

# **Diagnostics & Transformations 2**

**Lecture 13** 

**STA 371G** 

#### Newly hired manager salaries



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- Salary (response)
- Manager Rating
- Years of Experience

- NUmber of years since graduation
- Origin (internal or external hire)

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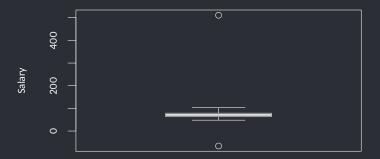
It is almost always necessary to explore and clean the data before doing the modeling

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boxplot(manager\$Salary, ylab='Salary')



There is a negative entry, and a very large one. We need to investigate these.

```
manager[manager$Salary>200,]
# A tibble: 15
 Salary MngrRating YearsExp YrsSinceGrad Origin
  <int>
            <dbl>
                    <int>
                             <int> <chr>
 511
             6.1
                                   2 Internal
   manager[manager$Salary<0,]</pre>
# A tibble: 15
 Salary MngrRating YearsExp YrsSinceGrad
                                      0rigin
  <int>
            <dbl>
                    <int>
                            <int> <chr>
1 -66
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1 -66
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```

These are probably just incorrect entries.

```
manager[manager$Salary>200.1
# A tibble: 15
 Salary MngrRating YearsExp YrsSinceGrad
                                         0rigin
  <int>
             <dbl>
                     <int>
                               <int> <chr>
              6.1
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             <dbl>
                     <int>
                                 <int>
  <int>
                                          <chr>
1 -66
              5.7
                                     2 Internal
```

These are probably just incorrect entries.

Try to correct the data whenever you can. If not possible, we will omit them.

mclean <- manager[manager\$Salary>0 & manager\$Salary<200,]</pre>



mclean <- manager[manager\$Salary>0 & manager\$Salary<200,]</pre>

Select the subset of the data where the salary is between 0 and 200K.



boxplot(mclean\$YearsExp, ylab='Years of Experience')



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mclean\$YearsExp[mclean\$YearsExp==99] <- NA</pre>

Now, what? We have missing entries our data! Great.

Let's see if we have other missing data.

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```
mclean[!complete.cases(mclean),]
# A tibble: 4 5
  Salary MngrRating YearsExp YrsSinceGrad
                                            Origin
   <int>
              <dbl>
                       <int>
                                    <int>
                                             <chr>
      75
                 NA
                                        8 Internal
      81
                 NA
                                        9 External
                5.9
                                        7 External
      73
                          NA
4
                8.0
      49
                                              <NA>
```

Let's see if we have other missing data.

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      73
                5.9
                          NA
                                         7 External
      49
                8.0
                                               <NA>
```

This should not come a surprise, because it is very common to have missing entries in your data

<sup>\*</sup>If you are not seeing the last entry, it is because na.strings is set to NA (it should be empty in RStudio, and na.strings=" should be used while in read.csv command).

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Let's try to fill in some estimates.

What should we replace the "NA"s in the Manager Rating and Years of Experience columns with?

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The simplest way would be to use the averages in the respective columns.

```
average_MngrRating <- mean(mclean$MngrRating, na.rm=TRUE)
mclean$MngrRating[is.na(mclean$MngrRating)] <- average_MngrRating
average_YearsExp <- mean(mclean$YearsExp, na.rm=TRUE)
mclean$YearsExp[is.na(mclean$YearsExp)] <- average_YearsExp</pre>
```

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mclean$MngrRating[is.na(mclean$MngrRating)] <- average_MngrRating
average_YearsExp <- mean(mclean$YearsExp, na.rm=TRUE)
mclean$YearsExp[is.na(mclean$YearsExp)] <- average_YearsExp</pre>
```

A smarter and more advanced way is to predict, e.g., what the Manager Rating would be for a person with \$75K salary, 8 years of experience and who is an internal hire.

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mclean <- na.omit(mclean)</pre>

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There are also ways of predicting the missing entries in a categorical variable.

Or we could have treated the missing entries as a seperate level (e.g. "Unknown").

#### Important things to consider:

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- Making predictions for missing data based on available data enforces the already existing relationships between variables, therefore impacts the standard error.
- If a lot of data is missing (e.g. more than 5%) for a particular variable, you may have to discard the whole column.

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#### It is a problem, because:

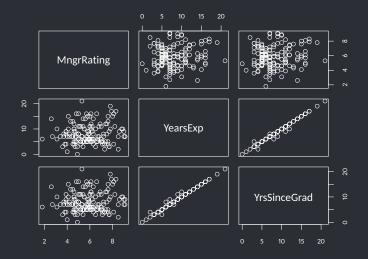
 Any conclusions based on the p-values, coeffients and confidence intervals of the highly correlated variables will be unreliable.

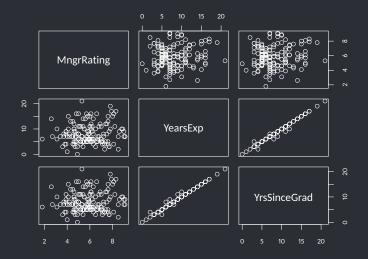
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#### It is a problem, because:

- Any conclusions based on the p-values, coeffients and confidence intervals of the highly correlated variables will be unreliable.
- These statistics will not be stable: adding new data or predictors to the model could drastically change them.

```
model<- lm(Salary ~ MngrRating + YearsExp</pre>
                  + YrsSinceGrad + Origin, data=mclean)
  summary(model)
Call:
lm(formula = Salary ~ MngrRating + YearsExp + YrsSinceGrad +
   Origin. data = mclean)
Residuals:
     Min
             10 Median
                               30
                                      Max
-19.7766 -4.2842 -0.2906 3.3266 28.2773
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          2.6071 20.771 < 2e-16 ***
(Intercept)
            54.1521
MngrRating 4.5147
                          0.3997 11.296 < 2e-16 ***
YearsExp -1.5262 1.3790 -1.107 0.270203
YrsSinceGrad 0.7692 1.3833 0.556 0.578976
OriginInternal -4.7314
                          1.3878 -3.409 0.000838 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 6.838 on 149 degrees of freedom
Multiple R-squared: 0.6065, Adjusted R-squared: 0.596
F-statistic: 57.42 on 4 and 149 DF, p-value: < 2.2e-16
```





If you check the correlation between the two:

cor(mclean\$YearsExp,mclean\$YrsSinceGrad)

[1] 0.9947616

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A better way to check multicollinearity:

```
library(car)
vif(model)

MngrRating YearsExp YrsSinceGrad Origin
1.136002 95.954255 97.011260 1.540448
```

Drop one of the predictors that has a VIF higher than 5.

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library(car)
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MngrRating YearsExp YrsSinceGrad Origin
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```

Drop one of the predictors that has a VIF higher than 5.

Remember: Multicollinearity could exist between more than two predictors (e.g. having seperate columns with binary values for Spring, Summer, Autumn, Winter).

```
model2<- lm(Salary ~ MngrRating + YearsExp</pre>
                   + Origin, data=mclean)
  summary(model2)
Call:
lm(formula = Salary ~ MngrRating + YearsExp + Origin, data = mclean)
Residuals:
              10 Median
    Min
                               30
                                       Max
-19.8115 -4.3474 -0.3964 3.3358 28.1801
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          2.5999 20.812 < 2e-16 ***
(Intercept)
            54.1080
                          0.3977 11.394 < 2e-16 ***
MngrRating
            ____ 4.5309
YearsExp -0.7651
                          0.1687 -4.534 1.18e-05 ***
OriginInternal -4.6467
                          1.3762 -3.376 0.000935 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 6.823 on 150 degrees of freedom
Multiple R-squared: 0.6057.Adjusted R-squared: 0.5978
F-statistic: 76.82 on 3 and 150 DF. p-value: < 2.2e-16
```

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• Look for a horizontal red line in the Residuals-Fitted plot for linearity.

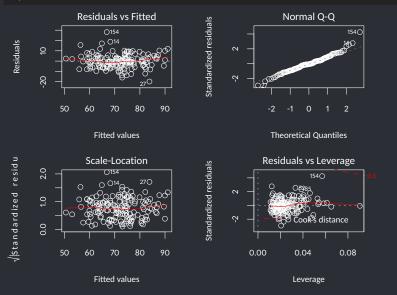
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- Look for a horizontal red line in the Residuals-Fitted plot for linearity.
- Look for a horizontal red line in the Scale-Location plot for equal variance.
- Look for a straight line in the Normal Q-Q plot for normality.

# par(mfrow=c(2,2)) # Change the panel layout to 2 x 2 plot(model2)



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We can display the indices of all of the outliers among the residuals.

```
boxplot(resid(model2))$out

14 27 52 85 154

18.76901 -19.81152 17.14133 15.66079 28.18007
```

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Basically, the model is not able to explain these cases very well.

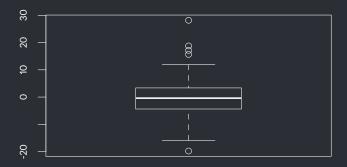
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Basically, the model is not able to explain these cases very well. Let's also see them on the

plot.

boxplot(resid(model2))



Someone with only 1 year of experience and poor rating is hired as manager at \$95K!

Someone with only 1 year of experience and poor rating is hired as manager at \$95K!

If you decide that this is an anomaly (e.g. CEO's son promoted!) that you don't want to include in your analysis, omit that row and report it in your conclusions.

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Look for the cases on the upper/lower right corners (beyond the dashed curves).