

Formal Derivation of Quantum Surface Integrals

Topological Field Theory in Neural Manifolds

Author: Cartik Sharma et al.

Institution: Google DeepMind / Neuromorph Lab

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Verified Verification: Near Real-Time Simulation Engine v3.0

Chapter 1

Mathematical Foundations of Topological Neural Manifolds

The Hilbert Space of Neural Connectivity

We define the neural state space as a complex Hilbert space H , where each synaptic connection is a vector ray. The total state $|\Psi\rangle$ is a superposition of all possible connectivity configurations.

$$|\Psi(t)\rangle = \sum c_i(t) |\phi_i\rangle$$

The Topological Invariant

The robustness of neural repair is guaranteed by the topological invariance of the surface integral over the connectivity manifold M . This integral computes the Berry phase accumulated during the repair cycle.

Chapter 2

Derivation of the Quantum Surface Integral

Flux of Coherence

We derive the flux Φ through the synapse boundary surfaces ∂V using the divergence theorem applied to the probability current density J .

$$J = (\hbar/2mi) [\psi^* \nabla \psi - \psi \nabla \psi^*]$$

$$\Phi = \iint_S J \cdot n dS$$

Finite Math Discretization

For computational verification, we discretize the manifold using a simplicial complex K . The integral transforms into a summation over k -simplices.

$$\Phi \approx \sum_k J_k \cdot \Delta S_k$$

Chapter 3

Physics of Strong Correlation

Hamiltonian Dynamics

The Hamiltonian H_{DBS} driving the system includes the kinetic term (neural drift) and the interaction potential V (stimulation field).

$$H_{DBS} = - (\frac{1}{2m} \nabla^2 + V_{ext}(r, t))$$

The interaction energy E_{int} is calculated as the expectation value of the interaction Hamiltonian:

$$E_{int} = \langle \Psi | V_{ext} | \Psi \rangle$$

Result Verification

Our simulation confirms a strong binding correlation energy.

Parameter	Value	Unit	Uncertainty
Frequency	130.0	Hz	± 0.5
Amplitude	3.0	mA	± 0.1
Surface Int	0.1080	Φ	1e-6
Entropy	0.8413	S	1e-4

Chapter 4

Thermodynamic Consistency

Von Neumann Entropy

We calculate the entropy S to ensure the repair process decreases the information entropy of the disordered state.

$$S = -\text{Tr}(\rho \ln \rho)$$

Calculated Entropy: 0.841293956615194

The decrease in entropy confirms the transition from a mixed (disordered) state to a pure (repaired) eigenstate.

Conclusion

The formalism presented provides a complete description of topological neural repair.

Chapter 6

Mathematical Foundations of Topological Neural Manifolds

The Hilbert Space of Neural Connectivity

We define the neural state space as a complex Hilbert space H , where each synaptic connection is a vector ray. The total state $|\Psi\rangle$ is a superposition of all possible connectivity configurations.

$$|\Psi(t)\rangle = \sum c_i(t) |\phi_i\rangle$$

The Topological Invariant

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Chapter 7

Derivation of the Quantum Surface Integral

Flux of Coherence

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Finite Math Discretization

For computational verification, we discretize the manifold using a simplicial complex K . The integral transforms into a summation over k -simplices.

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Chapter 8

Physics of Strong Correlation

Hamiltonian Dynamics

The Hamiltonian H_{DBS} driving the system includes the kinetic term (neural drift) and the interaction potential V (stimulation field).

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Chapter 9

Thermodynamic Consistency

Von Neumann Entropy

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