

Model Building

Lecture 14

STA 371G

There is a Primary Care Physician Shortage in Texas!





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What might explain this? There are many potential predictors!

- Small counties
- Poverty
- Health insurance

- Unemployment
- Large rural areas
- Something else?



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- However, figuring out what variables to use to predict the number of physicians that a county has, is a critical portion of the analysis in this case.
- This type of analysis is an exploratory study.

An exploratory study of the Texas physician shortage

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An exploratory study of the Texas physician shortage

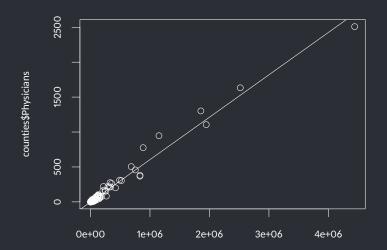
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- Multicollinearity is much more likely in an exploratory study than in an experiment or a confirmatory study.
- Exploratory studies require the most in terms of model selection. Automated tools are helpful, but judgement is still needed!

Population as a predictor of number of physicians

```
plot(counties$Population, counties$Physicians)
popmodel <- lm(counties$Physicians ~ counties$Population)
abline(popmodel)</pre>
```



Transform and Subset the data



The 10 potential x variables

- LandArea: Area in square miles
- PctRural: Percentage rural land
- MedianIncome: Median household income
- Population: Population
- PctUnder18: Percent children
- PctOver65: Percent seniors
- PctPoverty: Percent below the poverty line
- PctUninsured: Percent without health insurance
- PctSomeCollege: Percent with some higher education
- PctUnemployed: Percent unemployed

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- If there are n candidate predictor variables, there are 2ⁿ possible models, and we need to look at ALL of them to be sure that we have found the best model.
- This is where R's automated model building tools help.



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- All model measuring criteria try to find a balance between the predictive power of the model and the number of variables.
- No method is ideal in all situations, so it is generally best to use multiple methods and compare the results.

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- AIC (Akaike's Information Criterion) and the very similar BIC (your reading calls it SBC) are other widely used criteria.
- There more, but we won't go into them.

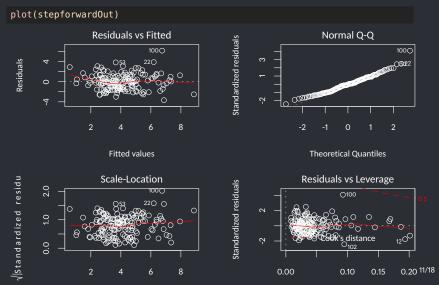
Stepping forwards

The step() function uses the AIC criterion to compare models. You must build the null and the full models first.

```
null <- lm(PhysiciansPer10000~1. data=mcounties)</pre>
full <- lm(PhysiciansPer10000 ~ LandArea + PctRural + MedianIncome
                             + Population + PctUnder18 + PctOver65
                             + PctPovertv + PctUninsured
                             + PctSomeCollege + PctUnemployed,
                             data=mcounties)
stepforwardOut <- step(null, scope=list(lower=null, upper=full),</pre>
                            direction ="forward")
Start: AIC=238.65
PhysiciansPer10000 ~ 1
                Df Sum of Sa RSS
                                       ATC
+ PctSomeCollege 1 150.125 558.67 203.28
+ Population 1 132.562 576.23 208.14
+ PctRural 1 119.850 588.94 211.57
+ PctUnemployed 1 32.121 676.67 233.37
+ MedianIncome
                   30.413 678.38 233.76
```

Check the LINE assumptions

model stepforwardOut's residuals look ok



Examine stepforwardOut

```
# check the summary
#summary(stepforwardOut)
# Check stepForwardOut for multicollinearity
vif(stepforwardOut)
PctSomeCollege
                     PctRural
                                   Pct0ver65
                                                  Population
                                                              PctUnemployed
      1.541539
                     1.911623
                                    1.776352
                                                    1.843085
                                                                   1.125032
  PctUninsured
      1.029993
```



Stepping backwards and both ways

This model looks pretty good, but is it the best? You can also step backward or on both directions.

```
stepbackwardOut <- step(null, scope=list(lower=null, upper=full),</pre>
                       direction ="backward")
Start: AIC=238.65
PhysiciansPer10000 ~ 1
stepbothOut <- step(null, scope=list(lower=null, upper=full),</pre>
                   direction ="both")
Start: ATC=238.65
PhysiciansPer10000 ~ 1
                Df Sum of Sa RSS
                                       ATC
+ PctSomeCollege 1 150.125 558.67 203.28
+ Population
                 1 132,562 576,23 208,14
+ PctRural
          1 119.850 588.9<u>4 211.57</u>
+ PctUnemployed 1 32.121 676.67 233.37
+ MedianIncome
                 1 30.413 678.38 233.76
+ PctPovertv
                   14.337 694.45 237.44
                             708 79 238 65
<none>
```

Best Subsets Regression

Step only uses AIC criterion for comparing models. regsubsets is more flexible about criteria and calculates all possible subsets.

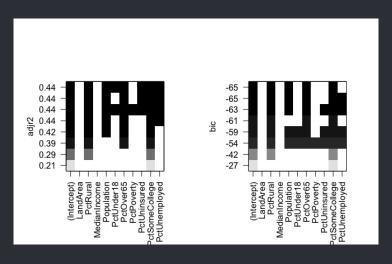
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```
# Set the plot window up so you can examine the output side by side
layout(matrix(1:2, ncol=2))
#plot(regsubsets.out, scale="adjr2") # use adjusted R^2
#plot(regsubsets.out, scale="bic") # use SBC

# Don't forget to reset the plot window!
layout(matrix(1:1, ncol=1))
```

Look at this interesting plot



Black indicates that a variable is included in the model, while white indicates that it is not.

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- Find the middle ground between an underspecified model and extraneous variables.
- Fine tune the model to get a correctly specified model; you may need to transform predictors and/or add interactions.
- Think about logical reasons why certain predictors might be useful, don't just focus on p-values.

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- Otherwise, you can select the ones that happen to fit the data the best and essentially create a spurious correlation!
- Rember to check for multicolliearity and the LINE assumptions!