## ipopt

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This file is part of CasADi.

CasADi -- A symbolic framework for dynamic optimization.

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## 1 nlpsol

```
[1]: from casadi import * from numpy import *
```

In this example, we will solve a few optimization problems with increasing complexity

## 2 Scalar unconstrained problem

```
\min_x \qquad (x-1)^2 \ \backslash \ \text{subject to} \ -10 \le x \le 10 \ \backslash \ \ \  with x scalar
```

```
[2]: x=SX.sym('x')
nlp = {'x':x, 'f':(x-1)**2}
```

```
[3]: solver = nlpsol('solver', 'ipopt', nlp)
    sol = solver(lbx=-10, ubx=10)
    This program contains Ipopt, a library for large-scale nonlinear optimization.
     Ipopt is released as open source code under the Eclipse Public License (EPL).
            For more information visit https://github.com/coin-or/Ipopt
    This is Ipopt version 3.14.11, running with linear solver MUMPS 5.4.1.
    Number of nonzeros in equality constraint Jacobian ...:
    Number of nonzeros in inequality constraint Jacobian.:
                                                                0
    Number of nonzeros in Lagrangian Hessian...:
    Total number of variables...:
                        variables with only lower bounds:
                   variables with lower and upper bounds:
                                                                1
                        variables with only upper bounds:
                                                                0
    Total number of equality constraints...:
    Total number of inequality constraints...:
            inequality constraints with only lower bounds:
                                                                0
       inequality constraints with lower and upper bounds:
                                                                0
            inequality constraints with only upper bounds:
                                                                0
    iter
           objective
                        inf_pr
                                 inf_du lg(mu) ||d|| lg(rg) alpha_du alpha_pr ls
       0 1.0000000e+00 0.00e+00 2.00e+00 -1.0 0.00e+00
                                                          - 0.00e+00 0.00e+00
       1 8.2644627e-03 0.00e+00 1.53e-02 -1.0 9.09e-01
                                                          - 9.16e-01 1.00e+00f
       2 3.3212748e-06 0.00e+00 2.08e-17 -1.0 8.91e-02
                                                          - 1.00e+00 1.00e+00f
       3 9.3171258e-10 0.00e+00 7.11e-17 -2.5 1.79e-03
                                                          - 1.00e+00 1.00e+00f
       4 2.3111166e-12 0.00e+00 2.40e-17 -3.8 2.90e-05
                                                          - 1.00e+00 1.00e+00f
       5 3.4736752e-16 0.00e+00 5.92e-17 -5.7 1.50e-06
                                                          - 1.00e+00 1.00e+00f 1
       6 6.4072417e-22 0.00e+00 3.96e-17 -8.6 1.86e-08
                                                          - 1.00e+00 1.00e+00f 1
    Number of Iterations...: 6
                                      (scaled)
                                                              (unscaled)
                 6.4072416740416713e-22
                                          6.4072416740416713e-22
    Objective ...:
    Dual infeasibility...:
                          3.9625445352197450e-17
                                                   3.9625445352197450e-17
                            0.000000000000000e+00
    Constraint violation...:
                                                     0.000000000000000e+00
    Variable bound violation:
                               0.000000000000000e+00
                                                        0.000000000000000e+00
    Complementarity...:
                       2.5059073699316697e-09
                                                2.5059073699316697e-09
    Overall NLP error...:
                         2.5059073699316697e-09
                                                  2.5059073699316697e-09
```

Number of objective function evaluations

```
Number of objective gradient evaluations
    Number of equality constraint evaluations
    Number of inequality constraint evaluations
    Number of equality constraint Jacobian evaluations
    Number of inequality constraint Jacobian evaluations = 0
    Number of Lagrangian Hessian evaluations
    Total seconds in IPOPT
                                                              = 0.004
    EXIT: Optimal Solution Found.
           solver :
                        t_proc
                                     (avg) t_wall
                                                           (avg)
                                                                     n eval
            nlp_f | 50.00us ( 7.14us) 19.60us ( 2.80us)
                                                                          7
      nlp_grad_f | 38.00us ( 4.75us) 18.10us ( 2.26us)
                                                                          8
      nlp_hess_1 | 21.00us ( 3.50us) 10.50us ( 1.75us)
                                                                          6
                        9.05ms ( 9.05ms) 4.53ms ( 4.53ms)
            total
                                                                          1
    The solution is obviously 1:
[4]: print(sol['x'])
     assert(abs(sol['x']-1)<1e-9)</pre>
    1
         Constrained problem
             (x-1)^T \cdot (x-1) \setminus \text{subject to } -10 \le x \le 10 \setminus \text{subject to } 0 \le x_1 + x_2 \le 1 \setminus \text{subject to } \$
    x 0 = 2$
    with x \in \mathbf{R}^n
[5]: n = 5
[6]: x=SX.sym('x',n)
    Note how we do not distinguish between equalities and inequalities here
[7]: nlp = \{ 'x' : x, 'f' : mtimes((x-1).T,x-1), 'g' : vertcat(x[1]+x[2],x[0]) \}
[8]: solver = nlpsol('solver', 'ipopt', nlp)
     sol = solver(lbx=-10, ubx=10, lbg=[0,2], ubg=[1,2])
    This is Ipopt version 3.14.11, running with linear solver MUMPS 5.4.1.
    Number of nonzeros in equality constraint Jacobian ...:
    Number of nonzeros in inequality constraint Jacobian .:
                                                                        2
    Number of nonzeros in Lagrangian Hessian ...:
    Total number of variables ...:
                           variables with only lower bounds:
                                                                        0
```

variables with lower and upper bounds:

```
variables with only upper bounds:
                                                              0
Total number of equality constraints...:
Total number of inequality constraints ...:
        inequality constraints with only lower bounds:
                                                              0
   inequality constraints with lower and upper bounds:
                                                              1
        inequality constraints with only upper bounds:
iter
        objective
                     inf_pr
                              inf_du lg(mu) ||d|| lg(rg) alpha_du alpha_pr
   0 5.0000000e+00 2.00e+00 2.00e+00 -1.0 0.00e+00
                                                        - 0.00e+00 0.00e+00
   1 2.7716739e+00 0.00e+00 1.16e+00 -1.0 2.00e+00
                                                        - 3.75e-01 1.00e+00f
   2 1.5112117e+00 0.00e+00 4.53e-01 -1.0 1.31e+00
                                                        - 9.44e-01 6.62e-01f
   3 1.5183915e+00 0.00e+00 1.11e-16 -1.7 3.46e-02
                                                        - 1.00e+00 1.00e+00f
   4 1.5009100e+00 0.00e+00 2.03e-04 -3.8 1.73e-02
                                                        - 9.88e-01 1.00e+00f
   5 1.5000028e+00 0.00e+00 2.22e-16 -5.7 9.07e-04
                                                        - 1.00e+00 1.00e+00f
   6 1.5000000e+00 0.00e+00 2.04e-16 -8.6 2.85e-06
                                                        - 1.00e+00 1.00e+00f
Number of Iterations...: 6
                                   (scaled)
                                                            (unscaled)
Objective ...:
              1.4999999925191814e+00
                                        1.4999999925191814e+00
Dual infeasibility...:
                                                 2.0424918385704731e-16
                       2.0424918385704731e-16
Constraint violation ...:
                                                   0.000000000000000e+00
                         0.000000000000000e+00
Variable bound violation:
                            0.000000000000000e+00
                                                      0.000000000000000e+00
Complementarity...:
                    2.5191812953934411e-09
                                              2.5191812953934411e-09
Overall NLP error...:
                      2.5191812953934411e-09
                                                2.5191812953934411e-09
Number of objective function evaluations
                                                     = 7
                                                     = 7
Number of objective gradient evaluations
Number of equality constraint evaluations
Number of inequality constraint evaluations
Number of equality constraint Jacobian evaluations
Number of inequality constraint Jacobian evaluations = 7
Number of Lagrangian Hessian evaluations
                                                     = 6
Total seconds in IPOPT
                                                     = 0.004
EXIT: Optimal Solution Found.
      solver :
                 t_proc
                              (avg)
                                    t_{	t wall}
                                                  (avg)
                                                           n eval
      nlp_f | 30.00us ( 4.29us) 13.70us ( 1.96us)
                                                                7
      nlp_g
             | 47.00us ( 6.71us) 18.50us ( 2.64us)
                                                                7
 nlp_grad_f
                33.00us ( 4.12us) 15.00us ( 1.88us)
                                                                8
 nlp_hess_l
                18.00us ( 3.00us)
                                    8.90us ( 1.48us)
                                                                6
                22.00us (
                           2.75us) 10.60us (
                                                1.33us)
                                                                8
  nlp_jac_g
                  8.09ms ( 8.09ms)
                                     4.04ms ( 4.04ms)
                                                                1
       total
```

 $\$\ 2\ x\_0\ 2\$$  is not really as bad it looks. Ipopt will recognise this situation as an equality constraint.

The solution is obviously [2,0.5,0.5,1,1]:

```
[9]: print(sol['x'])
      for (i,e) in zip(list(range(n)),[2,0.5,0.5,1,1]):
        assert(abs(sol['x'][i]-e)<1e-7)</pre>
     [2, 0.5, 0.5, 1, 1]
     4 Problem with parameters
             (x-a)^2 \setminus \text{subject to } -10 \le x \le 10 \setminus 10^{-6}
     with x scalar
[10]: x=SX.sym('x')
      a=SX.sym('a')
      a = 2
      nlp={(x':x, 'p':a, 'f':(x-a)**2}
[11]: solver = nlpsol('solver', 'ipopt', nlp)
      sol = solver(lbx=-10, ubx=10, p=a_)
     This is Ipopt version 3.14.11, running with linear solver MUMPS 5.4.1.
     Number of nonzeros in equality constraint Jacobian ...:
     Number of nonzeros in inequality constraint Jacobian .:
                                                                     0
     Number of nonzeros in Lagrangian Hessian...:
     Total number of variables...:
                           variables with only lower bounds:
                                                                     0
                      variables with lower and upper bounds:
                                                                     1
                           variables with only upper bounds:
                                                                     0
     Total number of equality constraints...:
     Total number of inequality constraints...:
              inequality constraints with only lower bounds:
                                                                     0
        inequality constraints with lower and upper bounds:
                                                                     0
             inequality constraints with only upper bounds:
                                                                     0
                                    inf_du lg(mu) ||d|| lg(rg) alpha_du alpha_pr ls
     iter
             objective
                           inf_pr
        0 4.0000000e+00 0.00e+00 4.00e+00 -1.0 0.00e+00
                                                               - 0.00e+00 0.00e+00
        1 3.3057851e-02 0.00e+00 5.64e-02 -1.0 1.82e+00
                                                               - 8.45e-01 1.00e+00f
        2 2.8894889e-05 0.00e+00 1.53e-16 -1.0 1.76e-01
                                                               - 1.00e+00 1.00e+00f
        3 4.4774726e-09 0.00e+00 1.08e-16 -2.5 5.31e-03
                                                               - 1.00e+00 1.00e+00f
        4 9.8332283e-12 0.00e+00 2.02e-16 -3.8 6.38e-05
                                                               - 1.00e+00 1.00e+00f
        5 1.4777036e-15 0.00e+00 3.79e-18 -5.7 3.10e-06
                                                               - 1.00e+00 1.00e+00f 1
        6 2.7255842e-21 0.00e+00 1.26e-17 -8.6 3.84e-08
                                                               - 1.00e+00 1.00e+00f 1
     Number of Iterations...: 6
```

(unscaled)

(scaled)

1.2569571890559792e-17 1.2569571890559792e-17 Dual infeasibility...: Constraint violation...: 0.000000000000000e+00 0.000000000000000e+00 Variable bound violation: 0.000000000000000e+00 0.0000000000000000e+00 Complementarity...: 2.5059124009153784e-09 2.5059124009153784e-09 Overall NLP error...: 2.5059124009153784e-09 2.5059124009153784e-09 Number of objective function evaluations Number of objective gradient evaluations Number of equality constraint evaluations Number of inequality constraint evaluations Number of equality constraint Jacobian evaluations Number of inequality constraint Jacobian evaluations = 0 Number of Lagrangian Hessian evaluations = 0.003Total seconds in IPOPT EXIT: Optimal Solution Found. solver : t\_proc t\_wall (avg) (avg) n eval nlp f | 42.00us ( 6.00us) 16.50us ( 2.36us) 7 nlp grad f | 29.00us ( 3.62us) 12.90us ( 1.61us) 8 nlp\_hess\_l | 16.00us ( 2.67us) 8.00us ( 1.33us) 6 total 6.11ms ( 6.11ms) 3.06ms ( 3.06ms) 1 The solution is obviously a: [12]: print(sol['x']) assert(abs(sol['x']-a\_)<1e-9)</pre> 2 The parameter can change inbetween two solve calls: [13]:  $sol = solver(lbx=-10, ubx=10, p=2*a_)$ This is Ipopt version 3.14.11, running with linear solver MUMPS 5.4.1. Number of nonzeros in equality constraint Jacobian ...: Number of nonzeros in inequality constraint Jacobian.: 0 Number of nonzeros in Lagrangian Hessian ...: Total number of variables...: variables with only lower bounds: 0 variables with lower and upper bounds: 1 variables with only upper bounds: 0 Total number of equality constraints...: Total number of inequality constraints ...: inequality constraints with only lower bounds: 0 inequality constraints with lower and upper bounds:

2.7255841628426173e-21

Objective ...:

2.7255841628426173e-21

Number of Iterations...: 6

(scaled) (unscaled)

Complementarity...: 2.5059305083202185e-09 2.5059305083202185e-09 Overall NLP error...: 2.5059305083202185e-09 2.5059305083202185e-09

```
Number of objective function evaluations = 7

Number of objective gradient evaluations = 7

Number of equality constraint evaluations = 0

Number of inequality constraint evaluations = 0

Number of equality constraint Jacobian evaluations = 0

Number of inequality constraint Jacobian evaluations = 0

Number of Lagrangian Hessian evaluations = 6

Total seconds in IPOPT = 0.003
```

EXIT: Optimal Solution Found.

```
solver :
               t_proc
                           (avg)
                                  t_{wall}
                                             (avg)
                                                      n eval
    nlp_f | 90.00us ( 6.43us) 35.40us ( 2.53us)
                                                          14
 nlp grad |
               5.00us ( 5.00us)
                                 2.80us ( 2.80us)
                                                          1
nlp_grad_f | 55.00us ( 3.44us) 26.10us ( 1.63us)
                                                          16
nlp hess 1 |
              33.00us ( 2.75us) 16.70us ( 1.39us)
                                                          12
    total |
               7.40ms ( 7.40ms)
                                  3.81ms ( 3.81ms)
                                                           1
```

The solution is obviously 2\*a:

```
[14]: print(sol['x'])
assert(abs(sol['x']-2*a_)<1e-9)
```

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