Análisis en frecuencia de sistemas dinámicos

$$H(s) = Ks^{\pm N} \prod_{i=1}^{n} \frac{p_i}{s + p_i} \prod_{k=1}^{m} \frac{s + c_k}{c_k} \prod_{o=1}^{r} \frac{\omega_{no}^2}{s^2 + 2\zeta_o \omega_{no} s + \omega_{no}^2} \prod_{u=1}^{t} \frac{s^2 + 2\zeta_u \omega_{nu} s + \omega_{nu}^2}{\omega_{nu}^2}$$

 $|H(j\omega)|_{dB}=20Log(|H(j\omega)|)$ Magnitud del sistema en dB

 $arg\{H(j\omega)\}$ fase del sistema

Ganancia:

$$H(s) = K$$

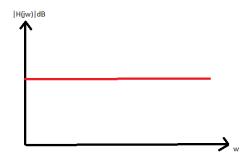
$$H(j\omega) = K$$

$$|H(j\omega)| = |K|$$

$$|H(j\omega)|_{dB} = 20Log(|K|) > 0 \quad if|K| > 1$$

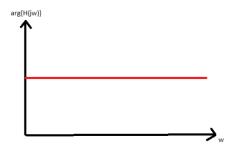
$$\left||H(j\omega)|_{dB} = 20Log(|K|) = 0 \ if \ |K| = 1\right|$$

$$|H(j\omega)|_{dB} = 20Log(|K|) < 0 \quad if|K| < 1$$



$$\arg\{H(j\omega)\} = 0 \text{ if } K > 0$$

$$arg\{H(j\omega)\} = 180^{\circ} if K < 0$$



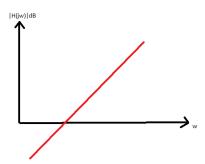
Derivador puro:

$$H(s) = s^N$$

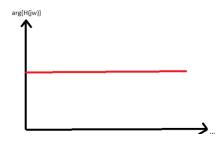
$$H(j\omega)=(j\omega)^N$$

$$|H(j\omega)| = \omega^{N}$$

$$|H(j\omega)|_{dB} = 20Log(\omega^{N}) = 20NLog(\omega)$$



$$arg{H(j\omega)} = arg{(j\omega)^N} = 90^{\circ}N$$



Integrador puro:

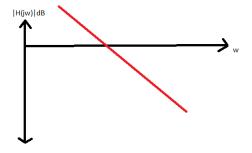
$$H(s) = s^{-N} = \frac{1}{s^{N}}$$

$$H(j\omega) = \frac{1}{(j\omega)^{N}}$$

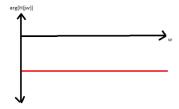
$$|H(j\omega)| = \frac{1}{\omega^{N}}$$

$$|H(j\omega)|_{dB} = 20Log(\frac{1}{\omega^{N}}) = 20Log(1) - 20Log(\omega^{N})$$

$$\overline{|H(j\omega)|_{dB}} = -20NLog(\omega)$$



$$\arg\{H(j\omega)\} = \arg\left\{\frac{1}{(j\omega)^N}\right\} = \arg\{1\} - \arg\{(j\omega)^N\}$$
$$\arg\{H(j\omega)\} = -90^\circ N$$



Derivador simple (ceros reales distintos de cero):

$$H(s) = \frac{s+c}{c}$$

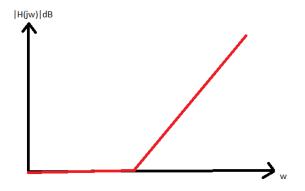
$$H(j\omega) = \frac{j\omega + c}{c}$$

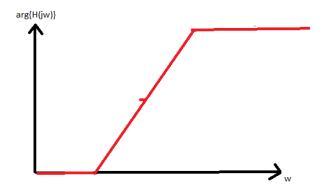
$$|H(j\omega)| = \frac{|j\omega + c|}{|c|} = \frac{\sqrt{\omega^2 + c^2}}{|c|}$$

$$|H(j\omega)|_{dB} = 20Log\left(\frac{\sqrt{\omega^2+c^2}}{|c|}\right) = 20Log\left(\sqrt{\omega^2+c^2}\right) - 20Log(|c|)$$

$$|arg {j\omega + c \choose c}| = arg {j\omega + c} - arg {c}| = atan {\omega \choose c}$$

ω	$ H(j\omega) _{dB}$	$\arg\left\{\frac{j\omega+c}{c}\right\}^{\circ}$
$(pequeña)\omega \approx 0$	0	0
$\omega = c$	3.01	45
$(grande)\omega \approx \infty$	$20Log(\omega)$	90





Integrador simple (polos reales distintos de cero):

$$H(s) = \frac{p}{s+p}$$

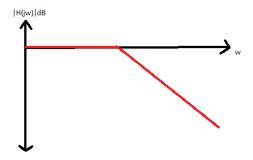
$$H(j\omega) = \frac{p}{j\omega + p}$$

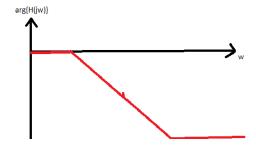
$$|H(j\omega)| = \frac{|p|}{|j\omega + p|} = \frac{|p|}{\sqrt{\omega^2 + p^2}}$$

$$|H(j\omega)|_{dB} = 20 Log \left(\frac{|p|}{\sqrt{\omega^2 + p^2}}\right) = 20 Log(|p|) - 20 Log \left(\sqrt{\omega^2 + p^2}\right)$$

$$\overline{\arg\left\{\frac{p}{j\omega+p}\right\} = \arg\{p\} - \arg\{j\omega+p\} = -\operatorname{atan}\left(\frac{\omega}{p}\right) }$$

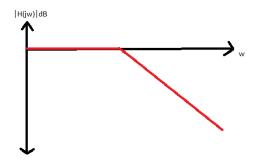
ω	$ H(j\omega) _{dB}$	$\arg\left\{\frac{j\omega+c}{c}\right\}^{\circ}$
$(peque\tilde{n}a)\omega \approx 0$	0	0
$\omega = p$	-3.01	-45
$(grande)\omega \approx \infty$	$-20Log(\omega)$	-90

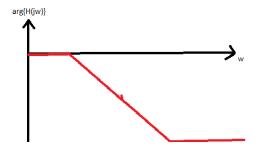




Polos complejos conjugados:

$$H(s) = \frac{\omega_n^2}{s^2 + 2\zeta_o \omega_n s + \omega_n^2}$$





Ceros complejos conjugados:

$$H(s) = \frac{s^2 + 2\zeta_u \omega_n s + \omega_n^2}{\omega_n^2}$$

