\cdot : \cdot \vdash !(!(p) \multimap !(p))}
                                                   \cdot : \cdot \vdash !(!(p) \multimap !(p)) \otimes !(!(p) \multimap !(p)) 
 file: SYN/SYN391+1.p (454 ms)
```

```
file: SYN/SYN392+1.p (timeout!)
file: SYN/SYN393+1.p (timeout!)
 file: SYN/SYN416+1.p (fail)
18 file: SYN/SYN915+1.p (17 ms)
file: SYN/SYN916+1.p (fail)
     file: SYN/SYN977+1.p (fail)
33 | file: SYN/SYN978+1.p (93 ms)
   \frac{\overline{a,b:\cdot\vdash b}}{a,b:\cdot\vdash!(b)} \stackrel{!}{\underbrace{a,b:\cdot\vdash a}} = \frac{\overline{a,b:\cdot\vdash a}}{a,b:\cdot\vdash!(a)} \stackrel{!}{\underbrace{a,b:\cdot\vdash!(a)}} \stackrel{!}{\underbrace{a,b:\cdot\vdash!(a)}} \stackrel{!}{\underbrace{a,b:\cdot\vdash!(b)\multimap!(a)}} \star \\ \frac{\overline{a,b:\cdot\vdash!(a)\multimap!(b)}}{a,b:\cdot\vdash!(!(a)\multimap!(b))} \stackrel{!}{\underbrace{a,b:\cdot\vdash!(b)\multimap!(a)}} \star
                     a, b: \cdot \vdash !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a))
    \overline{\cdot : \cdot \vdash !(a) \otimes !(b) \multimap !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a))} 
\overline{\cdot : \cdot \vdash !(!(a) \otimes !(b) \multimap !(!(a) \multimap !(b)) \otimes !(!(b) \multimap !(a)))}
```

References

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- [2] Chuck Liang & Dale Miller (2009): Focusing and polarization in linear, intuitionistic, and classical logics. Theor. Comput. Sci. 410(46), pp. 4747–4768, doi:10.1016/j.tcs.2009.07.041.