

(Q4)

The contrapositive of a conditional statement  $A \Rightarrow B$  is  $\neg B \Rightarrow \neg A$ .

This is because  $A \Rightarrow B$  does not go both ways:

$$A \Rightarrow B \neq B \Rightarrow A$$

Intuitively speaking,  $A \Rightarrow B$  means that "If  $A$  is true, then  $B$  must be true."

This does not necessarily imply that "If  $B$  is true, then  $A$  must be true", as  $B$  being true does not necessarily mean that  $A$  is true.

In order to achieve the logical equivalent of  $A \Rightarrow B$ , we need to negate both the condition and outcome in  $B \Rightarrow A$ :

$$A \Rightarrow B = \neg B \Rightarrow \neg A$$

This clearly makes more sense, as from the earlier intuitive definition, if  $B$  is false then we know that  $A$  is false.

To apply this to the given statement:

If it's raining, then it's cloudy.

The logical equivalent of this statement is not "If it's cloudy, then it's raining". We know this intuitively: Just because it's cloudy, it doesn't mean there is rain. In order to achieve logical equivalency, we need to negate both sides:

If it's not cloudy, then it's not raining.

Which is the given contrapositive of the given statement.