

Q3

Using properties of integrals:

$$\begin{aligned}\int_{-\infty}^0 x^2 e^x dx &= - \int_0^{-\infty} x^2 e^x dx \\ &= - \lim_{b \rightarrow -\infty} \left[\int_0^b x^2 e^x dx \right]\end{aligned}$$

Integrating by parts, we assign

$$u = x^2, \quad du = 2x dx, \quad dv = e^x dx, \quad v = e^x$$

$$\int x^2 e^x dx = x^2 e^x - \int e^x 2x dx$$

Integrating by parts once again, we assign

$$u = 2x, \quad du = 2 dx, \quad dv = e^x dx, \quad v = e^x$$

$$\int 2x e^x dx = x^2 e^x - 2 \int e^x dx = x^2 e^x - 2e^x$$

So the improper integral evaluates to:

$$- \lim_{b \rightarrow -\infty} [e^x (x^2 - 2x - 2)]$$

Which is clearly minus infinity, and so the integral diverges.