

(Q6)

(a) True.

Proof. We observe that by properties of the integral,

$$\begin{aligned}\int_{-a}^a f(x)dx &= \int_{-a}^0 f(x)dx + \int_0^a f(x)dx \\ - \int_{-a}^0 f(x)dx &= \int_0^{-a} f(x)dx\end{aligned}$$

Since f is even, $f(a) = f(-a)$:

$$\int_0^a f(x)dx = \int_0^{-a} f(x)dx$$

The result follows. ■

(b) True.

Proof. Since $f(x)$ is continuous on $\mathbb{R} \setminus \{0\}$ and may or may not have a discontinuity at 0, the proof follows by proof of Q3. ■

(c) False.

(d) True.