

For the problem:

$$\begin{aligned} \text{Min} \quad & -x_1 - x_2 \\ & x_1 + 2x_2 - 3 \leq 0 \\ & 0 \leq x_i \leq 3, \quad x_i \in \mathbb{Z} \end{aligned}$$

1. Find the duality gap if it exists; find the dual-lagrangian function and its maximum
2. Reproduce, in the corresponding dominium, the result:

$$\varphi^c(s, t) = \psi(s, t) = \text{Max}_{\lambda, \mu \geq 0} \left[\text{Min}_x_{x \in X} f(x) - \lambda^t h(x) - \mu^t g(x) \right]$$