

Q1

Given X, Y as follows:

$$X = [7, 4], Y = \left(-\frac{14}{8}, 8\right)$$

These are the answers:

(a) $X \cup Y = (-7, 8]$

(b) $Y \cap X = \left(-\frac{14}{5}, 4\right]$

(c)

$$Y^c = (-\infty, -\frac{14}{5}] \cup [8, \infty)$$

$$X = [-7, 4]$$

$$Y^c \cup X = [-7, -\frac{14}{5}] \cup [4, 8]$$

(d)

$$X^c = (-\infty, -7) \cup (4, \infty)$$

$$Y = \left(-\frac{14}{5}, 8\right)$$

$$X^c \cup Y = (-\infty, -\frac{14}{5}] \cup [4, \infty)$$

(e) $Y \setminus X = (4, 8)$

(f)

$$X^c = (-\infty, 7) \cup (4, \infty)$$

$$Y \cap X^c = \left(-\frac{14}{5}, 8\right)$$

$$(Y \cap X^c) \cap \mathbb{Z} = \{-2, -1, 0, 1, 2, 3, 4, 5, 6, 7\}$$

(g)

$$\mathbb{Z}^c = \{x \in \mathbb{R} : x \notin \mathbb{Z}\} = \mathbb{R} \setminus \mathbb{Z}$$

$$(Y \cap X) \cup \mathbb{Z}^c = (4, 5) \cup (5, 6) \cup (6, 7) \cup (7, 8)$$