# Modeling of Time-Series Cross-Sectional / Panel Data

David Carlson

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- This heterogeneity could be different baselines, different slopes (treatment effects), etc.
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- Unfortunately, there is no one best solution; you need to carefully consider the level of aggregation, the likely DGP, etc.

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- Fixed effects control for heterogeneity in the data
- The inclusion of unit and time fixed effects accounts for both unit-specific (but time-invariant) and time-specific (but unit-invariant) unobserved confounders in a flexible manner

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- Very simple to run; just a linear model with factors

 Linearity (although one could nonparametrically adjust for unit-specific (time-specific) unobserved confounders by matching a treated observation with control observations of the same unit (time period), no other observation shares the same unit and time indices. Thus, the 2FE estimator critically relies upon the linearity assumption for its simultaneous adjustment for the two types of unobserved confounders)

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- Adjustment for the two types of unobserved confounders cannot be done nonparametrically under the 2FE framework

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- However, we need to assume parallel trends, i.e. the units (municipalities) have parallel trends in the outcome if it were not for treatment

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- When corrected SEs and un-corrected disagree, you very likely have a mis-specified model

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- Easy in R, but for the above reasons not as simple as a flag as in STATA

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- This also absorbs variation that may be meaningful
- Great for prediction, but not for inference; nevertheless this is another robustness check that is often asked for

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- First-difference estimators are designed to control for unobserved covariates in panel data, so we require less assumptions about the underlying mean function

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  - We no longer make the assumption of separability, and estimate the covariation of the parameters

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- Assumes that errors are uncorrelated with regressors

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