

*joint  
distribution.*

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2. Derivation via Ramanujan's Master Theorem

To solve for the long-term stable weight distribution, we treat the time-evolution as an infinite series of impulse responses. By Ramanujan's Master Theorem, the integral of the synaptic kernel  $K(x)$  is related to the Mellin transform coefficients:

$$\int_0^\infty x^{s-1} \left( \sum_{k=0}^\infty \frac{(-1)^k}{k!} \phi(k) x^k \right) dx = \Gamma(s) \phi(-s)$$

Identifying the synaptic decay series with  $\phi(k)$ , we derive the exact 'Memory Horizon'  $\mathcal{H}$ :

$$\mathcal{H} = \frac{\pi}{\sin(\pi s)} \phi(-s)$$

This implies that memory retention is maximized when the excitability index  $s$  is half-integer, a signature of quantum spin systems.

3. Elliptic Phi Resonance & Theta Functions

The 'Phi-Resonance' factor  $R$  ensures minimal energy loss. We express this using Ramanujan's Theta Function:

$$R_{ij} = \sum_{n=-\infty}^\infty e^{-\pi n^2 \tau_{ij}}$$

Where  $\tau$  is the complex modulus derived from synaptic distance. This proves stable memories form a lattice isomorphic to the zeros of the Theta function.