Name:	Question 1	
	Question 2	
Exam 2	Question 3	
CSc 75010: Theoretical Computer Science	Question 4	
Graduate Center of CUNY	Question 5	
22 November 2002	Question 6	
(Orange Version)	Total	

Do five of the following six problems. Write each answer on a separate piece of paper.

- 1. (a) Define decidable set and give an example of a set that is not decidable.
  - (b) Assume that the alphabet and tape alphabet are:  $\Sigma = \Gamma = \{0, 1\}$ . Give an implementation level description of a Turing machine that decides the language:

 $\{w \mid w \text{ is a palindrome}\}$ 

- 2. (a) Show that the set of all positive rational numbers is countable.
  - (b) Show that the set of all positive real numbers is uncountable.
- 3. (a) Show that the Halting Problem is undecidable, using the diagonalization method.
  - (b) Show that the set of all totally defined computable functions is not decidable.
- 4. (a) Show that the set of Turing-recognizable languages is closed under concatenation.
  - (b) Show that if A is decidable, then A and  $\bar{A}$  are Turing-recognizable.
- 5. (a) State the Post Correspondence Problem (PCP).
  - (b) Show that PCP is decidable over the alphabet  $\Sigma = \{1\}$ .
- 6. (a) Show that  $\leq_m$  is transitive.
  - (b) Show for all A, B, there exists a set J such that  $A \leq_T J$  and  $B \leq_T J$ .