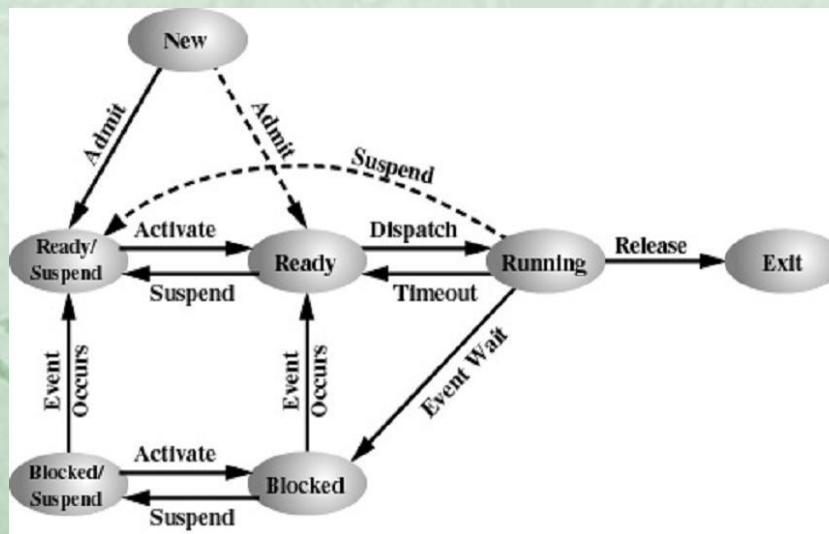


# Assignment 2 and Discrete Event Simulation



# Problem Specification

- For this assignment, you are to write a **Discrete Event Simulation** to analyze different CPU scheduling algorithms.
- A number of simultaneous processes (threads) will be simulated, each alternating between bursts of CPU usage and I/O waiting. The process data will be read in from a data file.



# Discrete Event Simulation

- Set up a loop, jump forward in time with each iteration to whenever the next meaningful event occurs. Some time steps may be small ( even 0 if two or more things happen at the same time ) and some may be large.
- Some events may trigger other events, which are then put on the schedule to be processed when their time comes.
- This approach is called **Discrete Event Simulation** (DES).
- An important data structure in DES is **Priority Queue** which holds events to be scheduled.



# Priority Queue ADT

- A priority queue stores a collection of items
- An item is a pair (key, element)
- Main methods of the Priority Queue ADT
  - ⌘ `insertItem(k, e)`  
inserts an item with key `k` and element `e`
  - ⌘ `e = removeMin()`  
removes the item with smallest key and returns its element `e`
- Additional methods
  - ⌘ `minKey()`  
returns, but does not remove, the smallest key of an item
  - ⌘ `minElement()`  
returns, but does not remove, the element of an item with smallest key
  - ⌘ `size()`, `isEmpty()`
- Applications:
  - ⌘ Standby flyers
  - ⌘ Auctions
  - ⌘ Discrete Event Simulation



# Example: Priority Queue

Operator	Output	Priority Queue
insertItem(5, A)	—	(5,A)
insertItem(9, C)	—	(5,A),(9,C)
insertItem(3, B)	—	(3,B),(5,A),(9,C)
insertItem(7, D)	—	(3,B),(5,A),(7,D),(9,C)
minElement()	B	(3,B),(5,A),(7,D),(9,C)
minKey()	3	(3,B),(5,A),(7,D),(9,C)
removeMin()	B	(5,A),(7,D),(9,C)
size()	3	(5,A),(7,D),(9,C)
removeMin()	A	(7,D),(9,C)
removeMin()	D	(9,C)
removeMin()	C	
removeMin()	error	
isEmpty()	true	



# Total Order Relation

- Keys in a Priority Queue can be arbitrary objects on which an order is defined. For example, simulation time.
- Two distinct items in a priority queue can have the same key. For example, two processes arrive at the same time.
- For a pair events:  $(t1, p1)$  and  $(t2, p2)$ , we define a “happen before” relation  $\Rightarrow$  such that:
  - $(t1, p1) \Rightarrow (t2, p2)$  if  $t1 < t2$
  - Or  $(t1, p1) \Rightarrow (t2, p2)$  if  $t1 == t2$  and  $p1 < p2$  (where pids are unique)



# Using heap to implement PQ

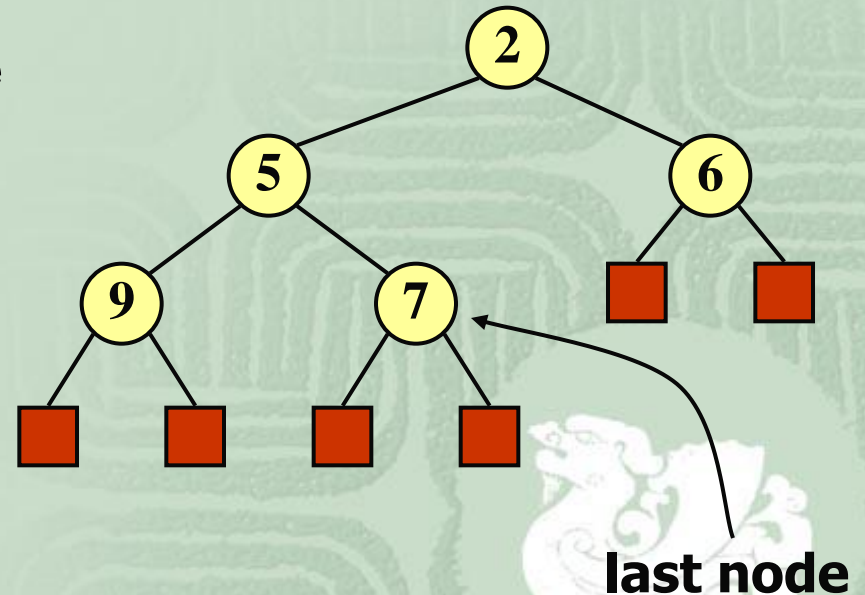
- A heap is a binary tree storing keys at its internal nodes and satisfying the following properties:
- The last node of a heap is the rightmost internal node of depth  $h - 1$

⌘ **Heap-Order:** for every internal node  $v$  other than the root,

$$\text{key}(v) \geq \text{key}(\text{parent}(v))$$

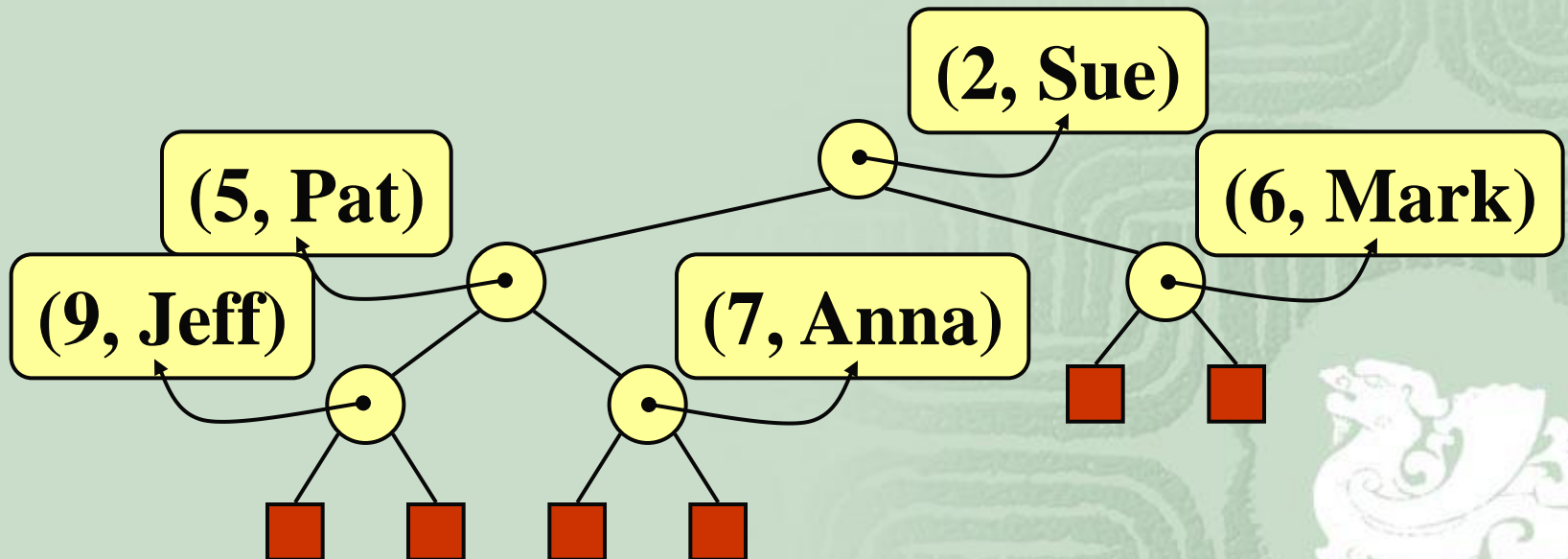
⌘ **Complete Binary Tree:** let  $h$  be the height of the heap

- for  $i = 0, \dots, h - 1$ , there are  $2^i$  nodes of depth  $i$
- at depth  $h - 1$ , the internal nodes are to the left of the external nodes



# Heaps and Priority Queues

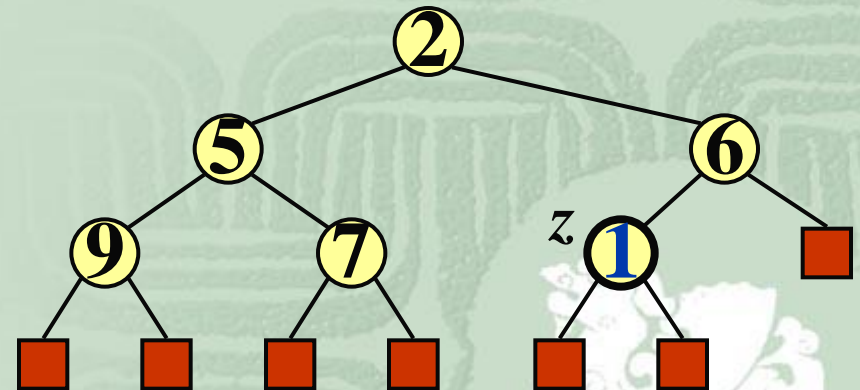
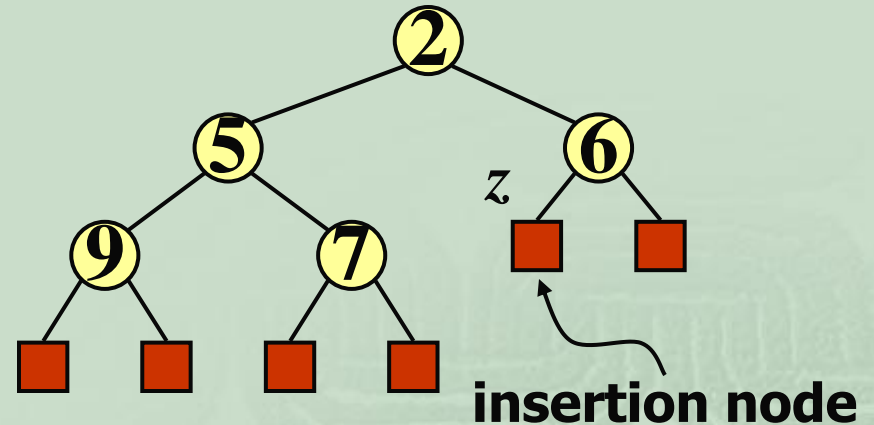
- We can use a heap to implement a priority queue
- We store a (key, element) item at each internal node
- We keep track of the position of the last node
- For simplicity, we show only the keys in the pictures





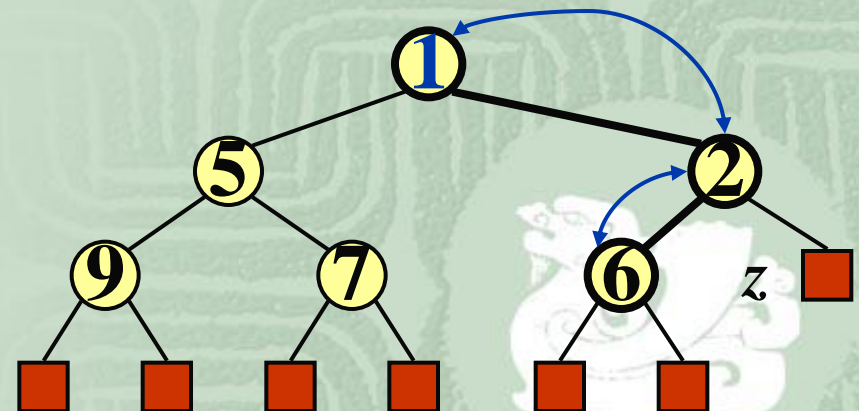
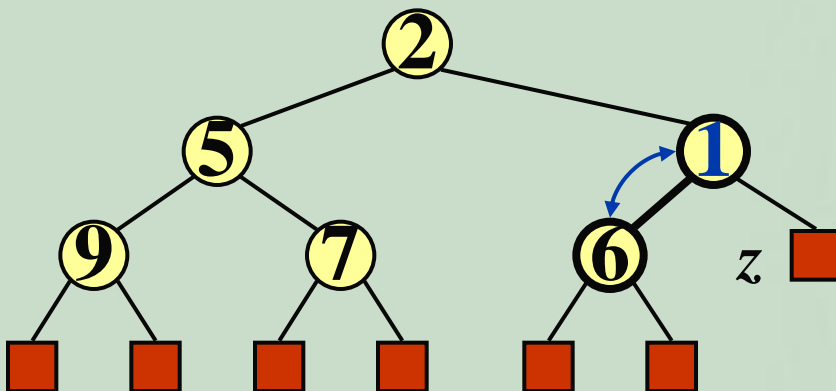
# Insertion into a Heap

- The insertion algorithm consists of three steps
  - ∞ Find the insertion position  $z$  (the new last node)
  - ∞ Store  $k$  at  $z$  and expand  $z$  into an internal node
  - ∞ Restore the heap-order property (discussed next)



# Upheap

- After the insertion of a new key  $k$ , the heap-order property may be violated
- Algorithm upheap restores the heap-order property by swapping  $k$  along an upward path from the insertion node
- Upheap terminates when the key  $k$  reaches the root or a node whose parent has a key smaller than or equal to  $k$
- Since a heap has height  $O(\log n)$ , upheap runs in  $O(\log n)$  time



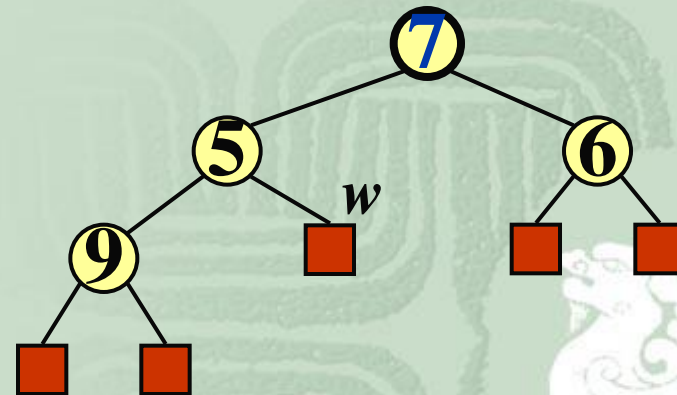
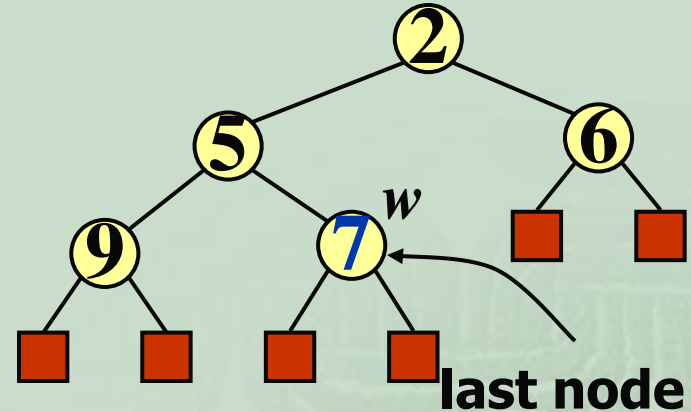
# Removal from a Heap

The removal algorithm consists of three steps

Replace the root key with the key of the last node  $w$

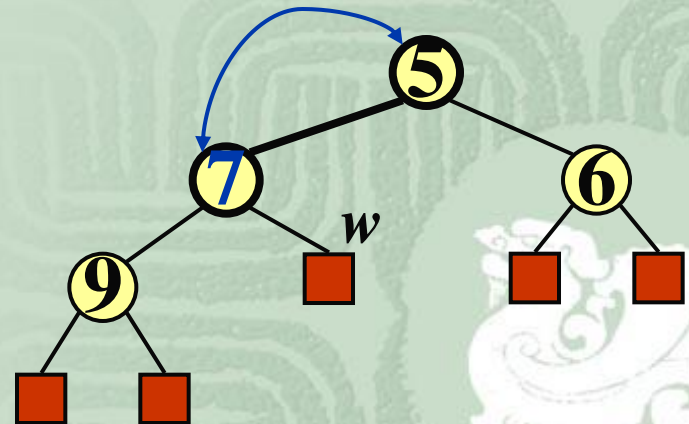
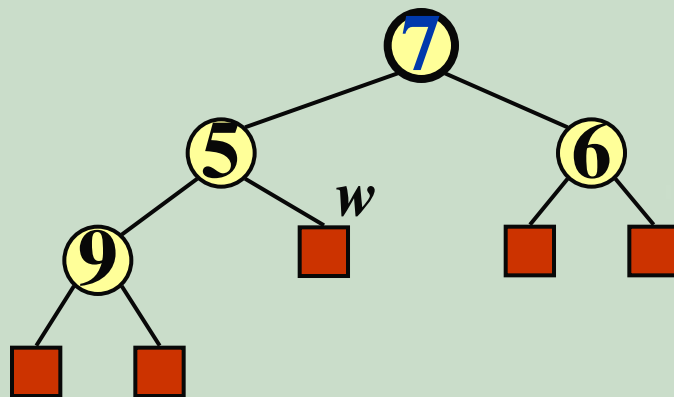
Delete  $w$

Restore the heap-order property (discussed next)



# Downheap

- After replacing the root key with the key  $k$  of the last node, the heap-order property may be violated
- Algorithm downheap restores the heap-order property by swapping key  $k$  along a downward path from the root
- Downheap terminates when key  $k$  reaches a leaf or a node whose children have keys greater than or equal to  $k$
- Since a heap has height  $O(\log n)$ , downheap runs in  $O(\log n)$  time



## The general pseudo code for a DES is as follows:

*Initialize PQ.*

*while( PQ not empty ) {*

*extract an **Event** from the PQ.*

*update time to match the Event.*

*switch( type of **Event** ) {*

*Process this event, possibly adding  
        new Events to the PQ.*

*} // switch*

*} // while*

*Process statistics collected during Event processing & report.*



# Input file format

number\_of\_processes thread\_switch process\_switch

process\_number(1) number\_of\_threads(1)

thread\_number(1) arrival\_time(1) number\_of\_CPU(1)

1 cpu\_time io\_time

2 cpu\_time io\_time

.

.

number\_of\_CPU(1) cpu\_time

...





# Example

```
2 3 7          // number_of_processes thread_switch process_switch

1 4            // process_number(1)  number_of_threads(1)
1 0 6          // thread_number(1) arrival_time(1)  number_of_CPU(1)
1 15 400       // 1  cpu_time io_time
2 18 200       // 2  cpu_time io_time
3 15 100       // 3  cpu_time io_time
4 15 400       // 4  cpu_time io_time
5 25 100       // 5  cpu_time io_time
6 240          // 6  cpu_time

2 12 4         // thread_number(2) arrival_time(2)  number_of_CPU(2)

...
```

