

$$e_{a} = iR_{a} + \alpha \dot{\theta}$$

$$(J_{m} + J_{t})\ddot{\theta} = \alpha i - B_{1}\dot{\theta} - Fr$$

$$M\ddot{x} = F - B_{2}\dot{x} - F_{d}$$

$$e_{2} = K\dot{\theta}$$

$$e_{a} = -K_{A}(e_{2} - e_{1}) = K_{A}(e_{1} - e_{2})$$

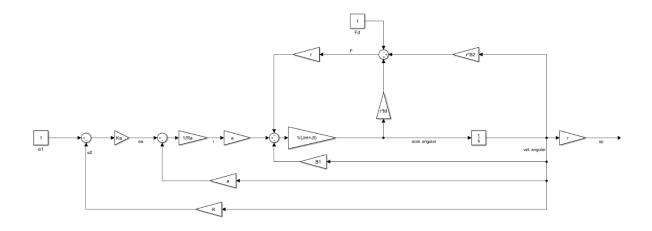
$$x = r\theta$$

$$\dot{x} = r\dot{\theta}$$

$$\ddot{x} = r\ddot{\theta}$$

Diagrama de bloques:

$$\ddot{\theta} = \frac{\alpha i - B_1 \dot{\theta} - Fr}{J_m + J_t}$$
 
$$F = M \ddot{x} + B_2 \dot{x} + F_d$$



VE:

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} \theta \\ \dot{\theta} \end{bmatrix}$$
$$\begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} e_1 \\ F_d \end{bmatrix}$$
$$y = \dot{x} = r\dot{\theta} = rx_2$$

Derivamos los estados

$$\dot{x}_1 = x_2$$

$$\dot{x}_2 = \ddot{\theta} = \frac{\alpha i - B_1 \dot{\theta} - Fr}{J_m + J_t}$$

$$F = M\ddot{x} + B_2 \dot{x} + F_d = Mr\ddot{\theta} + B_2 r\dot{\theta} + F_d$$

$$i = \frac{e_a - \alpha \dot{\theta}}{R_a}$$

$$e_a = K_A (e_1 - K\dot{\theta})$$

$$i = \frac{K_A (e_1 - K\dot{\theta}) - \alpha \dot{\theta}}{R_a}$$

$$\ddot{\theta} = \frac{\alpha \frac{K_A (e_1 - K\dot{\theta}) - \alpha \dot{\theta}}{R_a} - B_1 \dot{\theta} - (Mr\ddot{\theta} + B_2 r\dot{\theta} + F_d)r}{J_m + J_t}$$

$$(J_m + J_t + Mr^2) \ddot{\theta} = \alpha \frac{K_A (e_1 - K\dot{\theta}) - \alpha \dot{\theta}}{R_a} - B_1 \dot{\theta} - B_2 r^2 \dot{\theta} - F_d r$$

$$\ddot{\theta} = \frac{\alpha \frac{K_A (e_1 - K\dot{\theta}) - \alpha \dot{\theta}}{R_a} - B_1 \dot{\theta} - B_2 r^2 \dot{\theta} - F_d r}{J_m + J_t + Mr^2}$$

$$\dot{x}_2 = \frac{\alpha \frac{K_A(u_1 - Kx_2) - \alpha x_2}{R_a} - B_1 x_2 - B_2 r^2 x_2 - u_2 r}{J_m + J_t + M r^2}$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{pmatrix} 0 & 1 & 0 \\ 0 & -\frac{\alpha K_A K + \alpha^2}{R_a} + B_1 + B_2 r^2 \\ J_m + J_t + M r^2 \end{pmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{pmatrix} 0 & 0 \\ \frac{\alpha K_A}{R_a} & -r \\ J_m + J_t + M r^2 & J_m + J_t + M r^2 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$

$$y = (0 \quad r) \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$