

# **Model Building**

**Lecture 14** 

**STA 371G** 

#### There is a Primary Care Physician Shortage in Texas!





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What might explain this? There are many potential predictors!

- Small counties
- Poverty
- Health insurance

- Unemployment
- Large rural areas
- Something else?



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- However, selecting the explanatory variables, or figuring out what predicts the number of physicians that a county has, is a large part of the analysis in this case.
- This type of analysis is an exploratory study.

# An exploratory study of the Texas physician shortage

 Exploratory studies are observational studies, in that the variables are observed rather than controlled, which is different from an experiment.

# An exploratory study of the Texas physician shortage

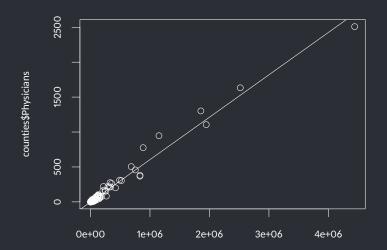
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- Exploratory studies are observational studies, in that the variables are observed rather than controlled, which is different from an experiment.
- Multicollinearity is much more likely in an exploratory study than in an experiment or a confirmatory study.
- Exploratory studies require the most in terms of model selection. Automated tools are helpful, but judgement is still needed!

# Population as a predictor of number of physicians

```
plot(counties$Population, counties$Physicians)
popmodel <- lm(counties$Physicians ~ counties$Population)
abline(popmodel)</pre>
```



#### Transform and Subset the data



#### The 10 potential x variables

- LandArea: Area in quare miles
- PctRural: Percentage rural land
- MedianIncome: Median household income
- Population: Population
- PctUnder18: Percent children
- PctOver65: Percent seniors
- PctPoverty: Percent below the poverty line
- PctUninsured: Percent without health insurance
- PctSomeCollege: Percent with some higher education
- PctUnemployed: Percent unemployed

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- If there are n candidate predictor variables, there are 2<sup>n</sup> possible models, and we need to look at ALL of them to be sure that we have found the best model.
- This is where R's automated model building tools help.

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- But R<sup>2</sup> is not good for comparing models with different numbers of variables because
  it tends to increase a little bit with each additional variable just due to randomness.
- Adjusted-R<sup>2</sup> is better because it multiplies R<sup>2</sup> by a penalty that depends on the number of variables, but the penalty is somewhat arbitrary and increases as the number of variables increases.

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- No method is ideal in all situations, so it is generally best to use multiple methods and look at the results.
- AIC (Akaike's Information Criterion) and the very similar BIC (your reading calls it SBC) are other widely used criterion that often gives different results than Adjusted-R<sup>2</sup>.



# Stepping forwards

The step() function uses the AIC criterion to compare models. You must build the null and the full models first.

```
null <- lm(PhysiciansPer10000~1. data=mcounties)</pre>
full <- lm(PhysiciansPer10000 ~ LandArea + PctRural + MedianIncome
                             + Population + PctUnder18 + PctOver65
                             + PctPoverty + PctUninsured
                             + PctSomeCollege + PctUnemployed.
                             data=mcounties)
stepforwardOut <- step(null, scope=list(lower=null, upper=full),</pre>
                            direction ="forward")
Start: ATC=238.65
PhysiciansPer10000 ~ 1
                Df Sum of Sq RSS
                                      AIC
+ PctSomeCollege 1 150.125 558.67 203.28
+ Population
                 1 132,562 576,23 208,14
+ PctRural 1 119.850 588.94 211.57
+ PctUnemployed 1 32.121 676.67 233.37
+ MedianIncome 1 30.413 678.38 233.76
+ PctPovertv 1 14.337 694.45 237.44
                             708 79 238 65
<none>
```

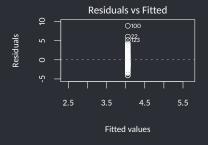
### Stepping backwards and both ways

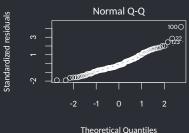
You can also step backward or on both directions

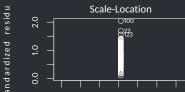
```
stepbackwardOut<- step(null, scope=list(lower=null, upper=full),</pre>
                  direction ="backward")
Start: ATC=238.65
PhysiciansPer10000 ~ 1
stepboth.out <-
                  step(null, scope=list(lower=null, upper=full),
                  direction = "both")
Start: ATC=238.65
PhysiciansPer10000 ~ 1
                Df Sum of Sa
                                RSS
                                       AIC
+ PctSomeCollege
                   150.125 558.67 203.28
+ Population
                   132,562,576,23,208,14
+ PctRural
                 1 119.850 588.94 211.57
+ PctUnemployed
                 1 32.121 676.67 233.37
+ MedianIncome
                   30.413 678.38 233.76
+ PctPovertv
                      14.337 694.45 237.44
                             708.79 238.65
<none>
+ PctUnder18
                    2.503 706.29 240.09
+ LandArea
                       2.260 706.53 240.15
```

### Check the LINE assumptions









#### Check for multicollinearity

This model looks pretty good, but is it the best that can be done?

#### **Best Subsets Regression**

Step only uses AIC criterion for comparing models. regsubsets is more flexible about criteria and calculates all possible subsets.

```
regsubsets.out <- regsubsets(PhysiciansPer10000 ~ LandArea + PctRural
+ MedianIncome + Population + PctUnder18
+ PctOver65 + PctPoverty + PctUninsured
+ PctSomeCollege + PctUnemployed, data=mcounties)
```

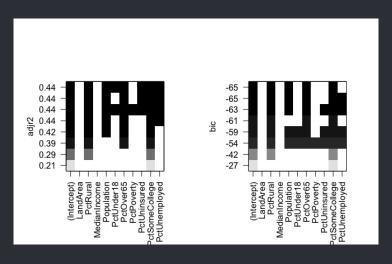
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```
# Set the plot window up so you can examine the output side by side
layout(matrix(1:2, ncol=2))
#plot(regsubsets.out, scale="adjr2") # use adjusted R^2
#plot(regsubsets.out, scale="bic") # use SBC

# Don't forget to reset the plot window!
layout(matrix(1:1, ncol=1))
```

### Look at this interesting plot



Black indicates that a variable is included in the model, while white indicates that it is not.

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- Find the middle ground between an underspecified model and extraneous variables.
- Fine tune the model to get a correctly specified model you may need to transform predictors and/or add interactions.
- Think about logical reasons why certain predictors might be useful, don't just focus on p-values.

#### Be careful of getting to crazy

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- A general guideline is that you should not even consider more than one variable for every 10 to 15 cases in your dataset.
- Otherwise, you can select the ones that happen to fit the data the best and essentially create a spurious correlation!
- Rember to check for multicolliearity and the LINE assumptions!