

# Package ‘GPA’

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**Title** GPA (Genetic analysis incorporating Pleiotropy and Annotation)

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ggrepel, plyr, vegan, DT, shiny, shinyBS

**Suggests** gpaExample

**LinkingTo** Rcpp

## Description

This package provides functions for fitting GPA, a statistical framework to prioritize GWAS results by integrating pleiotropy information and annotation data. In addition, it also includes ShinyGPA, an interactive visualization toolkit to investigate pleiotropic architecture.

**License** GPL (>= 2)

**URL** <http://dongjunchung.github.io/GPA/>

**NeedsCompilation** yes

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GPA-package

*GPA (Genetic analysis incorporating Pleiotropy and Annotation)***Description**

This package provides functions for fitting GPA, a statistical approach to prioritizing GWAS results by integrating pleiotropy information and annotation data, along with ShinyGPA, a visualization toolkit to investigate the pleiotropic architecture using GWAS results.

**Details**

Package:	GPA
Type:	Package
Version:	1.1.0
Date:	2017-06-30
License:	GPL (>= 2)
LazyLoad:	yes

This package contains a main class, GPA, which represents GPA model fit.

This package contains four main methods for the GPA framework (Chung et al., 2014), GPA, assoc, pTest, and aTest. GPA method fits the GPA model and assoc method implements association mapping. pTest and aTest methods implement hypothesis testing for pleiotropy and annotation enrichment, respectively.

This package contains two main methods for the ShinyGPA visualization toolkit (Kortemeier et al., 2017), fitAll and shinyGPA. fitAll function generates all the intermediate results needed to run shinyGPA. shinyGPA opens the ShinyGPA interface, which takes the results generated from fitAll as input.

**Author(s)**

Dongjun Chung, Emma Kortemeier

Maintainer: Dongjun Chung <chungd@musc.edu>

**References**

Chung D\*, Yang C\*, Li C, Gelernter J, and Zhao H (2014), "GPA: A statistical approach to prioritizing GWAS results by integrating pleiotropy information and annotation data," PLoS Genetics, 10: e1004787. (\* joint first authors)

Kortemeier E, Ramos PS, Hunt KJ, Kim HJ, Hardiman G, and Chung D (2017), "ShinyGPA: An interactive and dynamic visualization toolkit for genetic studies."

**See Also**

[GPA](#), [assoc](#), [pTest](#), [aTest](#), [GPA](#), [fitAll](#), [shinyGPA](#).

**Examples**

```

## Not run:
library(GPA)

# simulation setting

nBin <- 20000
pi1 <- 0.2
common <- 0.5
betaAlpha <- c( 0.6, 0.6 )
annP <- c( 0.2, 0.4, 0.4, 0.4 )
seed <- 12345

# simulation setting

nCommon <- round( pi1 * common * nBin )
nUniq <- round( pi1 * ( 1 - common ) * nBin )
nBg <- nBin - 2 * nUniq - nCommon

# M * K matrix of GWAS p-value

set.seed( seed )

pvec1 <- c( rbeta( nCommon, betaAlpha[1], 1 ), rbeta( nUniq, betaAlpha[1], 1 ),
  runif( nUniq ), runif( nBg ) )
pvec2 <- c( rbeta( nCommon, betaAlpha[2], 1 ), runif( nUniq ),
  rbeta( nUniq, betaAlpha[2], 1 ), runif( nBg ) )
pmat <- cbind( pvec1, pvec2 )

# M * D matrix of annotation

ann <- c(
  sample( c(1,0), nCommon, replace=TRUE, prob = c( annP[4], 1 - annP[4] ) ),
  sample( c(1,0), nUniq, replace=TRUE, prob = c( annP[2], 1 - annP[2] ) ),
  sample( c(1,0), nUniq, replace=TRUE, prob = c( annP[3], 1 - annP[3] ) ),
  sample( c(1,0), nBg, replace=TRUE, prob = c( annP[1], 1 - annP[1] ) ) )

# GPA without annotation data

fit.GPA.noAnn <- GPA( pmat, NULL )
cov.GPA.noAnn <- cov( fit.GPA.noAnn )

# GPA with annotation data

fit.GPA.wAnn <- GPA( pmat, ann )
cov.GPA.wAnn <- cov( fit.GPA.wAnn )

# GPA under pleiotropy H0

fit.GPA.pleiotropy.H0 <- GPA( pmat, NULL, pleiotropyH0=TRUE )

# association mapping

```

```

assoc.GPA.wAnn <- assoc( fit.GPA.wAnn, FDR=0.05, fdrControl="global" )

# hypothesis testing for pleiotropy

test.pleiotropy <- pTest( fit.GPA.noAnn, fit.GPA.pleiotropy.H0 )

# hypothesis testing for annotation enrichment

test.annotation <- aTest( fit.GPA.noAnn, fit.GPA.wAnn )

# simulator function

simulator <- function( risk.ind, nsnp=20000, alpha=0.6 ) {

  m <- length(risk.ind)

  p.sig <- rbeta( m, alpha, 1 )
  pvec <- runif(nsnp)
  pvec[ risk.ind ] <- p.sig

  return(pvec)
}

# run simulation

set.seed(12345)
nsnp <- 10000
alpha <- 0.4
pmat <- matrix( NA, nsnp, 5 )

pmat[,1] <- simulator( c(1:2000), nsnp=nsnp, alpha=alpha )
pmat[,2] <- simulator( c(501:2500), nsnp=nsnp, alpha=alpha )
pmat[,3] <- simulator( c(4001:6000), nsnp=nsnp, alpha=alpha )
pmat[,4] <- simulator( c(4501:7500), nsnp=nsnp, alpha=alpha )
pmat[,5] <- simulator( c(8001:10000), nsnp=nsnp, alpha=alpha )

# Fit GPA for all possible pairs of GWAS datasets

out <- fitAll( pmat )

# Run the ShinyGPA app using the output from fitAll()

shinyGPA(out)

## End(Not run)

```

## Description

Association mapping.

## Usage

```
assoc( object, ... )
## S4 method for signature 'GPA'
assoc( object, FDR=0.05, fdrControl="global", pattern=NULL )
```

## Arguments

object	GPA model fit.
FDR	FDR level.
fdrControl	Method to control FDR. Possible values are "global" (global FDR control) and "local" (local FDR control). Default is "global".
pattern	Pattern for association mapping. By default (i.e., pattern=NULL), assoc returns a binary matrix indicating association of SNPs for each phenotypes. If a pattern is specified, a corresponding binary vector is provided. See the details about how users can specify the pattern.
...	Other parameters to be passed through to generic assoc.

## Details

assoc uses the direct posterior probability approach of Newton et al. (2004) to control global FDR in association mapping.

Users can specify the pattern using 1 and \* in pattern argument, where 1 and \* indicate phenotypes of interest and phenotypes that are not of interest, respectively. For example, when there are three phenotypes, pattern="111" means a SNP associated with all of three phenotypes, while pattern="11\*" means a SNP associated with the first two phenotypes (i.e., association with the third phenotype is ignored (averaged out)).

## Value

If pattern=NULL, returns a binary matrix indicating association of SNPs for each phenotype, where its rows and columns match those of input p-value matrix for function GPA. Otherwise, returns a binary vector indicating association of SNPs for the phenotype combination of interest.

## Author(s)

Dongjun Chung

## References

Chung D\*, Yang C\*, Li C, Gelernter J, and Zhao H (2014), "GPA: A statistical approach to prioritizing GWAS results by integrating pleiotropy information and annotation data," *PLoS Genetics*, 10: e1004787. (\* joint first authors)

Newton MA, Noueiry A, Sarkar D, and Ahlquist P (2004), "Detecting differential gene expression with a semiparametric hierarchical mixture method," *Biostatistics*, Vol. 5, pp. 155-176.

**See Also**

[GPA](#), [GPA.](#)

**Examples**

```
## Not run:
fit.GPA.wAnn <- GPA( pmat, ann )
cov.GPA.wAnn <- cov( fit.GPA.wAnn )
assoc.GPA.wAnn <- assoc( fit.GPA.wAnn, FDR=0.05, fdrControl="global" )

## End(Not run)
```

---

aTest

*Hypothesis testing for annotation enrichment*


---

**Description**

Hypothesis testing for annotation enrichment.

**Usage**

```
aTest( fitWithoutAnn, fitWithAnn, vDigit=1000 )
```

**Arguments**

fitWithoutAnn	GPA model fit without using annotation data.
fitWithAnn	GPA model fit with using annotation data.
vDigit	Number of digits for reporting parameter estimates and standard errors. For example, setting it to 1000 means printing out values up to three digits below zero.

**Details**

aTest implements the hypothesis testing for annotation enrichment. It requires two GPA model fits, one fitted with using annotation data and one fitted without using annotation data, and evaluates annotation enrichment for risk-associated SNPs using the likelihood ratio test.

**Value**

Returns a list with components:

q	q estimates.
statistics	Statistics of the test for annotation enrichment.
pvalue	p-value of the test for annotation enrichment.

**Author(s)**

Dongjun Chung

## References

Chung D\*, Yang C\*, Li C, Gelernter J, and Zhao H (2014), "GPA: A statistical approach to prioritizing GWAS results by integrating pleiotropy information and annotation data," PLoS Genetics, 10: e1004787. (\* joint first authors)

## See Also

[pTest](#), [GPA](#), [GPA](#).

## Examples

```
## Not run:
# GPA without annotation data

fit.GPA.noAnn <- GPA( pmat, NULL )

# GPA with annotation data

fit.GPA.wAnn <- GPA( pmat, ann )

# hypothesis testing for annotation enrichment

test.annotation <- aTest( fit.GPA.noAnn, fit.GPA.wAnn )

## End(Not run)
```

---

fitAll

---

*Fit GPA model for all possible pairs of GWAS datasets*


---

## Description

Fit GPA model and the GPA model under H0 for all possible pairs of GWAS datasets.

## Usage

```
fitAll( pmat,
        maxIter=2000, stopping="relative", epsStopLL=1e-10,
        parallel=FALSE, nCore=8 )
```

## Arguments

pmat	p-value matrix from GWAS data, where row and column correspond to SNP and phenotype, respectively.
maxIter	Maximum number of EM iteration. Default is 2000.
stopping	Stopping rule for EM iteration. Possible values are "absolute" (based on absolute difference in log likelihood), "relative" (based on relative difference in log likelihood), or "aitken" (based on Aitken acceleration-based stopping rule). Default is "relative".

epsStopLL	Threshold to stop the EM iteration. Default is 1e-100.
parallel	Utilize multiple CPUs for parallel computing using "parallel" package? Possible values are TRUE (utilize multiple CPUs) or FALSE (do not utilize multiple CPUs). Default is FALSE (do not utilize multiple CPUs).
nCore	Number of CPUs when parallel computing is utilized.

## Details

`fitAll` function fits the GPA model and the GPA model under  $H_0$  for all possible pairs of GWAS datasets. Its output can be used as an input for the `shinyGPA` function.

## Value

A list with 6 elements, including `pmat` (original GWAS p-value matrix), `combs` (a matrix of GWAS pair indices), `combList` (a matrix of GWAS pair indices), `pTestPval` (a matrix of pleiotropy test p-values), `fitGPA` (a list of the GPA fit for each pair), and `fitH0` (a list of the GPA fit under  $H_0$  for each pair).

## Author(s)

Dongjun Chung, Emma Kortemeier

## References

Kortemeier E, Ramos PS, Hunt KJ, Kim HJ, Hardiman G, and Chung D (2017), "ShinyGPA: An interactive and dynamic visualization toolkit for genetic studies."

## See Also

[GPA](#), [pTest](#), and [shinyGPA](#).

## Examples

```
## Not run:
# simulator function

simulator <- function( risk.ind, nsnp=20000, alpha=0.6 ) {

  m <- length(risk.ind)

  p.sig <- rbeta( m, alpha, 1 )
  pvec <- runif(nsnp)
  pvec[ risk.ind ] <- p.sig

  return(pvec)
}

# run simulation

set.seed(12345)
nsnp <- 10000
```



```

alpha <- 0.4
pmat <- matrix( NA, nsnp, 5 )

pmat[,1] <- simulator( c(1:2000), nsnp=nsnp, alpha=alpha )
pmat[,2] <- simulator( c(501:2500), nsnp=nsnp, alpha=alpha )
pmat[,3] <- simulator( c(4001:6000), nsnp=nsnp, alpha=alpha )
pmat[,4] <- simulator( c(4501:7500), nsnp=nsnp, alpha=alpha )
pmat[,5] <- simulator( c(8001:10000), nsnp=nsnp, alpha=alpha )

# Fit GPA for all possible pairs of GWAS datasets

out <- fitAll( pmat )

# Run the ShinyGPA app using the output from fitAll()

shinyGPA(out)

## End(Not run)

```

GPA

*Fit GPA model*

## Description

Fit GPA model.

## Usage

```

GPA( gwasPval, annMat=NULL, pleiotropyH0=FALSE, empiricalNull=FALSE,
maxIter=2000, stopping="relative", epsStopLL=1e-10,
initBetaAlpha=0.1, initPi=0.1, initQ=0.75,
lbPi=NA, lbBetaAlpha=0.001, lbQ=0.001, lbPval=1e-30,
vDigit=1000, verbose=1 )

```

## Arguments

<code>gwasPval</code>	p-value matrix from GWAS data, where row and column correspond to SNP and phenotype, respectively.
<code>annMat</code>	Binary matrix from annotation data, where row and column correspond to SNP and annotation, respectively.
<code>pleiotropyH0</code>	Fit GPA under the null hypothesis of pleiotropy test? Possible values are TRUE (under the null hypothesis of pleiotropy test) or FALSE (usual assumption for GPA). Default is FALSE.
<code>empiricalNull</code>	Empirically estimate null distribution for GPA? Possible values are TRUE (empirical null distribution) or FALSE (theoretical null distribution). Default is FALSE.
<code>maxIter</code>	Maximum number of EM iteration. Default is 2000.

stopping	Stopping rule for EM iteration. Possible values are "absolute" (based on absolute difference in log likelihood), "relative" (based on relative difference in log likelihood), or "aitken" (based on Aitken acceleration-based stopping rule). Default is "relative".
epsStopLL	Threshold to stop the EM iteration. Default is 1e-100.
initBetaAlpha	Initial value for alpha estimate. Default is 0.1.
initPi	Initial value for pi estimate. Default is 0.1.
initQ	Initial value for q estimate. Default is 0.75.
lbPi	Lower bound for pi estimate. If lbPi=NA, lower bound is set to 1 / [number of SNPs]. Default is NA.
lbBetaAlpha	Lower bound for alpha estimate. Default is 0.001.
lbQ	Lower bound for q estimate. Default is 0.001.
lbPval	Lower bound for GWAS p-value. Any GWAS p-values smaller than lbPval are set to lbPval. Default is 1e-30.
vDigit	Number of digits for reporting parameter estimates. For example, setting it to 1000 means printing out values up to three digits below zero.
verbose	Amount of progress report during the fitting procedure. Possible values are 0 (minimal output), 1, 2, or 3 (maximal output). Default is 1.

## Details

GPA fits the GPA model. It requires to provide GWAS p-value to `gwasPval`, while users can also provide annotation data to `annMat`. It is assumed that number of rows of matrix provided to `gwasPval` equals to that provided to `annMat`.

`pTest` implements the hypothesis testing for pleiotropy. It requires two GPA model fits, one of interest and one under the null hypothesis, and they can be obtained by setting `pleiotropyH0=FALSE` and `pleiotropyH0=TRUE`, respectively.

`aTest` implements the hypothesis testing for annotation enrichment. It requires two GPA model fits, one fitted with using annotation data and one fitted without using annotation data, and they can be obtained by providing annotation data to `annMat` and not, respectively.

## Value

Construct GPA class object.

## Author(s)

Dongjun Chung

## References

Chung D\*, Yang C\*, Li C, Gelernter J, and Zhao H (2014), "GPA: A statistical approach to prioritizing GWAS results by integrating pleiotropy information and annotation data," *PLoS Genetics*, 10: e1004787. (\* joint first authors)

**See Also**

[assoc](#), [pTest](#), [aTest](#), [GPA](#).

**Examples**

```
## Not run:
# GPA without annotation data

fit.GPA.noAnn <- GPA( pmat, NULL )
cov.GPA.noAnn <- cov( fit.GPA.noAnn )

# GPA with annotation data

fit.GPA.wAnn <- GPA( pmat, ann )
cov.GPA.wAnn <- cov( fit.GPA.wAnn )

# GPA under the null hypothesis of pleiotropy test

fit.GPA.pleiotropy.H0 <- GPA( pmat, NULL, pleiotropyH0=TRUE )

## End(Not run)
```

---

GPA-class

---

Class "GPA"

---

**Description**

This class represents GPA model fit.

**Details**

When users use `fdr` method, users can specify the pattern using 1 and \* in `pattern` argument, where 1 and \* indicate phenotypes of interest and phenotypes that are not of interest, respectively. For example, when there are three phenotypes, `pattern="111"` means a SNP associated with all of three phenotypes, while `pattern="11*"` means a SNP associated with the first two phenotypes (i.e., association with the third phenotype is ignored (averaged out)).

**Objects from the Class**

Objects can be created by calls of the form `new("GPA", ...)`.

**Slots**

**fit:** Object of class "list", representing the fitted GPA model.

**setting:** Object of class "list", representing the setting for GPA model fitting.

**gwasPval:** Object of class "matrix", representing the p-value matrix from GWAS data.

**annMat:** Object of class "matrix", representing the annotation matrix.

## Methods

- show** signature(object = "GPA"): provide brief summary of the object.
- print** signature(x = "GPA"): provide the matrix of posterior probability that a SNP belongs to each combination of association status.
- fdr** signature(object = "GPA", pattern=NULL): provide local FDR. By default (i.e., pattern=NULL), it returns a matrix of local FDR that a SNP is not associated with each phenotype (i.e., marginal FDR), where the order of columns is same as that in input GWAS data. If a pattern is specified, a vector of corresponding local FDR is provided. See the details about how users can specify the pattern.
- cov** signature(object = "GPA", silent=FALSE, vDigitEst=1000, vDigitSE=1000 ): provide the covariance matrix for parameter estimates of GPA model. If silent=TRUE, it suppresses the summary output. vDigitEst and vDigitSE control number of digits for reporting parameter estimates and standard errors. For example, setting it to 1000 means printing out values up to three digits below zero.
- estimates** signature(object = "GPA"): extract parameter estimates from GPA model fit.
- se** signature(object = "GPA"): extract standard errors for parameter estimates from GPA model fit.

## Author(s)

Dongjun Chung

## References

Chung D\*, Yang C\*, Li C, Gelernter J, and Zhao H (2014), "GPA: A statistical approach to prioritizing GWAS results by integrating pleiotropy information and annotation data," PLoS Genetics, 10: e1004787. (\* joint first authors)

## See Also

[GPA](#), [pTest](#), [aTest](#).

## Examples

```
showClass("GPA")

## Not run:
fit.GPA.wAnn <- GPA( pmat, ann )
fit.GPA.wAnn
pp.GPA.wAnn <- print( fit.GPA.wAnn )
fdr.GPA.wAnn <- fdr( fit.GPA.wAnn )
fdr11.GPA.wAnn <- fdr( fit.GPA.wAnn, pattern="11" )
fdr1..GPA.wAnn <- fdr( fit.GPA.wAnn, pattern="1*" )
cov.GPA.wAnn <- cov( fit.GPA.wAnn )
est.GPA.wAnn <- estimates( fit.GPA.wAnn )
se.GPA.wAnn <- se( fit.GPA.wAnn )

## End(Not run)
```

---

pTest

*Hypothesis testing for pleiotropy*

---

### Description

Hypothesis testing for pleiotropy.

### Usage

```
pTest( fit, fitH0, vDigit=1000 )
```

### Arguments

fit	Fit of the GPA model of interest.
fitH0	GPA model fit under the null hypothesis of pleiotropy test.
vDigit	Number of digits for reporting parameter estimates and standard errors. For example, setting it to 1000 means printing out values up to three digits below zero.

### Details

pTest implements the hypothesis testing for pleiotropy. It requires two GPA model fits, one of interest and one under the null hypothesis (obtained by setting pleiotropyH0=TRUE when running GPA function), and evaluates genetical correlation among multiple phenotypes using the likelihood ratio test.

### Value

Returns a list with components:

pi	pi estimates.
piSE	Standard errors for pi estimates.
statistics	Statistics of the pleiotropy test.
pvalue	p-value of the pleiotropy test.

### Author(s)

Dongjun Chung

### References

Chung D\*, Yang C\*, Li C, Gelernter J, and Zhao H (2014), "GPA: A statistical approach to prioritizing GWAS results by integrating pleiotropy information and annotation data," PLoS Genetics, 10: e1004787. (\* joint first authors)

**See Also**

[aTest](#), [GPA](#), [GPA](#).

**Examples**

```
## Not run:
# GPA without annotation data

fit.GPA.noAnn <- GPA( pmat, NULL )

# GPA under the null hypothesis of pleiotropy test

fit.GPA.pleiotropy.H0 <- GPA( pmat, NULL, pleiotropyH0=TRUE )

# hypothesis testing for pleiotropy

test.pleiotropy <- pTest( fit.GPA.noAnn, fit.GPA.pleiotropy.H0 )

## End(Not run)
```

---

shinyGPA

---

*Run ShinyGPA app*


---

**Description**

Run ShinyGPA app.

**Usage**

```
shinyGPA( out=NULL )
```

**Arguments**

out                      output of fitAll function.

**Details**

shinyGPA runs the ShinyGPA app. It takes the output of the fitAll function, which fits the GPA model for all possible pairs of GWAS datasets, as input.

**Author(s)**

Dongjun Chung, Emma Kortemeier

**References**

Kortemeier E, Ramos PS, Hunt KJ, Kim HJ, Hardiman G, and Chung D (2017), "ShinyGPA: An interactive and dynamic visualization toolkit for genetic studies."

**See Also**[fitAll](#).**Examples**

```
## Not run:
# simulator function

simulator <- function( risk.ind, nsnp=20000, alpha=0.6 ) {

  m <- length(risk.ind)

  p.sig <- rbeta( m, alpha, 1 )
  pvec <- runif(nsnp)
  pvec[ risk.ind ] <- p.sig

  return(pvec)
}

# run simulation

set.seed(12345)
nsnp <- 10000
alpha <- 0.4
pmat <- matrix( NA, nsnp, 5 )

pmat[,1] <- simulator( c(1:2000), nsnp=nsnp, alpha=alpha )
pmat[,2] <- simulator( c(501:2500), nsnp=nsnp, alpha=alpha )
pmat[,3] <- simulator( c(4001:6000), nsnp=nsnp, alpha=alpha )
pmat[,4] <- simulator( c(4501:7500), nsnp=nsnp, alpha=alpha )
pmat[,5] <- simulator( c(8001:10000), nsnp=nsnp, alpha=alpha )

# Fit GPA for all possible pairs of GWAS datasets

out <- fitAll( pmat )

# Run the ShinyGPA app using the output from fitAll()

shinyGPA(out)

## End(Not run)
```

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