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a. Use the read.cvs command to read the Earnings_and_Height.cvs data set into R. Use the attach command to attach the data set into R.

```
eah <- read.csv("Earnings_and_Height.csv")</pre>
attach(eah)
```

b. Print out an summary of the data set. In particular, find and report the sample average of the variables earnings, height and sex, respectively.

```
# The summary shows: Min. 1st Qu. Median Mean
summary(eah)
                                                                      3rd Qu.
                                                                                Max
        sex
                                       mrd
                                                      educ
                        age
   Min.
          :0.0000
                   Min. :25.00 Min. :1.000
                                                 Min. : 0.00
   1st Qu.:0.0000
                   1st Qu.:33.00
                                 1st Qu.:1.000
                                                 1st Qu.:12.00
                                 Median :1.000
   Median :0.0000
                   Median:40.00
                                                 Median :13.00
         :0.4419
                   Mean :40.92 Mean :2.362
   Mean
                                                 Mean :13.54
   3rd Qu.:1.0000
                   3rd Qu.:48.00
                                 3rd Qu.:4.000
                                                 3rd Qu.:16.00
          :1.0000
                   Max. :65.00 Max. :6.000
   Max.
                                                 Max. :19.00
      cworker
                      region
                                      race
                                                   earnings
   Min.
          :1.000
                  Min. :1.000
                                 Min. :1.000
                                                Min. : 4726
                  1st Qu.:2.000
                                 1st Qu.:1.000
   1st Qu.:1.000
                                                1st Qu.:23363
   Median :1.000
                  Median :3.000
                                 Median :1.000
                                                Median :38925
         :1.964
                                 Mean :1.386
                                                Mean :46875
   Mean
                  Mean :2.551
                                 3rd Qu.:1.000
                                                3rd Qu.:84055
   3rd Qu.:3.000
                  3rd Qu.:3.000
          :6.000
                  Max. :4.000
                                 Max. :4.000
   Max.
                                                Max.
                                                       :84055
       height
                      weight
                                   occupation
##
   Min.
          :48.00
                  Min. : 80.0
                                 Min. : 1.000
   1st Qu.:64.00
                  1st Qu.:140.0
                                 1st Qu.: 2.000
   Median :67.00
                  Median:163.0
                                 Median : 5.000
          :66.96
                  Mean :170.4
                                 Mean : 6.011
   3rd Qu.:70.00
                  3rd Qu.:190.0
                                 3rd Qu.: 8.000
   Max.
          :84.00
                  Max. :501.0
                                 Max. :15.000
```

summary(earnings)

```
Min. 1st Qu. Median
                      Mean 3rd Qu.
                                     Max.
4726 23363
             38925
                     46875
                             84055
                                     84055
```

summary(height)

```
Min. 1st Qu. Median
                    Mean 3rd Qu.
48.00 64.00 67.00 66.96 70.00 84.00
```

summary(sex)

```
Min. 1st Qu. Median
                          Mean 3rd Qu.
## 0.0000 0.0000 0.0000 0.4419 1.0000 1.0000
```

The sex is a dummy variable where: 1=Male, 0 = Female

c. Run a regression of earnings on height. In particular, find and use a sentence to interpret the meaning of the regression coefficient of the variables height.

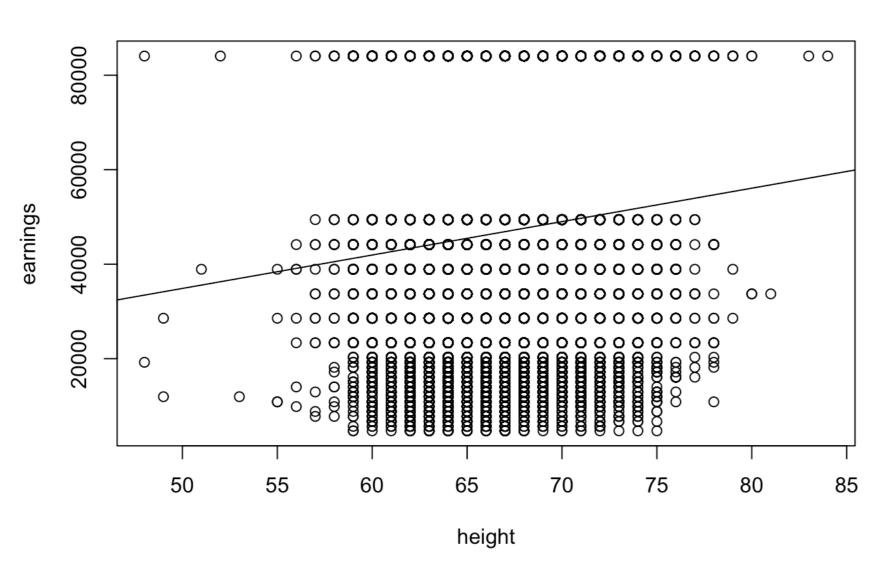
```
# Regression
ols <- lm(earnings ~ height)</pre>
summary(ols)
```

```
## Call:
## lm(formula = earnings ~ height)
## Residuals:
     Min
             10 Median
## -47836 -21879 -7976 34323 50599
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -512.73 3386.86 -0.151
                707.67 50.49 14.016 <2e-16 ***
## height
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 26780 on 17868 degrees of freedom
## Multiple R-squared: 0.01088, Adjusted R-squared: 0.01082
## F-statistic: 196.5 on 1 and 17868 DF, p-value: < 2.2e-16
```

```
# We have got that the height has this coefficients:
              707.67
                           (\beta 1) This means that when the height increases by 1 (one inch taller)
   Estimate
                           the earnings increase by $707.67.
   Std. Error 50.49
                           (standard error of eta1) This means that the average distance that the observed values
                           deviate from the regression line is 50.49
                            (The smaller the value, the closer our values are to the regression line)
   t value
                            This is the coefficient divided by its standard error
\# Pr(>|t|)
               <2e-16 *** p-value
```

d. Plot a graph of earnings over height. e) On the graph, add a fitted line of the regression.

```
plot(earnings ~ height)
abline(ols)
```



f. Suppose Alex is 65 inches; Bob is 67 inches; Chris is 70 inches tall. Based on the regression, predict their corresponding earnings.

```
# Alex (Method 1)
-512.73 + 707.67*65
```

[1] 45485.82

```
# Bob (Method 2)
ols$coefficient[1] + ols$coefficient[2] * 67
```

```
## (Intercept)
     46901.26
```

Chris(Method 3)

```
predict(ols, data.frame(height=70))
```

```
## 49024.28
```

g. Find the R2 and SER from the regression in part (c). Use a sentence to interpret each of them.

```
When we did the summary of the ols we got a residual standard error (SER) of $26780 and it is the measure
of the spread of the error term u (in this case is quite large so is not a good thing).
We also got the R2 which it appears to be 0.01088. This means that approximately 1.09% of earnings are
explained by the height.
```

h. Based on the regression in part (c), find the p-value of the variables height and perform a t-test.

```
The summary of the ols shows that our p-value is smaller than 2.2e-16.
If we do the t-test based on the p-value we get that the absolute value of the p-value is smaller than 1.96
For that reason we reject the null (H0: \beta1=0).
That means that \beta1!=0 so there is a relationship between height and earnings.
```

i. Based on the regression in part (c), use the confint command to calculate the Confidence Interval (CI) of the variables height. Does your CI give you the same t-test conclusion?

```
confint(ols)
```

```
2.5 % 97.5 %
## (Intercept) -7151.2994 6125.8322
## height
                608.7078 806.6353
```

We've got that the CI = [608.7078, 806.6353]. Since 0 is out of the CI we also end up rejecting the null. # This is to be expected as all three t-test methods are equivalent.

```
ols2<- lm(earnings ~ sex)</pre>
summary(ols2)
```

j. Run a regression of earnings on sex. For both the regression intercept and coefficient of the variables sex, use a sentence to interpret its

```
##
## Call:
## lm(formula = earnings ~ sex)
## Residuals:
     Min
           1Q Median
                          3Q Max
## -43733 -22258 -6696 35595 38434
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 45621.0 269.2 169.455 < 2e-16 ***
## sex
               2838.8 405.0 7.009 2.49e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 26890 on 17868 degrees of freedom
## Multiple R-squared: 0.002742, Adjusted R-squared: 0.002686
## F-statistic: 49.13 on 1 and 17868 DF, p-value: 2.485e-12
```

```
# We've got that Earnings = 45621 + 2838.8 \times Male (as the sex variables are 1=Male, 0 = Female).
# This means that men earn on average $2838.8 more than women.
# We can also see that the mean earnings of women is $45621.
# And if we want to know the mean earnings of men we just need to set the sex = 1 which results in:
45621.0+2838.8
```

```
## [1] 48459.8
```

meaning.