

Linear Regression Activity

① Fill in the table

Student	Hours Studied (x)	Exam Score (y)	xy	x ²	
1	1	52	52	1	
2	2	57	114	4	
3	3	61	183	9	
4	4	65	260	16	
5	5	76	380	25	
	$\Sigma x = 15$	$\Sigma y = 305$	$\Sigma xy = 989$	$\Sigma x^2 = 55$	

② Compute the slope

$$m = \frac{n(\Sigma xy) - (\Sigma x)(\Sigma y)}{n(\Sigma x^2) - (\Sigma x)^2} = \frac{5(989) - 15(305)}{5(55) - 15^2}$$

$$= \frac{4945 - 4575}{275 - 225} = \frac{220}{50}$$

$$m = 4.4$$

③ Compute the Intercept b

$$b = \frac{\Sigma y - m \Sigma x}{n} = \frac{305 - 4.4(15)}{5}$$

$$b = \frac{305 - 66}{5} = \frac{239}{5}$$

$$b = 47.8$$

④ Regression Equation

$$y = mx + b \quad y = 4.40x + 47.80$$

⑤ Draw the regression line using a scatter plot : $y = 4.4x + 47.8$:

Student	Hours Studied (x)	Exam Score (y)	Predicted Exam Score (y _{predict})
1	1	52	52.2
2	2	57	56.6
3	3	61	61.0
4	4	65	65.4
5	5	76	69.8

Solution:

① $y = 4.4(1) + 47.8 = 52.2$

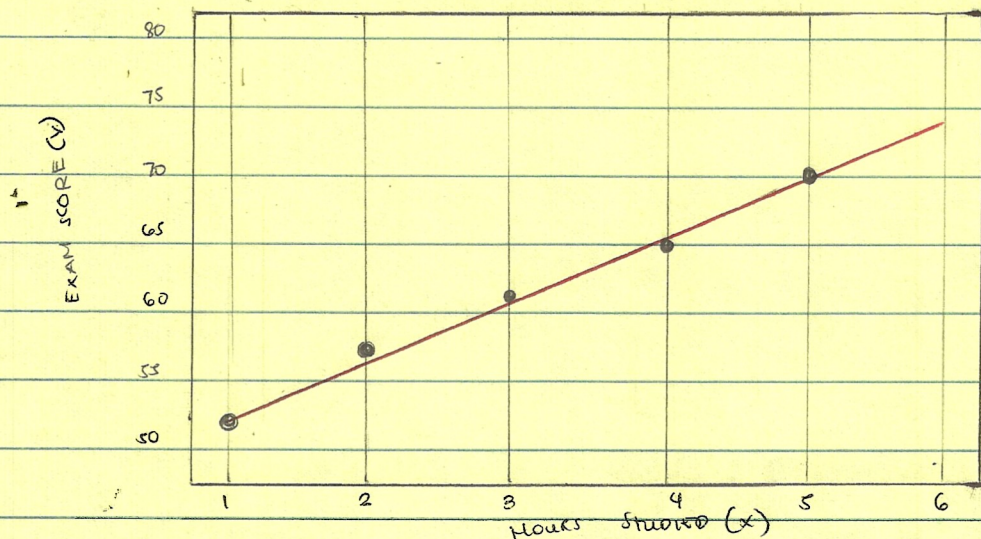
② $y = 4.4(2) + 47.8 = 56.6$

③ $y = 4.4(3) + 47.8 = 61.0$

④ $y = 4.4(4) + 47.8 = 65.4$

⑤ $y = 4.4(5) + 47.8 = 69.8$

5) Draw the regression line using a scatter plot



6) Calculate the Sum of Squared Errors

Student	Hours Studied (x)	Exam Score (y)	Predicted Exam Score (y _{pred})	y _i - y _{pred}	(y _i - y _{pred}) ²
1	1	52	52.2	-0.2	0.04
2	2	57	56.6	0.4	0.16
3	3	61	61.0	0.0	0.00
4	4	65	65.4	-0.4	0.16
5	5	70	69.8	0.2	0.04
SSE = 0.04 + 0.16 + 0 + 0.16 + 0.04					SSE = 0.40

7) Calculate the Sum of Squared Total

Get \bar{y} using this formula

$$\bar{y} = \frac{\sum y_i}{n} = \frac{305}{5} = 61$$

Get SST using this formula

$$SST = \sum (y_i - \bar{y})^2$$

Student	Hours Studied (x)	Exam Score (y _i)	Mean (\bar{y})	y _i - \bar{y}	(y _i - \bar{y}) ²
1	1	52	61	-9	81
2	2	57	61	-4	16
3	3	61	61	0	0
4	4	65	61	4	16
5	5	70	61	9	81
SST = (-9) ² + (-4) ² + 0 ² + 4 ² + 9 ² = 81 + 16 + 0 + 16 + 81 =					194

⑧ Compute R^2

Get R^2 using this formula

$$R^2 = 1 - \frac{SSE}{SST} = 1 - \frac{0.40}{194} = \boxed{0.997}$$

⑨ Prediction

Use your equation to predict score for a student who studied

6 hours

$$y = m(x) + b$$

$$y = 4.4(6) + 47.8 = 26.4 + 47.8 = \boxed{74.2}$$