

**(Q1)**

(a) We can factorize  $\frac{x+1}{x^2-x}$  as follows:

$$\frac{x+1}{x(x-1)}$$

Considering the denominator, we can only have a negative value of the term when  $x > 0, x < 1$ . Considering the numerator, the entire term stays negative for all  $x < -1$ , as all  $x$  terms will be negative.

Thus, the final interval is:

$$(-\infty, -1) \cup (0, 1)$$

(b) We can factorise  $3 < |3x+9| < 12$ :

$$\begin{aligned} 3 < 3|x+3| < 12 \\ 1 < |x+3| < 4 \end{aligned}$$

From this inequality we can infer

$$\begin{aligned} 1 < |x+3| + 4 &\implies -4 < x+3 < -1 \text{ and } 1 < x+3 < 4 \\ &\implies -7 < x < -4 \text{ and } -2 < x < 1 \end{aligned}$$

The final interval is:

$$(-7, -4) \cup (-2, 1)$$