

(Q6)

*Proof.* We formulate a homogenous system from the set given to us:

$$\begin{cases} a\mathbf{x} + c\mathbf{y} = 0 \\ b\mathbf{x} + d\mathbf{y} = 0 \end{cases}$$

We can then row-reduce:

$$\left(\begin{array}{cc|c} a & c & 0 \\ b & d & 0 \end{array}\right) \rightarrow \left(\begin{array}{cc|c} 1 & \frac{c}{a} & 0 \\ b & d & 0 \end{array}\right) \rightarrow \left(\begin{array}{cc|c} 1 & \frac{c}{a} & 0 \\ 0 & \frac{ad-bc}{a} & 0 \end{array}\right)$$

Since  $ad - bc \neq 0$ , this is not yet in RREF and we continue to row-reduce.

$$\left(\begin{array}{cc|c} 1 & \frac{c}{a} & 0 \\ 0 & 1 & 0 \end{array}\right) \rightarrow \left(\begin{array}{cc|c} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array}\right)$$

Which forms a linearly independent set. ■