The goal of this discussion section is to get familiar with maximizing likelihood.

Participation in discussion section counts as 5% of the grade. Completion of the worksheets counts as 20% of the grade. Submit your worksheet work by April 14th at 2:59pm.

1. Suppose that X is a discrete random variable with the following probability mass function:

with  $0 \le \theta \le 1$  is a parameter. The following 15 observations were taken from such a distibrution: (3,0,2,1,3,2,1,0,2,1,3,2,1,0,0). We want to estimate the maximum likelihood estimate of  $\theta$ .

- (a) Knowing that the Likelihood function is given by  $F(\theta) = \prod_{i=1}^{N} P(X = x_i)$ , given the observations  $x_1, \ldots, x_N$ , write  $F(\theta)$  using the 10 observations.
- (b) Write  $L(\theta) = \log F(\theta)$  and find the maximum  $\theta^*$ .
- 2. Let  $X_1, \ldots, X_N$  be independent and identically distributed sample from a Poisson distribution with parameter  $\lambda$ . In other words

$$P(X = x | \lambda) = \frac{\lambda^x e^{-\lambda}}{x!}.$$

Find the Maximum Likelihood Estimate of the parameter  $\lambda$  (Consider given observations  $x_1, x_2, \ldots, x_N$ ).

3. Submit your work on Catcourses under the assignment Worksheet 11 as a .pdf.