


# Aggregate Uncertainty and Discrete Choice

Computations and Quantitative Models in Macro

Carlos Rojas Quiroz

January 2023

# Aggregate Uncertainty and Discrete Choice

- ▶ I solved both questions in `Matlab`.
- ▶ Some details about the code and algorithms are described in the `README.md` file of each question (in my online repository). See them for more information.
- ▶ Questions 2 and 3 from the homework were joined in just one (Q2 in these slides).
- ▶ Codes of this homework can be found here: 
- ▶ Also, I've updated the results of model *a la* Aiyagari from homework 1 (see the new PDF file [here](#)).

# Aggregate Uncertainty: Krusell-Smith Algorithm

# Q1: Aggregate uncertainty: Krusell-Smith algorithm

## Questions

### 1. Use the Krusell-Smith algorithm to solve for the ALM

The estimated parameters of the ALM are the following:

- \* low-idiosyncratic productivity shock:  $\log(K_{t+1}) = 0.1491 + 0.9087 \log(K_t)$
- \* high-idiosyncratic productivity shock:  $\log(K_{t+1}) = 0.1556 + 0.9071 \log(K_t)$

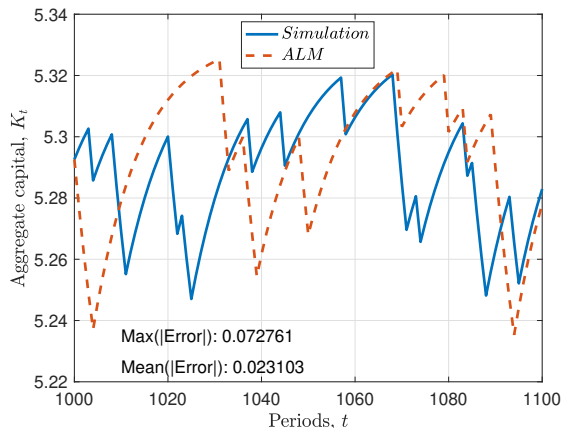
### 2. Calculate the $R^2$ of the ALM

- \* low-idiosyncratic productivity shock:  $R^2 = 0.999998803434357$
- \* high-idiosyncratic productivity shock:  $R^2 = 0.999998802891821$

# Q1: Aggregate uncertainty: Krusell-Smith algorithm

## Questions

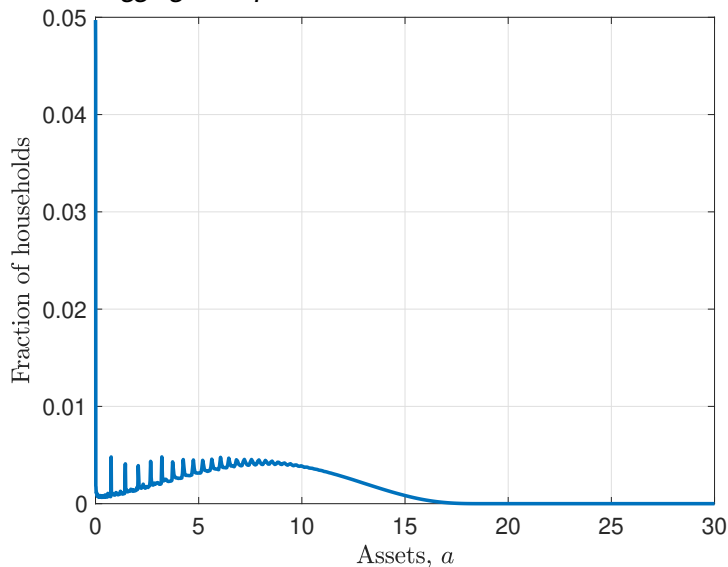
3. Calculate the DenHaan measure using the existing time series from period 1000-1100
- In the next figure, I plot both series of aggregate capital (non-stochastic simulation and ALM forecasting) and point out the maximum and average distance between both series.



# Q1: Aggregate uncertainty: Krusell-Smith algorithm

## Questions

### 4.1 Plot the distribution of aggregate capital

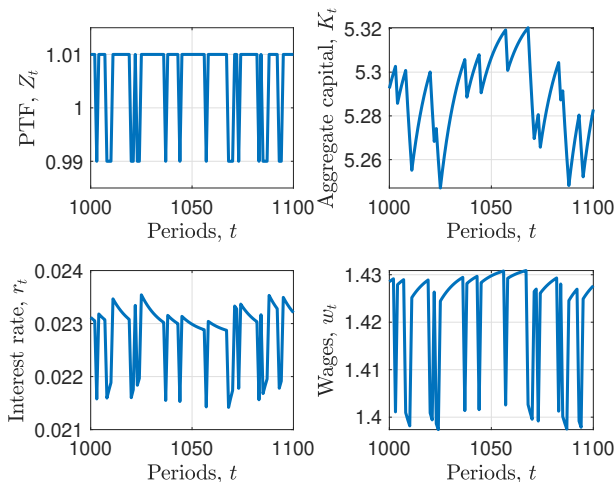


# Q1: Aggregate uncertainty: Krusell-Smith algorithm

## Questions

### 4.2 Plot the timeseries of aggregate capital, interest rate, wages and TFP

In order to ease the visualization, I plot these timeseries only for the period 1000-1100 (as in the DenHaan's test).



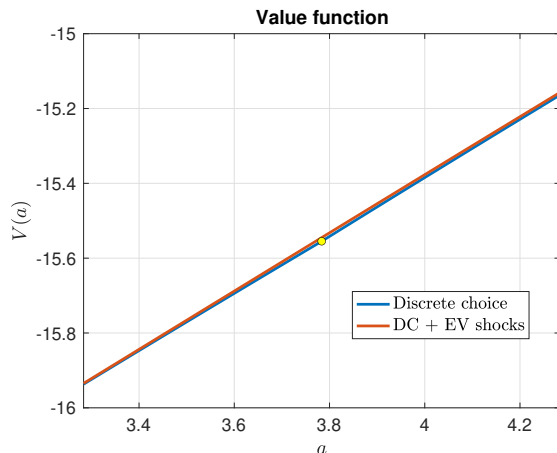
# **SIM with Discrete Choice - Adding Extreme Value Taste shocks**



## Q2: SIM with Discrete Choice and EV shocks

### Questions

#### 1.1 Plot the value function

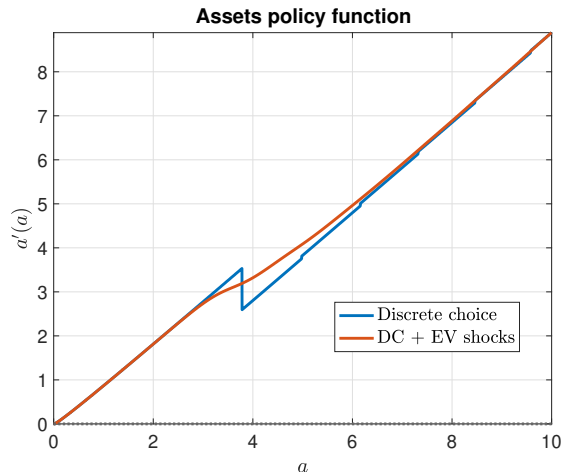


- ▶ I show value functions of the standard model with discrete choice (Discrete choice) and with extreme value shocks (DC + EV shocks).
- ▶ I graph both functions around the point where the value function changes (the round marker, although the difference in the curve's shape is not noticeable).
- ▶ At that point consumer decides to go out from the labor market.
- ▶ Adding extreme value shocks allows to “smooth” the value function.

## Q2: SIM with Discrete Choice and EV shocks

### Questions

#### 1.2 Plot the policy function for assets

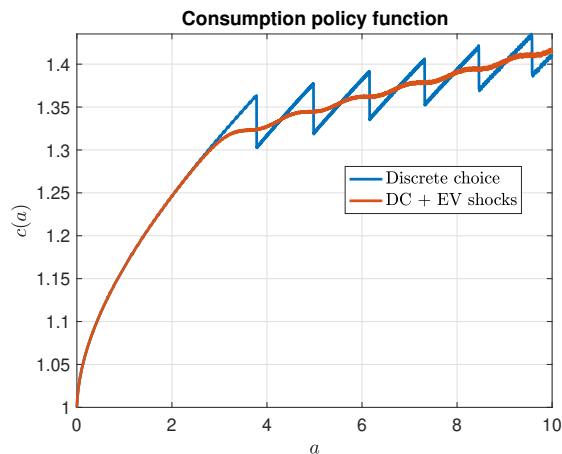


- ▶ In the standard model with discrete choice, we observe a sort of “regime change” at the point where the consumer decides not working. That point is  $a = 3.7835$ .
- ▶ If consumers don't supply labor, then they save less in order to finance consumption.
- ▶ Adding extreme value shocks makes the optimal choice of assets for the next period be smooth between both “regimes”.

## Q2: SIM with Discrete Choice and EV shocks

### Questions

#### 1.3 Plot the policy function for consumption

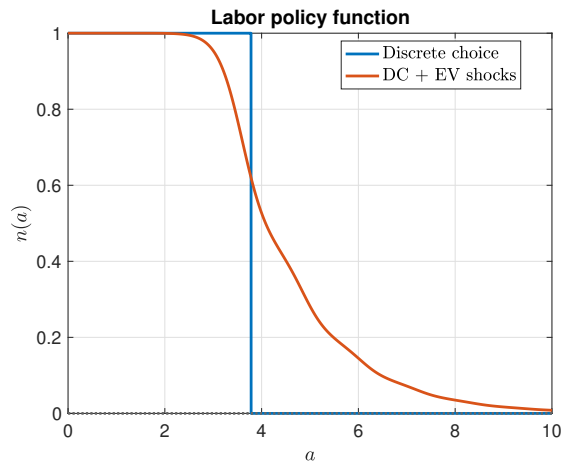


- ▶ In the standard model with discrete choice, we observe a change in its behavior for assets  $a > 3.7835$  (not work), with ups and downs around a increasing trend.
- ▶ Consumption and assets policy functions are non-monotonic in assets and have discontinuities given by the participation in the labor market and the consumption smoothing behavior.
- ▶ As before, including extreme value shocks makes consumption policy function be smooth after that point.

## Q2: SIM with Discrete Choice and EV shocks

### Questions

#### 1.4 Plot the policy function for labor



- ▶ The policy function for labor is totally different between both models. In the standard discrete choice model we observe a drastic change before (work) and after (not work) of  $a = 3.7835$ .
- ▶ The presence of extreme value shocks makes to obtain probabilities for the values in the assets grid instead of a discrete “regime change”.

## Q2: SIM with Discrete Choice and EV shocks

### Questions

2. Could you use EGM for either of the problems? Why / why not?

No, we can't. For implementing the EGM we should obtain, as a first step, the FOC from the (recursive) consumer's problem:

$$V(a, n, z) = \max_{a', n} U(nwz + (1+r)a - a') - \phi n + \beta \mathbb{E} V'(a', n', z')$$

The FOC is:

$$U_{a'}(\cdot) = \beta \mathbb{E} V'_{a'}(\cdot)$$

For a log utility form:

$$nwz + (1+r)a - a' = \left( \beta \mathbb{E} V'_{a'}(\cdot) \right)^{-\frac{1}{\sigma}}$$

## Q2: SIM with Discrete Choice and EV shocks

### Questions

2. Could you use EGM for either of the problems? Why / why not? (...continued)

The EGM implies that:

$$\alpha = \left[ \frac{1}{1+r} \right] \left\{ \left( \beta \mathbb{E} V'_{\alpha'}(\cdot) \right)^{-\frac{1}{\sigma}} + \alpha' - nwz \right\}$$

However, as we seen before,  $\alpha'$  is non-monotonic in  $\alpha$  and non-differentiable at  $\alpha = 3.7835$ , then we cannot apply the Envelope theorem. Moreover,  $V'(\cdot)$  is not concave so  $V'_{\alpha'}(\cdot)$  is non-monotonic as well (in terms of Carroll (2006),  $V'(\cdot)$  should be “well-behaved”).

Therefore we cannot apply the EGM for either of the problems. A solution could be to implement the EGM method with an Upper Envelope algorithm, such that the two (or more)  $\alpha'$  solutions that we obtain applying the EGM by itself, are reduced to just one by the selection of the  $\alpha'$  that maximizes the value function.