

```

1 begin
2     using StatsBase
3     using Distributions
4     using InformationMeasures
5     using Plots
6     using PlutoUI
7 end
8

```

 0.27

```

1 #Creating some sliders so we can change p (noise probability) and N (message length)
2 @bind p Slider(0:0.01:0.5, default = 0.1, show_value = true)

```

 20000

```

1 @bind N Slider(1000:1000:20000, default = 10000, show_value = true)

```

BitVector: [true, true, false, false, true, true, true, true, false, false, true, false, false]

```

1 begin
2     #Generating a random binary message and putting the message through a noisy channel
3     message = rand(Bool, N)
4
5     function binary_symmetric_channel(bits, p)
6         flips = rand(Bernoulli(p), length(bits))
7         return xor.(bits, flips)
8     end
9
10    received = binary_symmetric_channel(message, p)
11 end

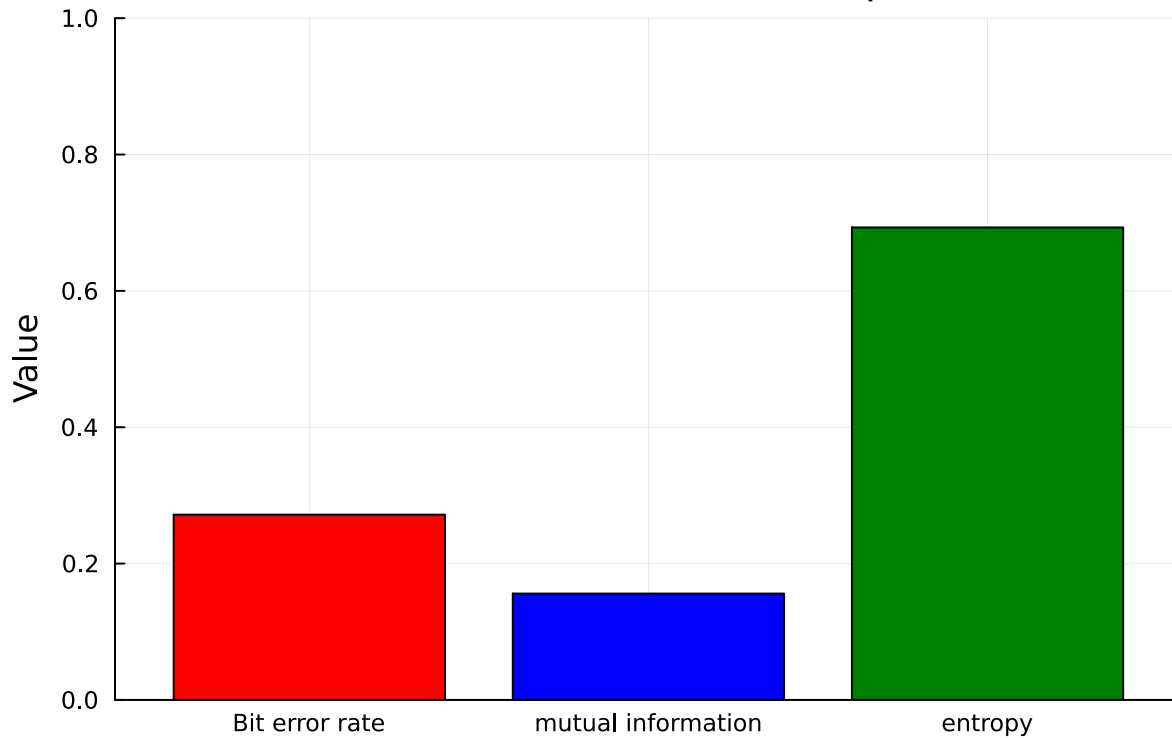
```

0.6930463571714478

```

1 begin
2     #Some information measures
3     bit_error_rate = sum(message .!= received) / N
4     mutual_info = get_mutual_information(message, received)
5     received_entropy = entropy(Float64[mean(received), 1 - mean(received)])
6 end

```

simulated channel measures $p = 0.27$ 

```

1 #Plotting things
2 bar(
3     ["Bit error rate", "mutual information", "entropy"],
4     [bit_error_rate, mutual_info, received_entropy],
5     legend = false,
6     color = [:red, :blue, :green],
7     ylim = (0,1),
8     title = "simulated channel measures p = $(round(p,digits=2))",
9     ylabel = "Value"
10 )

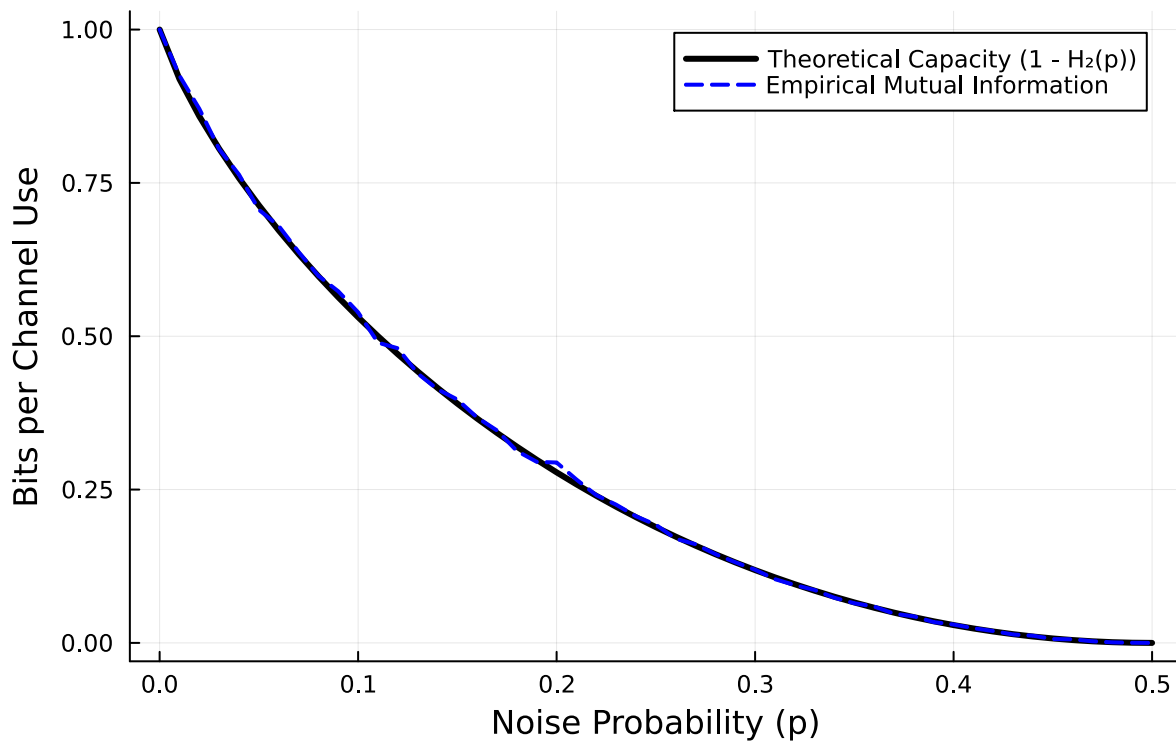
```

```

1 begin
2     #Comparing with Shannon's Thoeoretical Channel Capacity
3
4     function binary_entropy(p)
5         if p == 0 || p == 1
6             return 0.0
7         else
8             return -p*log2(p) - (1-p)*log2(1-p)
9         end
10    end
11
12    ps = 0:0.01:0.5
13    capacity = [1 - binary_entropy(p) for p in ps]
14
15    mutual_infos = Float64[]
16    for prob in ps
17        received_temp = binary_symmetric_channel(message,prob)
18        push!(mutual_infos, get_mutual_information(message, received_temp))
19    end
20 end

```

Shannon Capacity vs Simulated Mutual Information



```

1 begin
2     #Combining the plots
3     plot(
4         ps, capacity,
5         label="Theoretical Capacity (1 - H2(p))",
6         lw=3, color=:black,
7         xlabel="Noise Probability (p)",
8         ylabel="Bits per Channel Use",
9         title="Shannon Capacity vs Simulated Mutual Information",
10        legend=:topright
11    )
12
13    plot!(
14        ps, mutual_infos,
15        label="Empirical Mutual Information",
16        lw=2, color=:blue, ls=:dash
17    )
18
19 end

```