

Model Building

Lecture 14

STA 371G

There is a Primary Care Physician Shortage in Texas!





There is a Primary Care Physician Shortage in Texas!



What might explain this? There are many potential predictors!

- Small counties
- Poverty
- Health insurance smallest population

- Unemployment
- Large rural areas
- Something else?



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- This type of analysis is an exploratory study.

An exploratory study of the Texas physician shortage

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An exploratory study of the Texas physician shortage

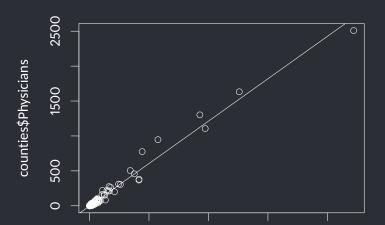
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- Multicollinearity is much more likely in an exploratory study than in an experiment or a confirmatory study.
- Exploratory studies require the most in terms of model selection. Automated tools are helpful, but judgement is still needed!

Population as a predictor of number of physicians

plot(counties\$Population, counties\$Physicians)
popmodel <- lm(counties\$Physicians ~ counties\$Population)
abline(popmodel)</pre>



Transform and Subset the data

```
# Transform Physians
counties$PhysiciansPer10000 <-
     (counties$Physicians/counties$Population)*10000
# Remove the very small and very large counties
mcounties <- counties[counties$Population < 500000 &
                      counties$Population > 10000,]
# Show medium counties with no physicians
mcounties[mcounties$Physicians == 0, c(1,5,12)]
      X MedianIncome PctUnemployed
                               3.5
157 157
               51481
                               5.5
159 159
               35069
```

The 10 potential x variables

- LandArea: Area in quare miles
- PctRural: Percentage rural land
- MedianIncome: Median household income
- Population: Population
- PctUnder18: Percent children
- PctOver65: Percent seniors
- PctPoverty: Percent below the poverty line
- PctUninsured: Percent without health insurance
- PctSomeCollege: Percent with some higher education
- PctUnemployed: Percent unemployed

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- If there are n candidate predictor variables, there are 2ⁿ
 possible models, and we need to look at ALL of them to be sure
 that we have found the best model.
- This is where R's automated model building tools help.

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- But R² is not good for comparing models with different numbers of variables because it tends to increase a little bit with each additional variable just due to randomness.
- Adjusted-R² is better because it multiplies R² by a penalty that depends on the number of variables, but the penalty is somewhat arbitrary and increases as the number of variables increases.

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- No method is ideal in all situations, so it is generally best to use multiple methods and look at the results.
- AIC (Akaike's Information Criterion) and the very similar BIC (your reading calls it SBC) are other widely used criterion that often gives different results than Adjusted-R².



Stepping forwards

The step() function uses the AIC criterion to compare models. You must build the null and the full models first.

```
PhysiciansPer10000 ~ 1
```

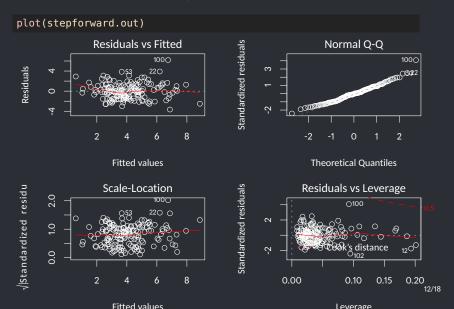
Start: AIC=238.65

Stepping backwards and both ways

You can also step backward or on both directions

```
stepbackward.out <-
    step(null, scope=list(lower=null, upper=full),
         direction ="backward")
Start: AIC=238.65
PhysiciansPer10000 ~ 1
stepboth.out <-
    step(null, scope=list(lower=null, upper=full),
         direction ="both")
Start: AIC=238.65
PhysiciansPer10000 ~ 1
```

Check the LINE assumptions



Check for multicollinearity

This model looks pretty good, but is it the best that can be done?

```
# Check the model for multicollinearity

vif(stepforward.out)

PctSomeCollege PctRural PctOver65 Population
    1.541539    1.911623    1.776352    1.843085
    PctUninsured
    1.029993
```

Best Subsets Regression

Step only uses AIC criterion for comparing models. regsubsets is more flexible about criteria and calculates all possible subsets.

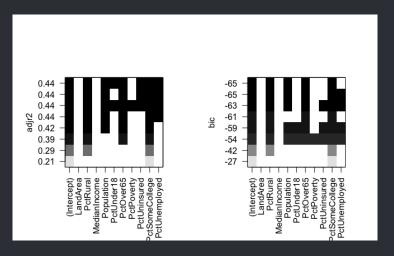
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```
# Set the plot window up so you can examine the output side
layout(matrix(1:2, ncol=2))
#plot(regsubsets.out, scale="adjr2") # use adjusted R^2
#plot(regsubsets.out, scale="bic") # use SBC

# Don't forget to reset the plot window!
layout(matrix(1:1, ncol=1))
```

Look at this interesting plot



Black indicates that a variable is included in the model, while white indicates that it is not.

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- Find the middle ground between an underspecified model and extraneous variables.
- Fine tune the model to get a correctly specified model you may need to transform predictors and/or add interactions.
- Think about logical reasons why certain predictors might be useful, don't just focus on p-values.

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- Otherwise, you can select the ones that happen to fit the data the best and essentially create a spurious correlation!
- Rember to check for multicolliearity and the LINE assumptions!