The goals of this discussion section are:

- 1. Work on your homework 7 group problem (early start compared to other times)
- 2. Get familiar with linear solvers

Participation in discussion section counts as 5% of the grade. Completion of the worksheets counts as 20% of the grade. Submit your worksheet work by April 7th at 2:59pm.

- 1. Work on your Homework 7 as a group. Take advantage of this common time to make the most of it (recall it is due by April 14th at 11:59pm). Take this time to get familiar with the problem and assign roles.
- 2. Solve a  $5 \times 5$  linear system of the form Ax = b, with A, b of your choice (A can't be the identity matrix, and should have most of its entry non zero). Compare with the solution obtained while computing directly  $x = A^{-1}b$  with the one obtained with the conjugate\_gradient function

```
def conjugate_gradient(A, b, x0, eta, Imax):
x = x0
r = b - A@x
d = r
n0 = np.dot(r,r)
n1 = n0
res = []
i = 0
while n0 > eta, and i < Imax:
    z = A@d
    alpha = n0 / (np.dot(z,d))
    x = x + alpha * d
    r = r - alpha * z
    n1 = np.dot(r,r)
    beta = n1 / n0
    d = r + beta * d
    n0 = n1
    i = i+1
    res = [res, np.sqrt(n1)]
    if np.sqrt(n1) > 1e10:
        break
return x, i, res
```

Provide comments on your choices of parameters, what you observe overall (computational time, error, etc.).

3. Submit your work (only item 2.) on Catcourses under the assignment Worksheet 10 as a .pdf. You will submit your work for item 1. within the assignment Homework 7 (group) in two weeks.