

#### **Preprocessing Strings**

- A trie (retrieval) is a special kind information access tree.
- If the text is large, immutable and searched for often (e.g., works by Shakespeare), we may want to preprocess the text.
- A trie is a compact data structure for representing a set of strings, such as all the words in a text
  - A trie supports pattern matching queries in time proportional to the pattern size

Tries and Huffman Codes

Standard Trie

The standard trie for a set of strings S is an ordered tree such that:

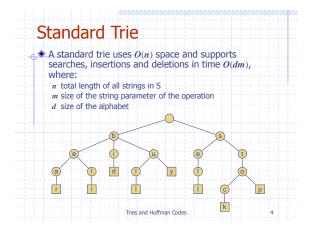
Each node but the root is labeled with a character

The children of a node are alphabetically ordered

The paths from the root to external nodes yield the strings of S

Example: standard trie for the set of strings

S = { bear, bell, bid, bull, buy, sell, stock, stop }



### Application:

- use a trie to perform a special type of pattern matching: word matching.
- differ from standard pattern matching since the pattern can not match with an arbitrary substring of the text, but only one of its words.
- suitable for applications where a series of queries is performed on a fixed text.

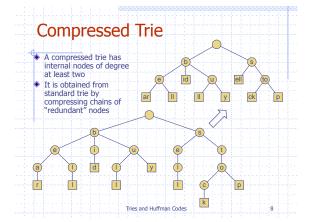
Tries and Huffman Codes 5

#### Word Matching with a Trie We insert the words of the text into a trie b | i | d | | s | t | o | c | k | ! | | b | i | d | | s | t | o | c | k | ! | Each leaf stores the occurrences of the associated word in the text d d r 12 k Tries and Huffman Codes

### **Compressed Tries:**

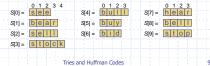
- An internal node ν of T is redundant if ν has one child and is not the root.
- A chain of redundant nodes can be compressed by replacing the chain with a single node with the concatenation of the labels of nodes in the chain.

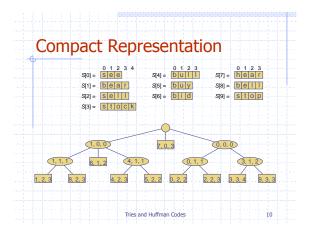
Tries and Huffman Codes



## **Compact Representation**

- Compact representation of a compressed trie for an array of strings:
  - Stores at the nodes ranges of indices instead of substrings
  - Uses O(s) space, where s is the number of strings in the array
  - Serves as an auxiliary index structure
  - S is an array of strings S[0], ... S[s-1]
  - Instead of storing a node label X explicitly, we represent it implicitly by a triplet of integers (i, j, k), such that X = s[i][j..k].





# **Huffman Encoding**

- Compression
  - Typically, in files and messages,
    - Each character requires 1 byte or 8 bits (fixed length coding)
    - Already wasting 1 bit for most purposes!
- Question
  - What's the smallest number of bits that can be used to store an arbitrary piece of text?
- 🌢 Idea
  - Find the frequency of occurrence of each character
  - Encode Frequent characters short bit strings
  - Rarer characters longer bit strings
  - Variable length coding

Tries and Huffman Codes

#### **Encoding Trie** A code is a mapping of each character of an alphabet to a binary code-word A prefix code is a binary code such that no code-word is the prefix of another code-word An encoding trie represents a prefix code · Each leaf stores a character The code word of a character is given by the path from the root to the leaf storing the character (0 for a left child and 1 for a right child) 00 010 011 10 а b d d е a b Tries and Huffman Codes

