

What is Statistical Learning?

Intuition behind Statistical Learning

N Weight Height ... Age				?		Blood Pressure
1	166	153	59			?
2	177	167	49			?
3	159	176	50			?
4	169	150	75			?
5	148	161	53			?
6	179	180	47			?
7	153	169	51			?
8	156	157	89			?
9	162	158	44			?

Traditional Approach

N	Weight	Height	Age	$Y = (0.3 * Weight) + (0.25 * Height) + (0.5 * Age)$	Blood Pressure
1	166	153	59		
2	177	167	49		
3	159	176	50		
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Traditional Approach

N	Weight	Height	Age	$Y = (0.3 * Weight) + (0.25 * Height) + (0.5 * Age)$	Blood Pressure
1	166	153	59	----->	117.55
2	177	167	49	----->	119.35
3	159	176	50	----->	116.7
4	169	150	75	----->	125.7
5	148	161	53	----->	111.15
6	179	180	47	----->	122.2
7	153	169	51	----->	113.65
8	156	157	89	----->	130.55
9	162	158	44	----->	110.1

Statistical Learning Approach

N	Weight	Height	...	Age		Blood Pressure
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Statistical Learning Approach

N	Weight	Height	...	Age		Blood Pressure
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Intuition behind Statistical Learning



Intuition behind Statistical Learning



Why do we estimate $f(\mathbf{x})$?

Why do we use Statistical Learning?

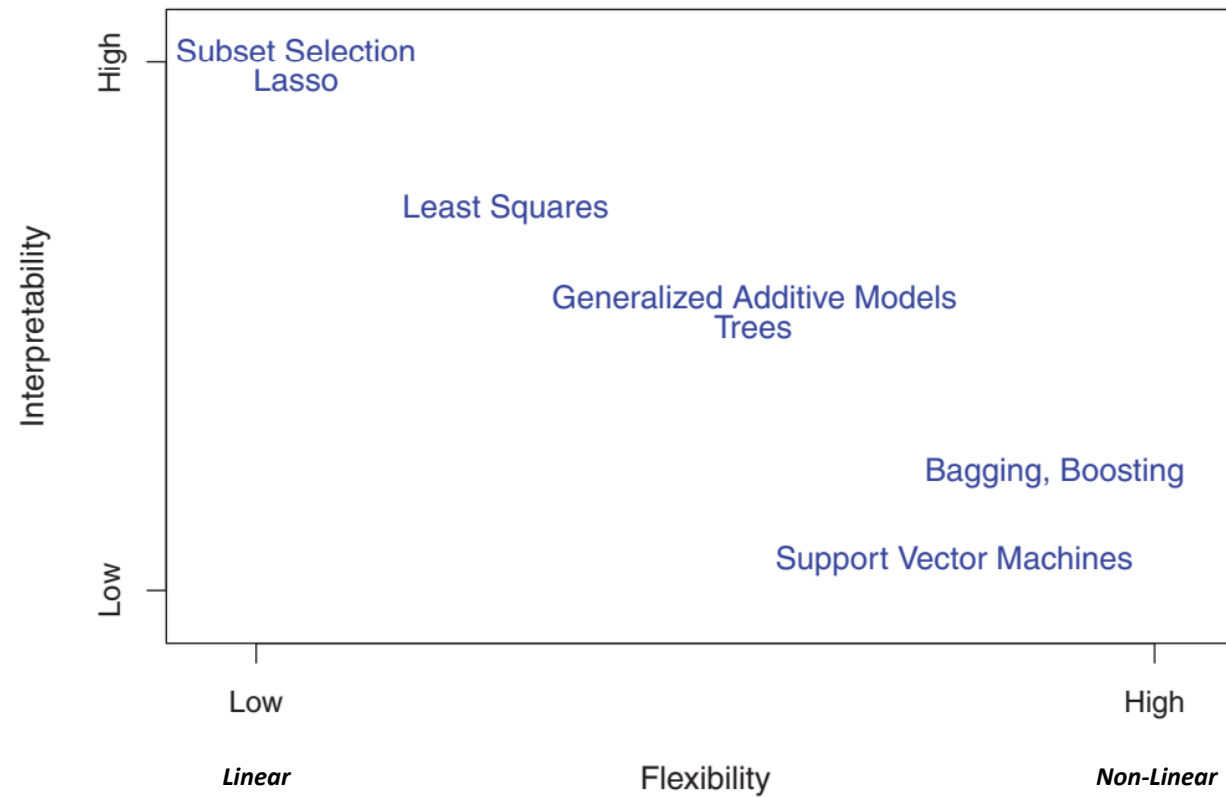
Prediction

N	Weight	Height	...	Age		Blood Pressure
1	166	153		59	<div><div><div></div><div></div><div></div></div><div><div></div><div></div><div></div></div><div><div></div><div></div><div></div></div></div> <div><div></div><div></div><div></div></div> <div>$Y = f(x)$</div> <div>$Y = (0.3 * Weight) + (0.25 * Height) + (0.5 * Age)$</div>	117.55
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Why do we use Statistical Learning?

- Which **Predictors** are associated with the **response**?
 - Not all variables used in models are substantially associated to the response.
- What is the **relationship** between the response and each **predictor**?
 - Some predictors can have positive effects in the response. Other predictors may have opposite effects.
- Can the relationship between **Y** and each predictor be adequately summarized using a **linear equation**, or is the relationship more complicated?
 - Not always the nature of the relationship is linear.

Trade-Off Between Prediction Accuracy and Model Interpretability

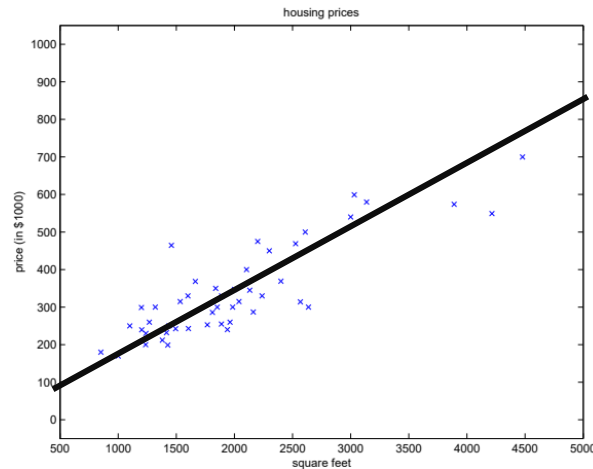


- The more linear the model, the more explainable.
- The more non-linear (flexible) the more

Types of Machine Learning Problems

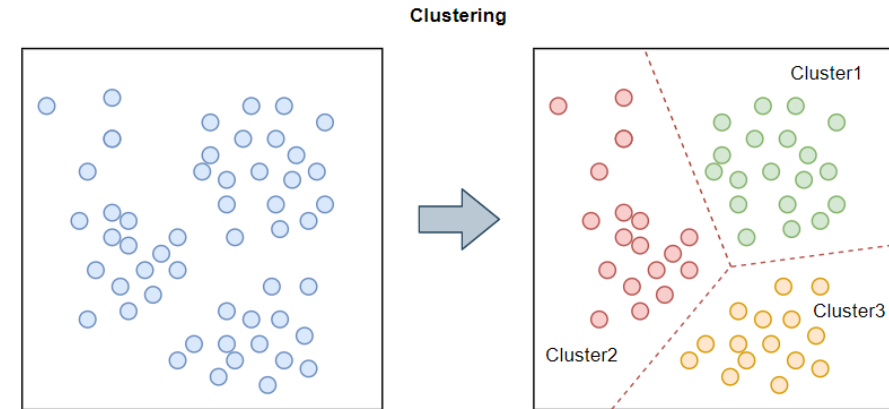
Supervised Learning

Living area (feet ²)	Price (1000\$)
2104	400
1600	330
2400	369
1416	232
3000	540
⋮	



We know the input (*features/predictors*) and the response or *target*.

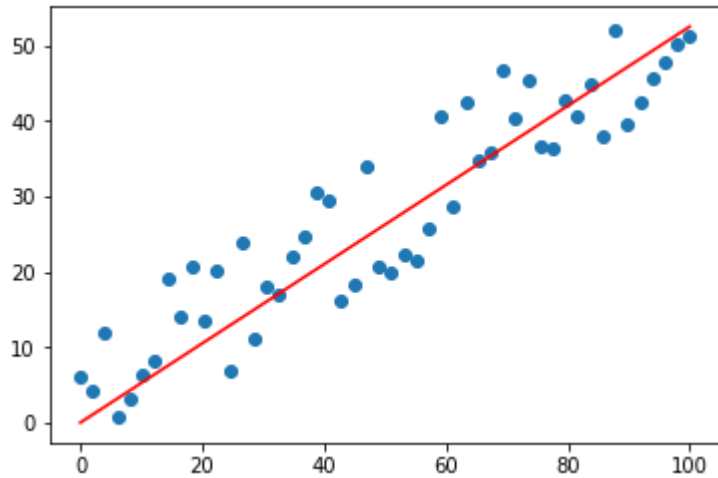
Unsupervised Learning



We do not have the answer (*Target*). However, we want to find structure in data (*clustering*).

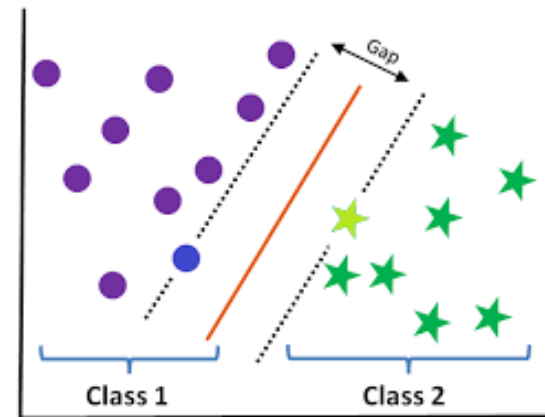
Supervised Learning

Regression



We are trying to **predict** a value (*Sales, Blood pressure*)

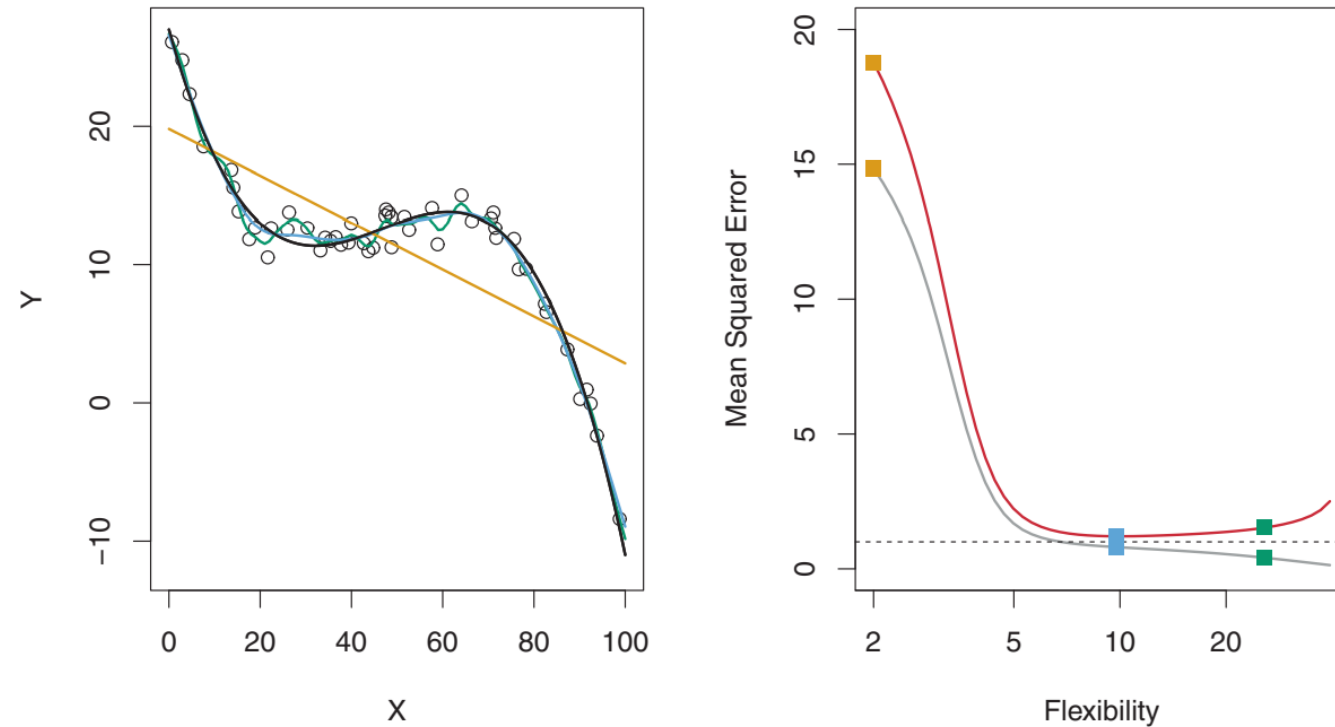
Classification



We are trying to **predict** whether a specific point belongs to a **category**

Different types of Regression

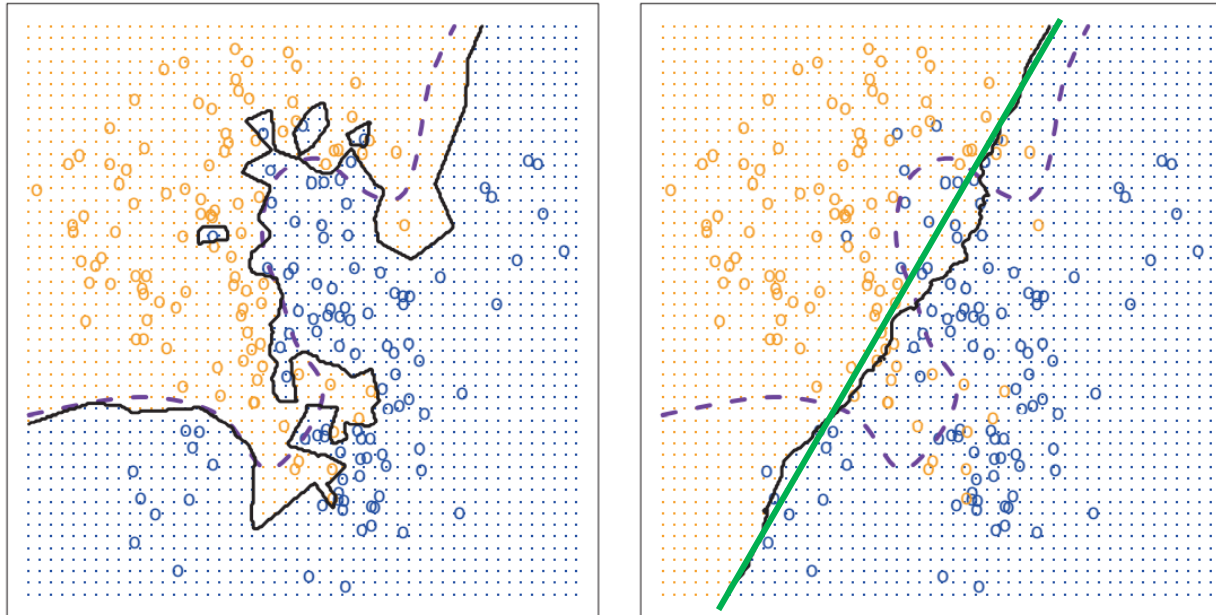
Error vs. Flexibility



* In the left chart we can find that we can adjust different types of curves to the same data. The nature of those curves can be either linear or non-linear

Different types of Classification

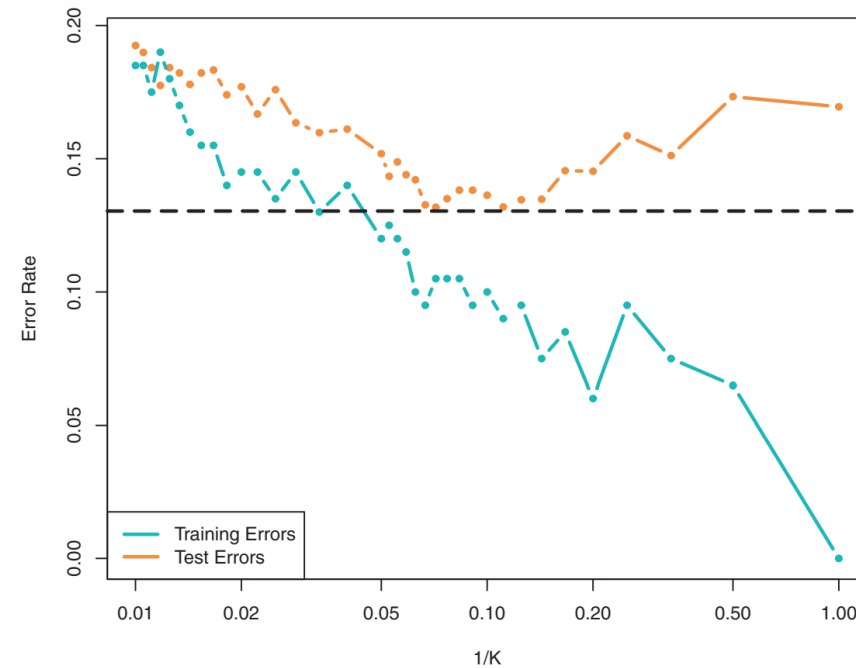
Classification



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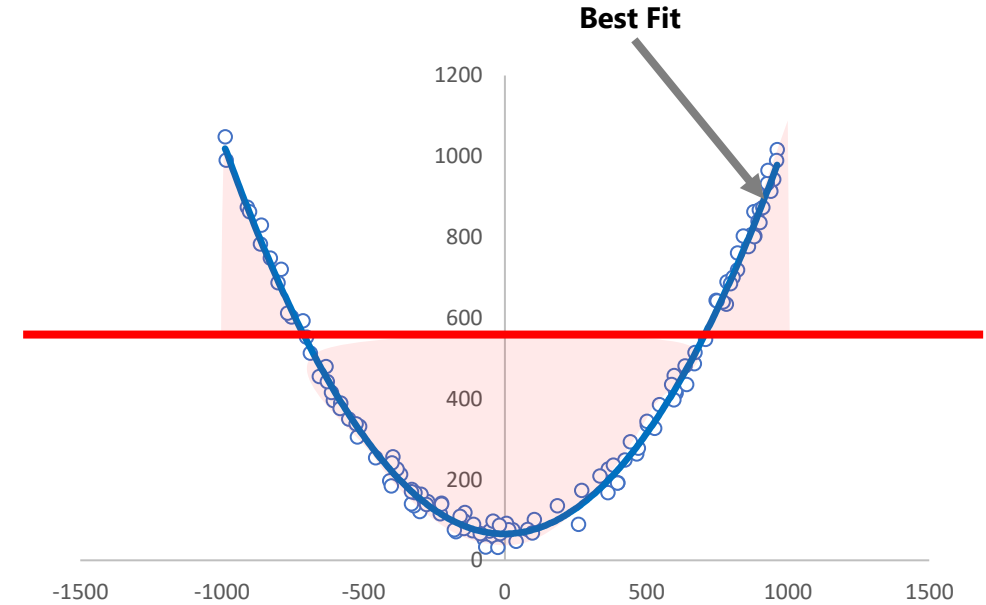
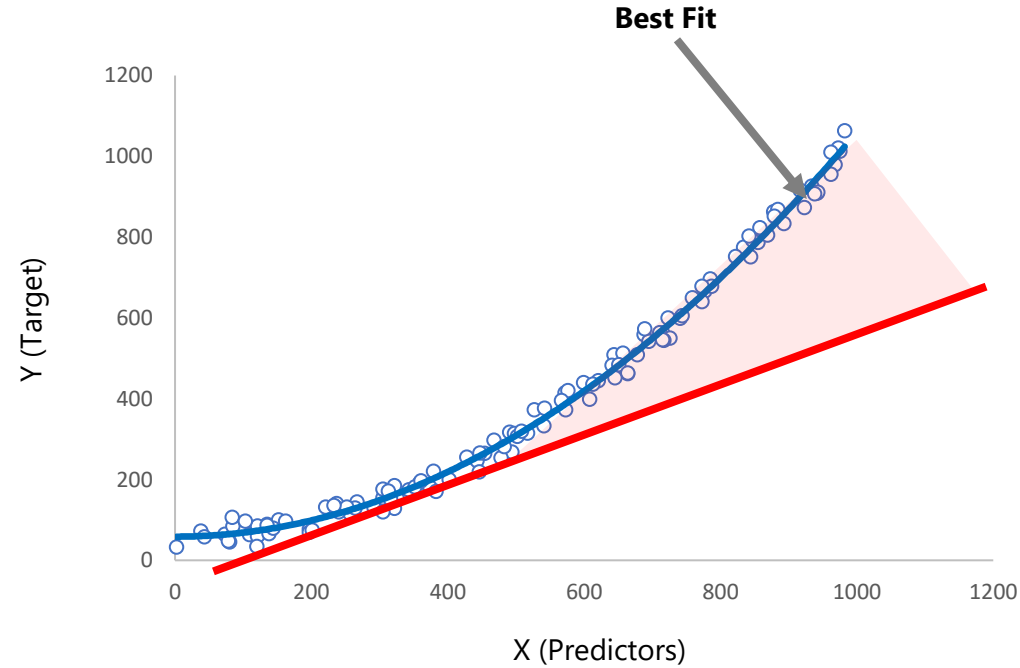
Different types of Classification

Classification



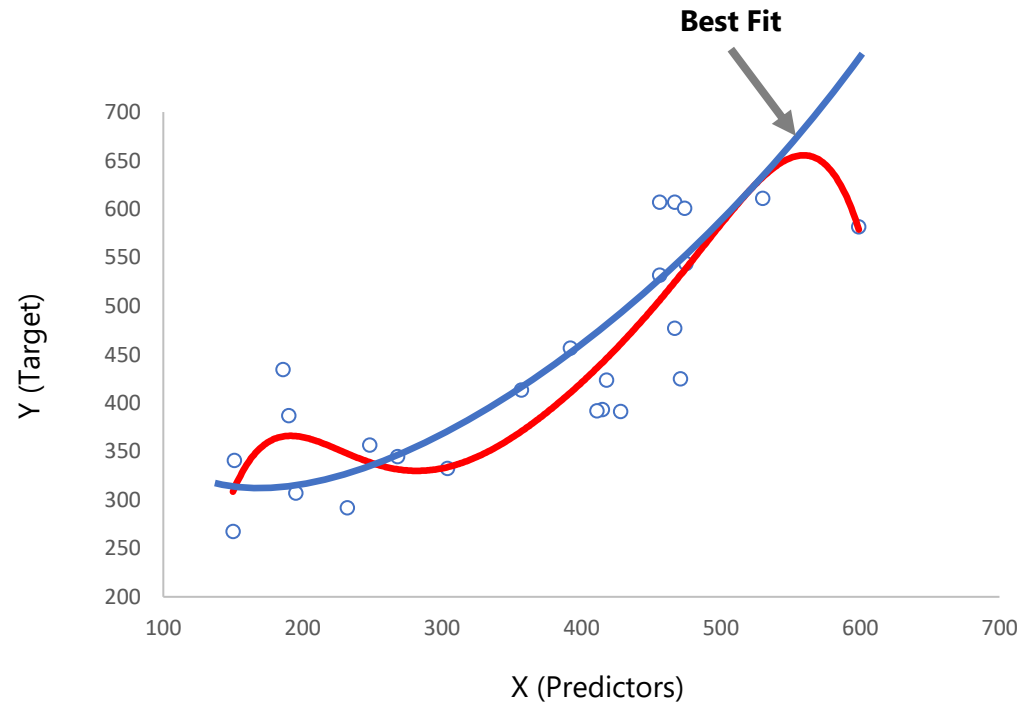
The more specific (**more flexible the model**), the higher the expected error for the testing data (**new data**).

Bias



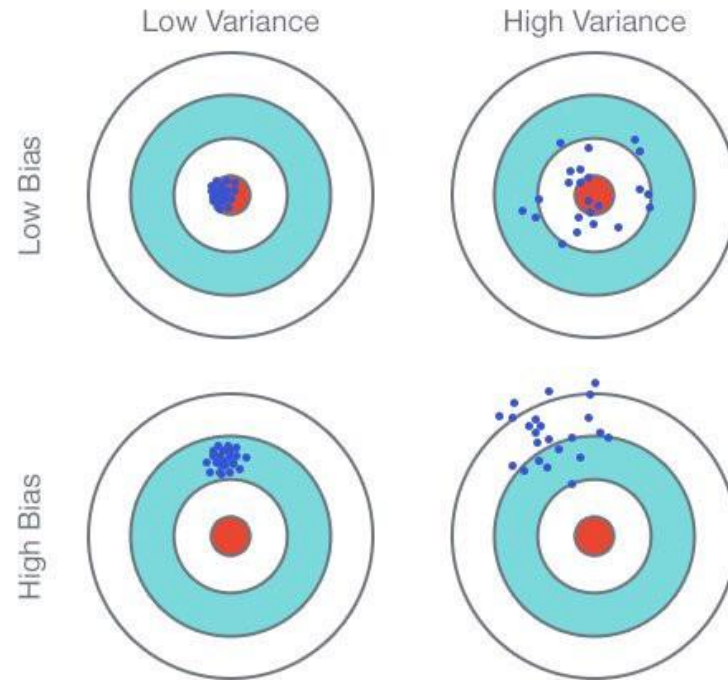
Bias can be understood as the behavior of always **underrepresenting** the data. **Bias** refers to the error of trying to explain an extremely complicated problem (**data**) with a much simpler model.

Variance



Variance can be understood as overrepresenting the training data. This means that the model is too specific to the data that the model has seen. However, it would not perform very well on new data.

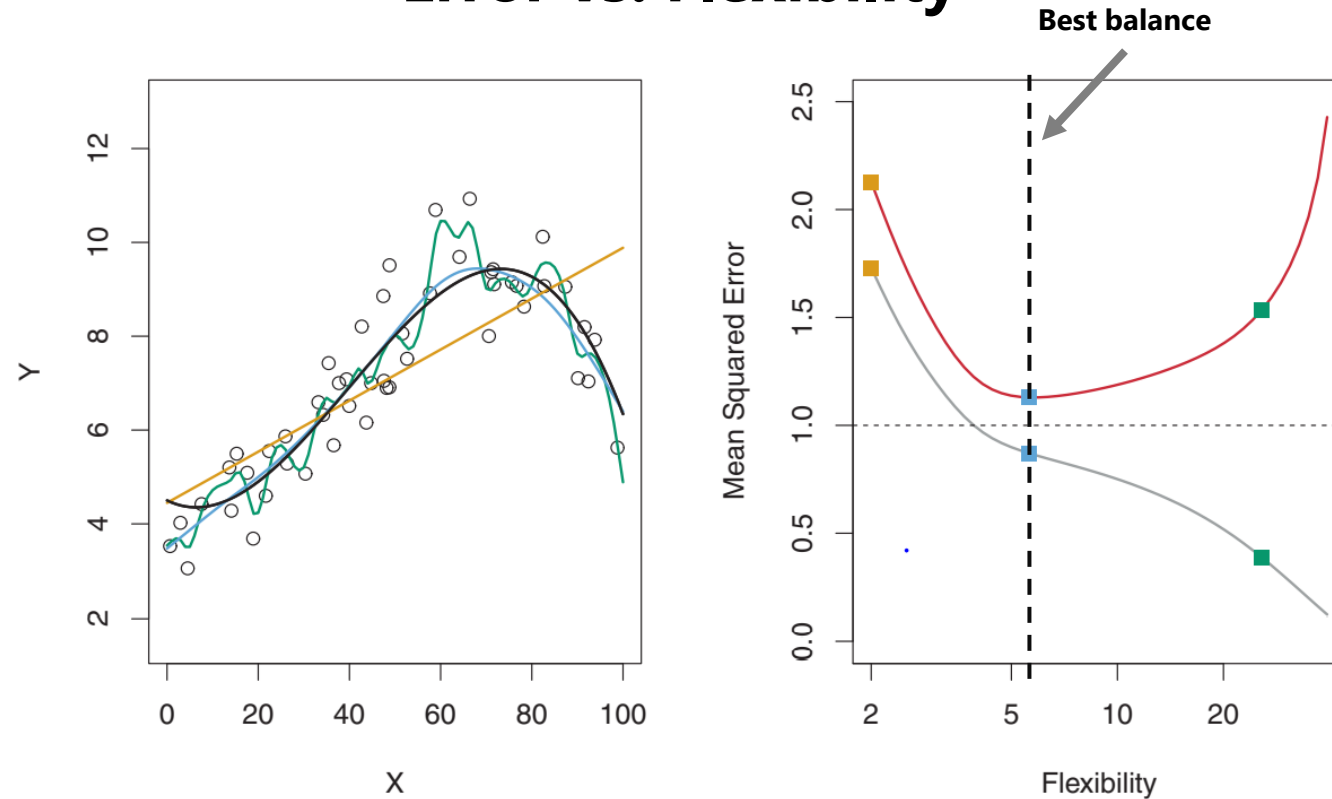
Bias and Variance



Visual representation of **Bias** and **Variance**.

Bias-Variance Trade-off

Error vs. Flexibility



The total error of the model is the sum of both the **Bias** and **Variance**. Thus we always want find the right balance between them.