## SCC

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This file is part of CasADi.

CasADi -- A symbolic framework for dynamic optimization.

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```
[1]: from casadi import * import numpy
```

Let's construct a block diagonal structure

```
[2]: A = diagcat(1,DM([[2,3],[3,4]]),DM([[5,6,7],[6,8,9],[7,9,10]]),11)
    print(A)
    A.sparsity().spy()
```

```
[[1, 00, 00, 00, 00, 00, 00], [00, 2, 3, 00, 00, 00, 00], [00, 3, 4, 00, 00, 00, 00], [00, 00, 00, 5, 6, 7, 00], [00, 00, 00, 6, 8, 9, 00], [00, 00, 00, 00, 7, 9, 10, 00], [00, 00, 00, 00, 00, 00, 11]]
```

```
. **...
     . **...
    ...***.
    ...***.
[3]: numpy.random.seed(2)
    We randomly permute this nice structure
[4]: perm = list(numpy.random.permutation(list(range(A.size1()))))
     AP = A[perm,perm]
[5]: print(AP)
     AP.sparsity().spy()
    [[8, 00, 6, 00, 00, 9, 00],
     [00, 2, 00, 3, 00, 00, 00],
     [6, 00, 5, 00, 00, 7, 00],
     [00, 3, 00, 4, 00, 00, 00],
     [00, 00, 00, 00, 11, 00, 00],
     [9, 00, 7, 00, 00, 10, 00],
     [00, 00, 00, 00, 00, 00, 1]]
    *.*..*.
    .*.*..
    *.*..*.
    .*.*..
    ...* . .
    *.*..*.
    ...*
    And use scc to recover the blocks
[6]: n,p,r = AP.sparsity().scc()
[7]: APrestored = AP[p,p]
[8]: print(APrestored)
     APrestored.sparsity().spy()
     print("# blocks: ", n)
     print("block boundaries: ", r[:n])
    [[8, 6, 9, 00, 00, 00, 00],
     [6, 5, 7, 00, 00, 00, 00],
     [9, 7, 10, 00, 00, 00, 00],
     [00, 00, 00, 2, 3, 00, 00],
```

```
[00, 00, 00, 3, 4, 00, 00],
[00, 00, 00, 00, 00, 11, 00],
[00, 00, 00, 00, 00, 00, 1]]

***...

***...

***...

...**..

...*

# blocks: 4
block boundaries: [0, 3, 5, 6]
```