

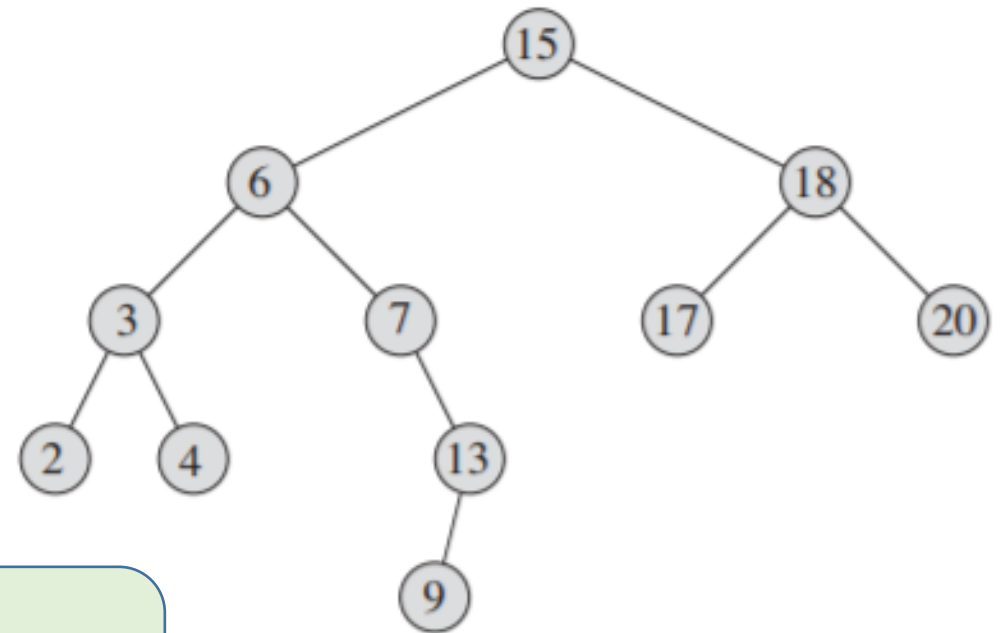


COMP 2611, Data Structures

LECTURE 8: BINARY TREES AND BINARY SEARCH TREES

Binary Trees: Inorder Traversal

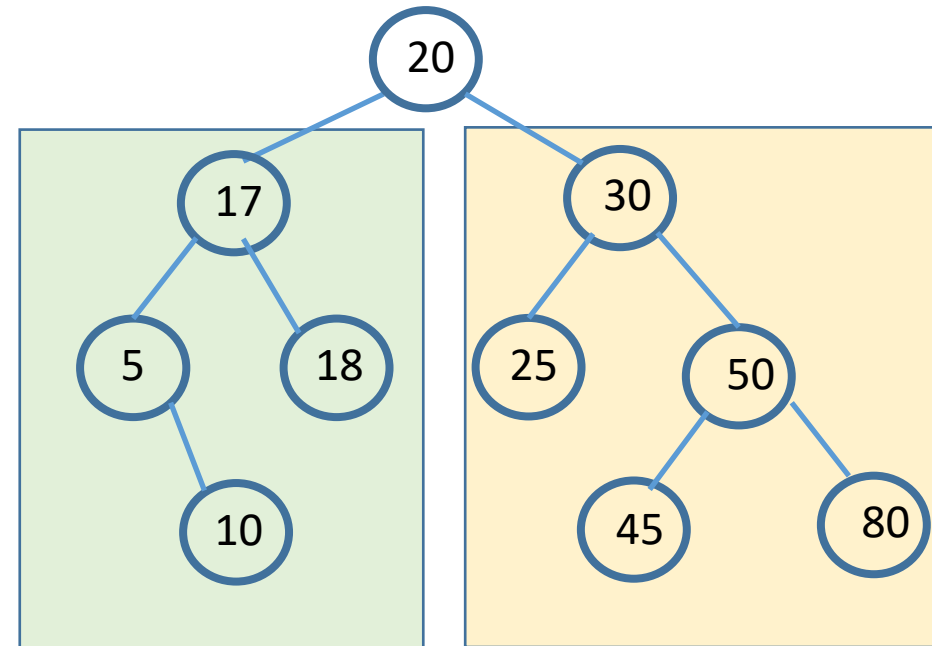
- Give the inorder traversal of this binary tree:



2, 3, 4, 6, 7, 9, 13, 15, 17, 18, 20

Binary Trees: Inorder Traversal

- Give the inorder traversal of this binary tree:

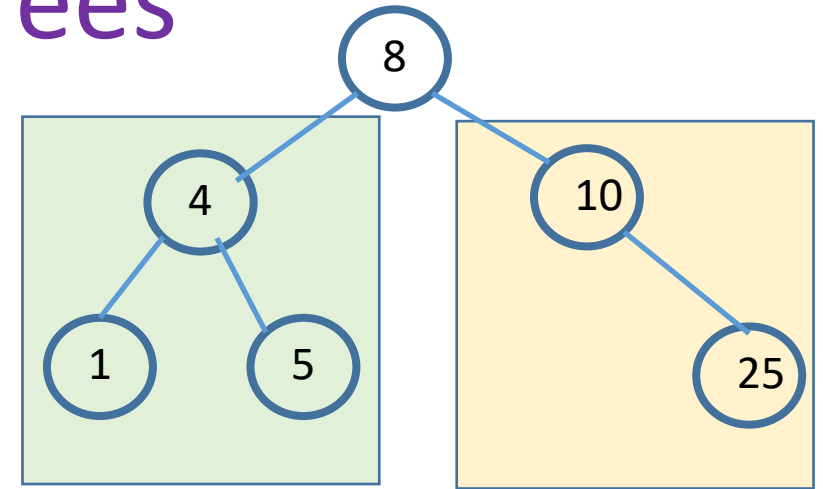


5, 10, 17, 18, 20, 25, 30, 45, 50, 80

Binary Search Trees

➤ A binary search tree (BST) is a binary tree where the keys stored at each node satisfy the *binary-search-tree property*:

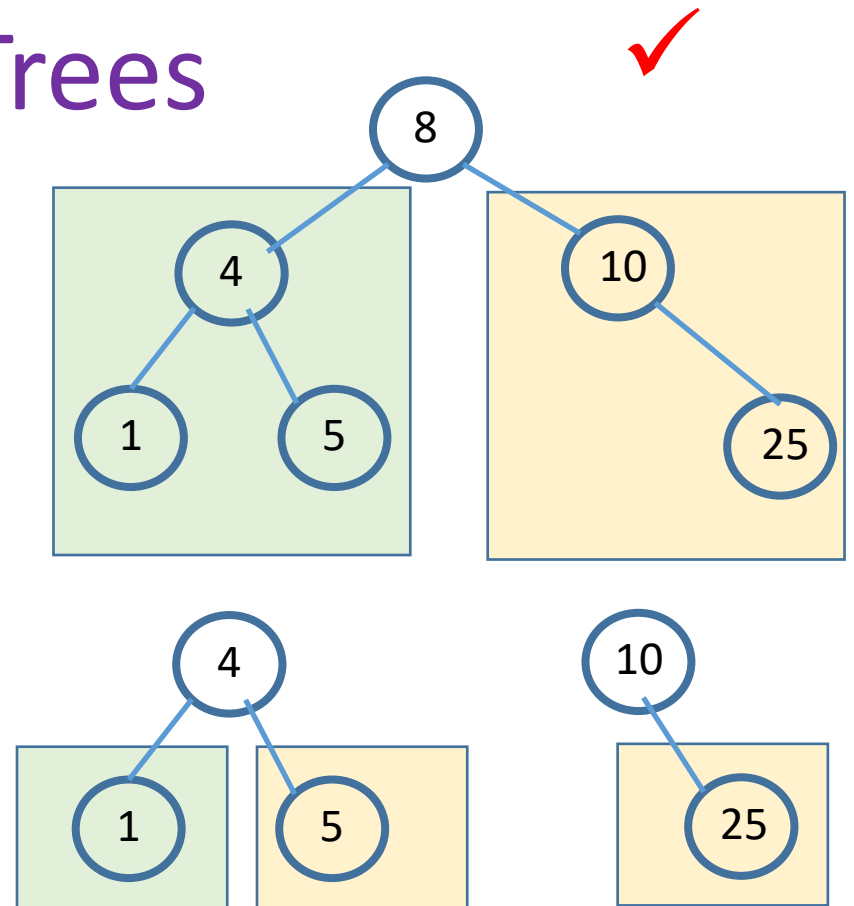
- Let x be a node in a BST.
- If y is a node in the left subtree of x , then $y.\text{key} \leq x.\text{key}$.
- If y is a node in the right subtree of x , then $y.\text{key} \geq x.\text{key}$.



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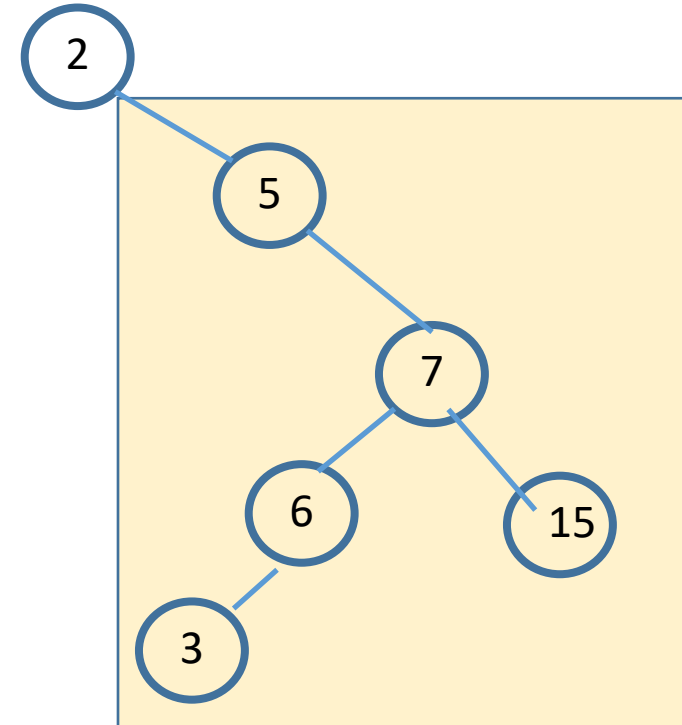
- Let x be a node in a BST.
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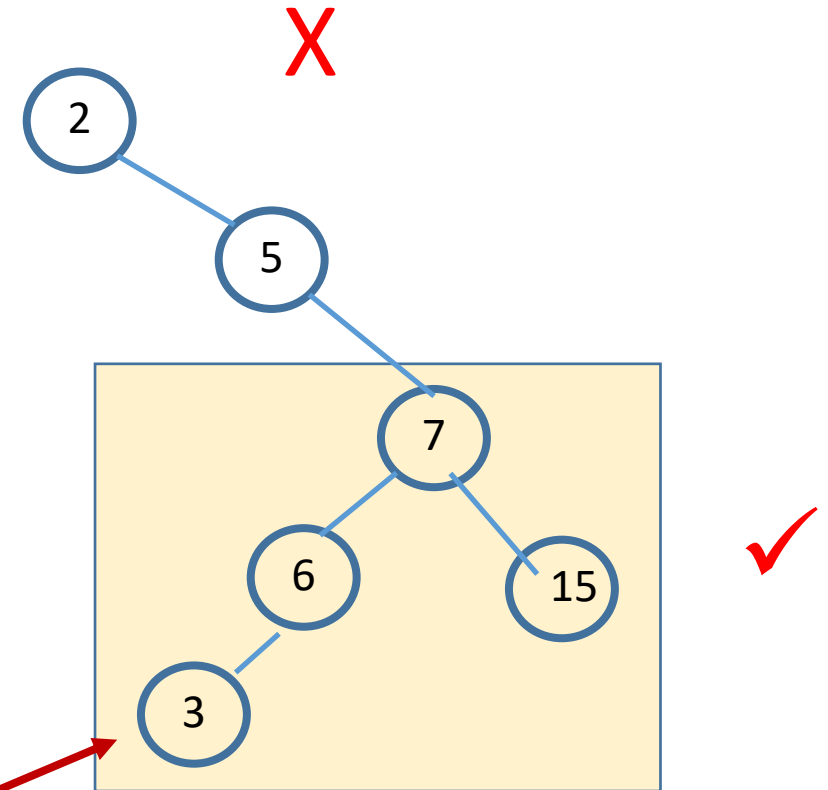
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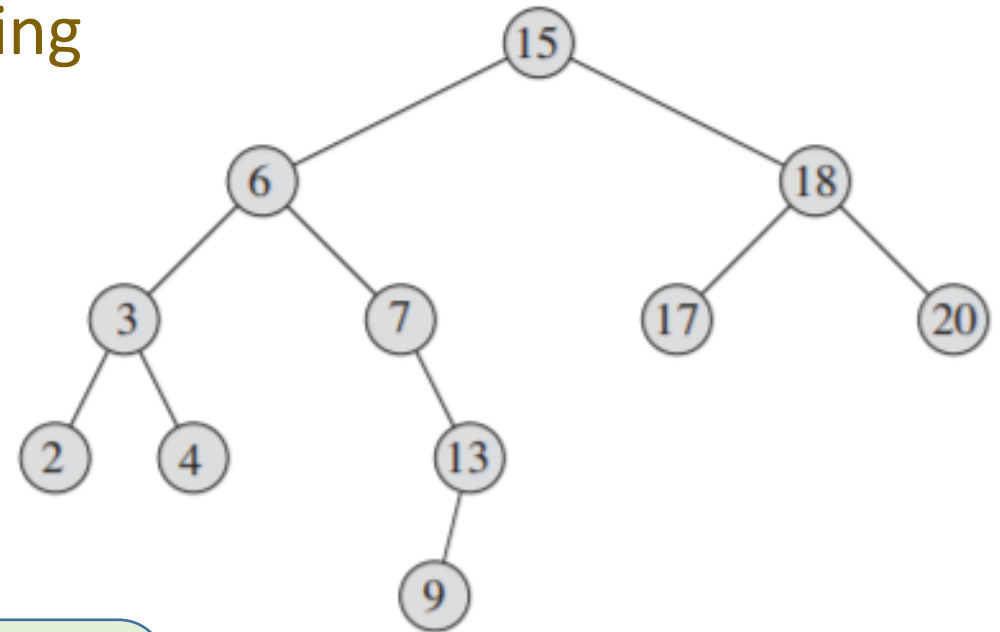
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3 is not
greater
than 5

Binary Search Trees: Inorder Traversal

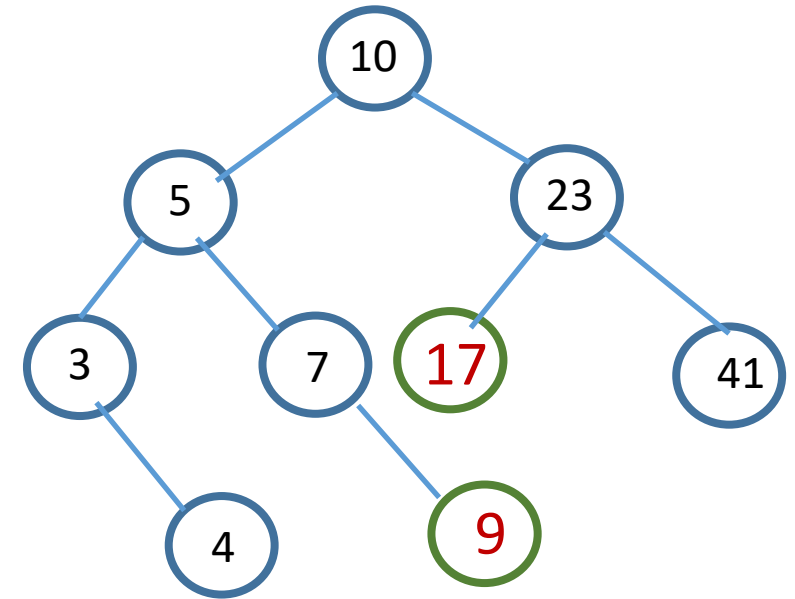
- An inorder traversal of a binary search tree always results in the nodes being visited in ascending order:



2, 3, 4, 6, 7, 9, 13, 15, 17, 18, 20

Binary Search Trees: Insertion

➤ Where to insert 9 and 17?

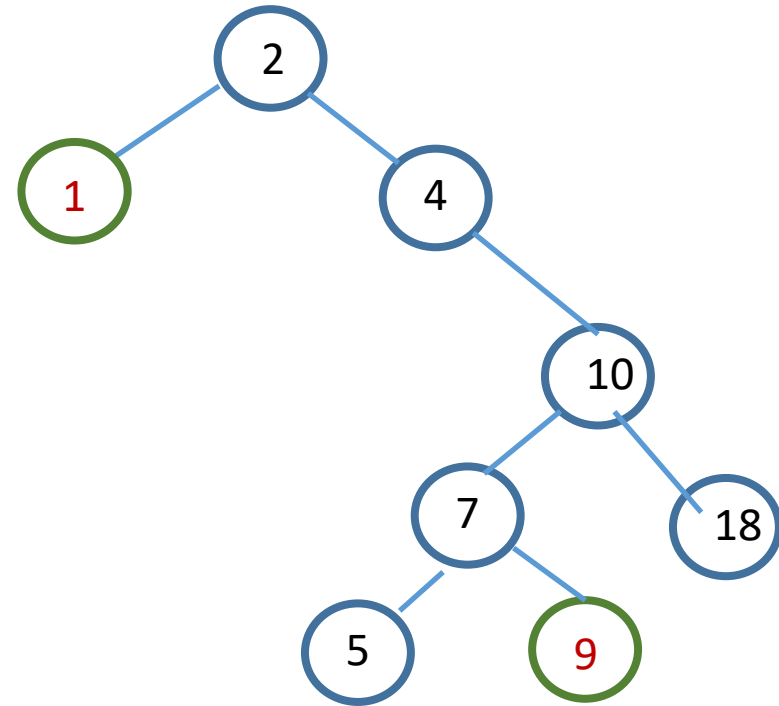


➤ Insert 9 as the right child of 7.

➤ Insert 17 as the left child of 23.

Binary Search Trees: Insertion

➤ Where to insert 1 and 9?



Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

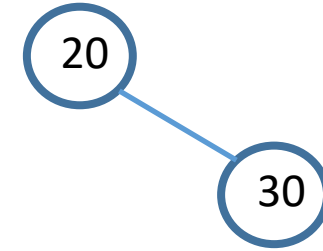
Insert 20:

Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 30:

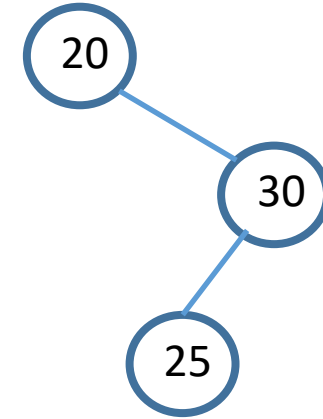


Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 25:

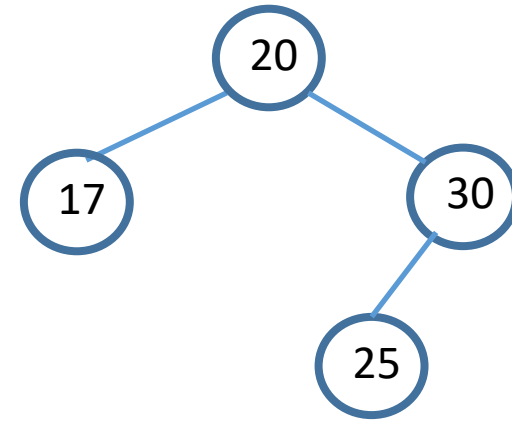


Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 17:

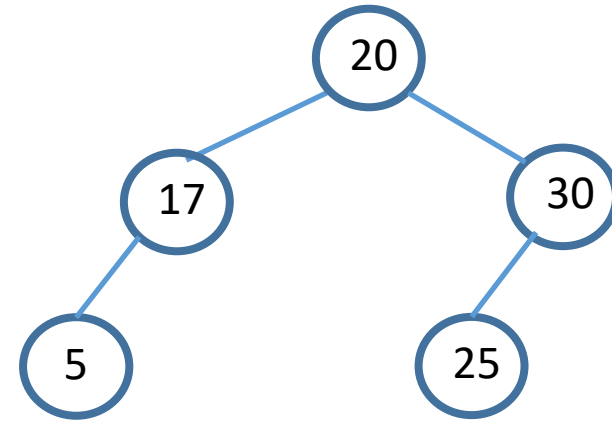


Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 5:

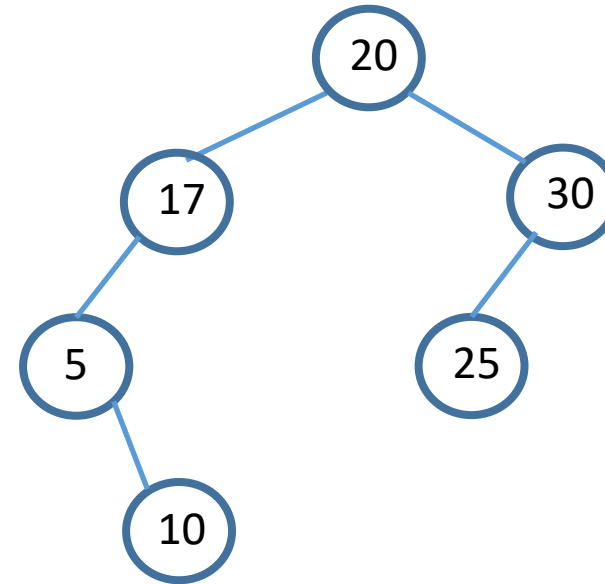


Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 10:

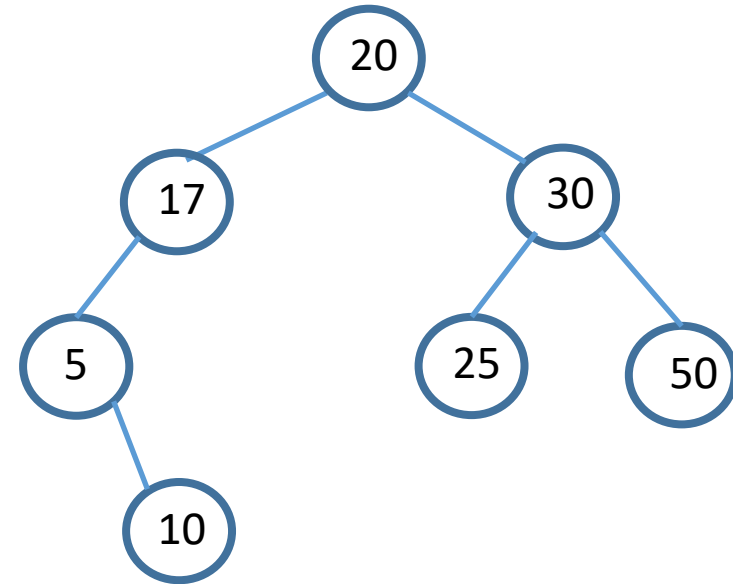


Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 50:

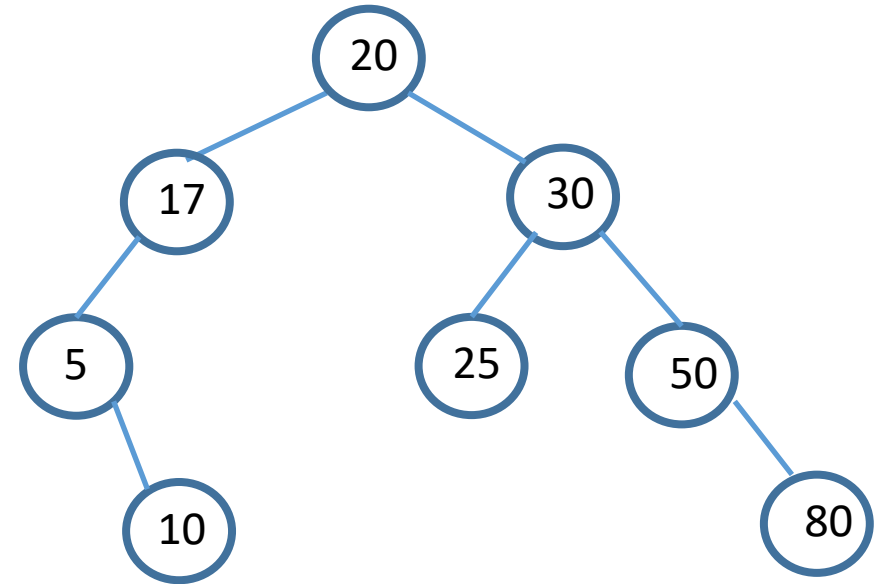


Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 80:

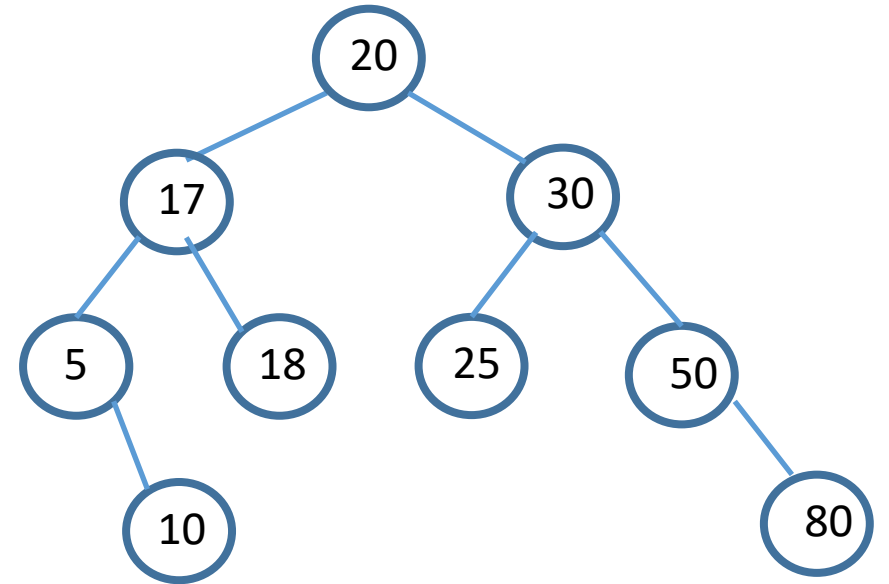


Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 18:



Binary Search Trees: Insertion

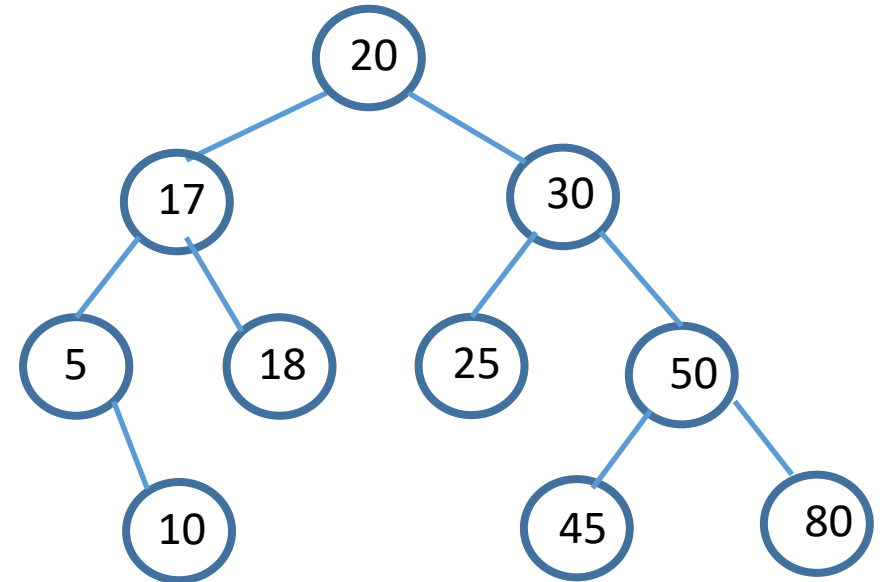
- Draw the BST obtained by inserting the following keys in the order given:

20, 30, 25, 17, 5, 10, 50, 80, 18, 45

Insert 45:

Inorder Traversal:

5, 10, 17, 18, 20, 25, 30, 45, 50, 80



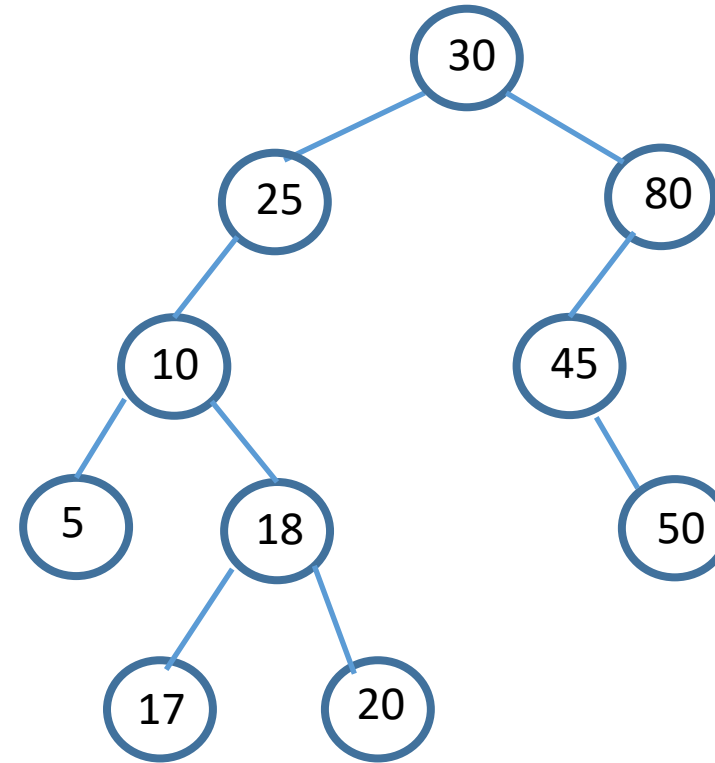
Binary Search Trees: Insertion

- Draw the BST obtained by inserting the following keys in the order given:

30, 25, 80, 45, 10, 18, 20, 5, 50, 17

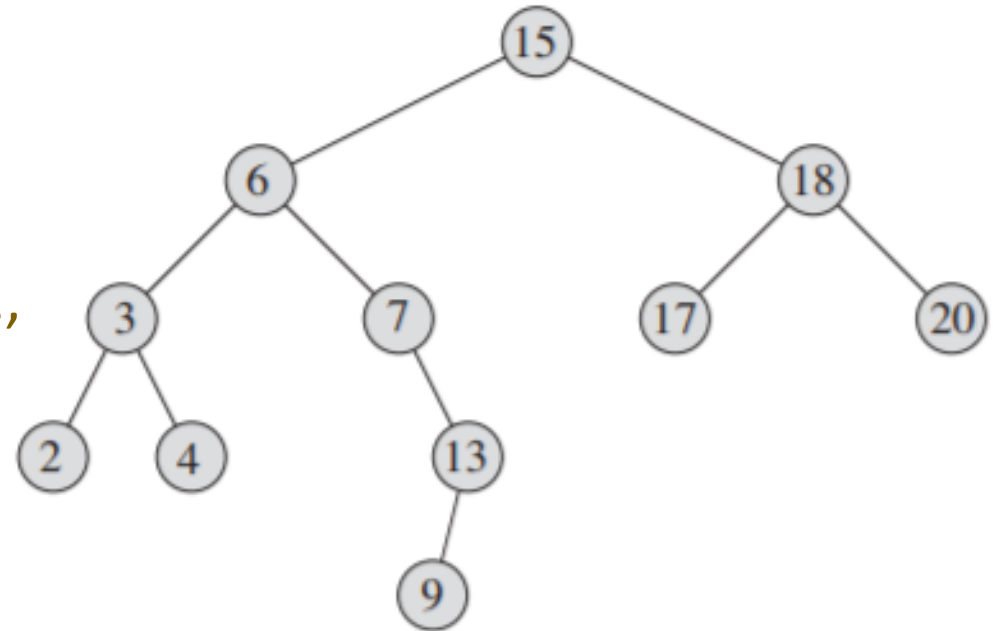
Inorder Traversal:

5, 10, 17, 18, 20, 25, 30, 45, 50, 80



Binary Search Trees: Insertion

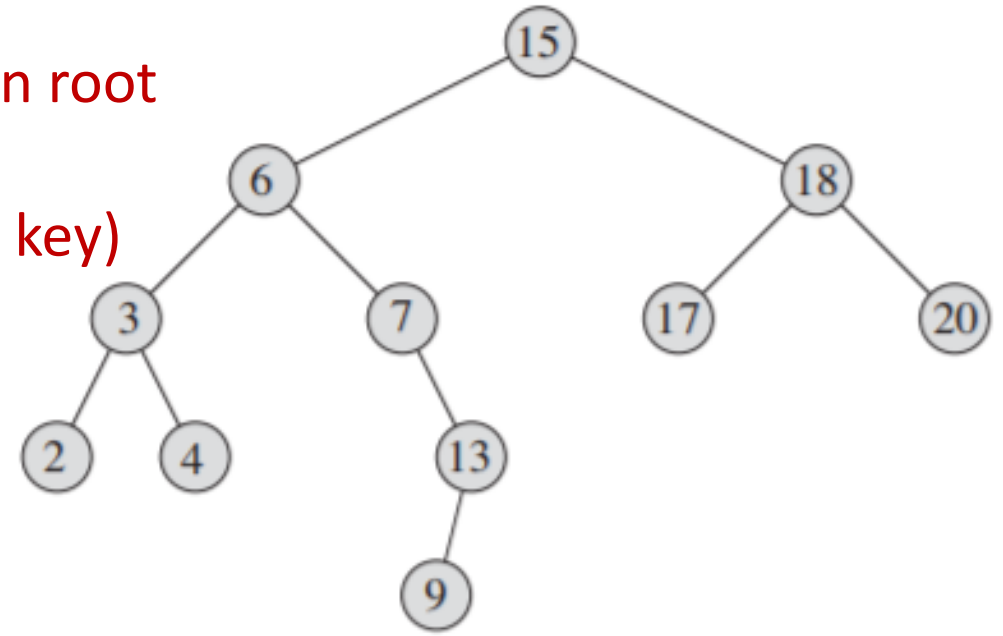
- Case 0: Tree is empty – insert node in empty tree (**root is the address of this node**)
- Case 1: If $\text{data} < \text{root} \rightarrow \text{data}$ – **go left**
- Case 2: If $\text{data} > \text{root} \rightarrow \text{data}$ – **go right**
- Repeat (1) and (2) until position found (i.e., parent with empty left or right subtree)
- Create BTreeNode and connect to parent.



Binary Search Trees: Search (Return Node Where Found)

Cases for `contains (BTNode * root, int key)`:

- The root of binary tree is empty: `return NULL (or root)`
- The root of the binary tree contains key: `return root`
- If `key < root->data`: `return contains(root->left, key)`
- Otherwise: `return contains(root->right, key)`



Binary Search Trees: Finding the Nodes with the Minimum and Maximum Keys

- `BTNode * minimum (BTNode * root)`
- `BTNode * maximum (BTNode * root)`

