9/26/2019 Subset Sums



# **Subset Sums**

**JRM** 

For many sets of consecutive integers from 1 through N ( $1 \le N \le 39$ ), one can partition the set into two sets whose sums are identical.

For example, if N=3, one can partition the set  $\{1, 2, 3\}$  in one way so that the sums of both subsets are identical:

• {3} and {1,2}

This counts as a single partitioning (i.e., reversing the order counts as the same partitioning and thus does not increase the count of partitions).

If N=7, there are four ways to partition the set  $\{1, 2, 3, ... 7\}$  so that each partition has the same sum:

- {1,6,7} and {2,3,4,5}
- {2,5,7} and {1,3,4,6}
- {3,4,7} and {1,2,5,6}
- $\{1,2,4,7\}$  and  $\{3,5,6\}$

Given N, your program should print the number of ways a set containing the integers from 1 through N can be partitioned into two sets whose sums are identical. Print 0 if there are no such ways.

Your program must calculate the answer, not look it up from a table.

#### **PROGRAM NAME: subset**

## **INPUT FORMAT**

The input file contains a single line with a single integer representing N, as above.

### **SAMPLE INPUT (file subset.in)**

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#### **OUTPUT FORMAT**

The output file contains a single line with a single integer that tells how many same-sum partitions can be made from the set {1, 2, ..., N}. The output file should contain 0 if there are no ways to make a same-sum partition.

### **SAMPLE OUTPUT (file subset.out)**

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