### FRB 121102: MULTI-TELESCOPE BURST PROPERTIES AND IMPLICATIONS FOR FRB POPULATION

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### ABSTRACT

The millisecond radio transients known as Fast Radio Bursts have recently emerged as a mysterious, new class of astrophysical transient. The discovery of repeating bursts from FRB 121102 has shown that at least some FRBs are not cataclysmic and opened potential for studying FRB properties via a homogenous sample of bursts. The recent localization of FRB 121102 with the Very Large Array has helped measure its distance and a host of intrinsic properties. This localization was made with 9 bursts seen by the VLA in coordination the Arecibo, Effelsberg, and AMI-LA observatories. We present a detailed analysis of these bursts, including the first simultaneous detection of an FRB with multiple telescopes. We show that the burst spectra typically have a broad Gaussian shape on the scale of  $\sim 500$  MHz with fine spectral structure consistent with either scintillation or unresolved temporal structure. We present the luminosity distribution and temporal statistics for FRB 121102 and argue that the whole FRB population is adequately described by a single class similar to FRB 121102. We close with thoughts on optimal strategies to make new interferometric localizations of FRBs.

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### 1. INTRODUCTION

Fast Radio Bursts (FRBs) are a new class of millisecond-duration radio transient with a dispersion measure (DM) that implies that they originate outside of our Galaxy. At extragalactic (and potentially cosmological) distances, they are not only unusually luminous, but they provide a new tracer of other galaxies and the intergalactic medium (IGM). In this way, FRBs have opened a whole new playground in astrophysics (e.g., Falcke & Rezzolla 2014; McQuinn 2014; Cordes & Wasserman 2016). However, that potential has been hamstrung by the lack of a definitive association of an FRB to an extragalactic host.

This paper is part of a series that presents the first localization and host identification of an FRB (CITE: LOC, OPT, EVN, RADIO CPART, XRAY, EFF, WEIRD). FRB 121102, also known as the "repeating FRB", was first detected in November 2012 by the Arecibo Observatory (Spitler et al. 2014). In mid 2015, new Arecibo observations revealed a series of bursts at the same DM and sky position demonstrating that FRBs are capable of repetition (Spitler et al. 2016). Beginning in August of 2015, we made the first of nine detections of FRB 121102 with the Very Large Array (CITE: LOC) and localized it with a precision of 0.1". Deep radio and optical observing shows that FRB 121102 is unambiguously associated with a persistent radio and optical source at a redshift of 0.193 (CITE: OPT, EVN).

FRB 121102 has now been localized three orders of magnitude better than any other FRB and placed at a cosmological distance. Its lookback and luminosity distances are 746 and 972 Mpc (?), which are orders of magnitude larger than any other millisecond transient. This shows that FRBs:

- ullet are extremely luminous,
- have a significant DM contribution from the IGM,
- can be used to probe the IGM and their host galaxy.

The promise implied by the first reported FRB (Lorimer et al. 2007) is now being realized.

The cosmological distance for FRB 121102 could have wide-ranging implications for the FRB population as a whole. However, it has not been demonstrated that FRB 121102 is representative of the overall FRB population. In fact, the repetition of its bursts is unique among all FRBs (Petroff et al. 2015), so it is natural to ask whether FRB 121102 is representative. An important first step is to demonstrate that the properties of FRB 121102 are consistent with the significant body of facts for the

overall population (Macquart & Johnston 2015; Katz 2016). The repeating nature of FRB 121102 provides us with several statistical tests we can use to test this connection.

We can also assume that FRB 121102 is representative and use it to constrain the physical processes at play in the overall FRB population. Although we now know that FRBs are luminous, it is not yet clear what process generates the radio bursts themselves (Katz 2014; Luan & Goldreich 2014; Cordes & Wasserman 2016). The simultaneous FRB 121102 observing campaign with the VLA, Arecibo, Effelsberg, GBT, and AMI-LA gives a more complete picture of the spectral structure of FRB radio emission. FRB repetition also has strong implications for the number of FRB-generating systems in the universe (Connor et al. 2016).

Given that FRBs are now known to be useful probes of the IGM, there is strong justification for continuing searches for new detections and localizations. The relatively faint counterpart to FRB 121102 argues that direct localization of the radio burst will continue to be the best way to find optical hosts to measure distances. Our multi-telescope constraints on burst spectra, measurement of host properties, burst rate estimates, and other properties will inform new strategies for finding FRBs...

# 2. OBSERVATIONS

The data presented here were obtained from multiple programs and telescopes, but the central goal was to interferometrically localize FRB 121102 with the VLA. The observing strategy was to ensure simultaneous observing between the VLA and Arecibo observatories and add other observatories added on a best-effort basis. We coordinated observing between the VLA, Arecibo, Effelsberg, and AMI-LA telescopes, as shown in figure 1. Below, we summarize these observations, with a focus on those conducted simultaneous with VLA burst detections from FRB 121102.

## 2.1. VLA

The FRB 121102 observing campaign started in late 2015 with a 10 hr campaign observed at 1.4 GHz in the compact D configuration. In April through May 2016, we conducted a 40 hr campaign at 3 GHz in the C and CnB configurations in coordination with Arecibo. We concluded with a new, 40 hr, coordinated campaign from August through September 2016 in the B configuration and during the move to the most extended A configuration. In this last campaign, the first 34 hours of VLA observations were made at 3 GHz, while the last 6 hours were observed at 6 GHz. This paper focuses on the data collected at 3 GHz, which includes all burst detections.

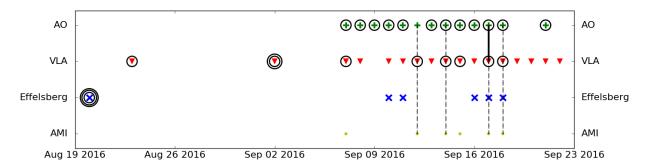


Figure 1. Summary of observing coverage and detections of FRB 121102 during the multi-telescope observing campaign. Symbols show days with observations and symbols with circles show detections of FRB 121102. Multiple circles indicate multiple burst detections, except for Arecibo, which typically has multiple detections per observing session (a detailed analysis is left for a future paper). The black dashed lines show the VLA burst detections with simultaneous coverage at other telescopes. The solid black line shows the simultaneous burst detection at VLA and Arecibo.

All VLA fast-sampled data were observed with 5 ms sampling, 256 channels, and dual-circular polarization (Law et al. 2015, as in). To maximize sensitivity, the channel frequency width was set to maintain sensitivity to the known DM of FRB 121102, while maximizing the total bandwidth. The total bandwidth at L (1.4 GHz), S (3 GHz), and C (6 GHz) bands was 256 MHz, 1024 MHz, and 2048 MHz, respectively. The 3 GHz data recorded data in 8 spectral windows with 32 channels each.

Observations in August and Septmeber were searched by a prototype version of  $realfast^1$ . realfast is a realtime, fast imaging transient search system. The current, prototype runs on existing, CPU-based hardware of the VLA correlator backend, while the future realfast will run on a dedicated GPU cluster. The transient search pipeline software is called  $rtpipe^2$  and is mostly written in Python. The transient search pipeline is described in Law et al. (2015) and performs data calibration, flagging, dedispersion, and imaging. Images were formed for each integration at DMs of 0, 546, 556.9, 560, and 565 pc cm<sup>-3</sup>. Gain calibration is read from the "telcal" system, which uses phase-only calibration on the previous gain calibrator. A flux scale is calculated for each spectral window from an observation on xx (Bryan) and applied to all burst spectra.

Burst detections and localizations were made within hours of data being recorded. The transient search starts when data are recorded, but this prototype of re-alfast is a factor of several times slower than real-time, so we refer to the detection as "quasi real-time". Each image with a pixel higher than  $6.4\sigma$  has some rudimentary data saved to capture both real and thermal-noise

candidates as a check of data quality. For each image with a pixel higher than  $7.4\sigma$ , realfast generates a candidate visualization with an image and spectrum. More detailed analysis, including improved calibration and localization, is conducted offline.

Computational notebooks to reproduce the transient detection and localization can be found at https://github.com/caseyjlaw/FRB121102. Time cut-out visibility data are available at https://doi.org/10.7910/DVN/TLDKXG. Original visibility data are available under VLA program codes 16A-459 and 16A-496 and can be downloaded at http://archive.nrao.edu.

# 2.2. Arecibo

During the joint Arecibo-VLA campaign, Arecibo observed with the L-wide receiver, which has an observational frequency range of 1.15 to 1.73 GHz and a full width at half maximum beam size of 3.3 arcmin. The PUPPI pulsar backend was used to record total intensity spectra with time and frequency resolutions of 10.24  $\mu$ s and 1.5625 MHz, respectively, and full Stokes polarization information. Each frequency channel was coherently dedispersed to 557 pc cm<sup>-3</sup>, thereby eliminating intra-channel dispersion smearing. PUPPI covers a total of 800 MHz of bandwidth centred at 1380.78125 MHz, but only  $\sim$  620 MHz of this band is usable due to radio frequency interference and receiver sensitivity roll-off at the band edges.

In total, twelve Arecibo observations had some simultaneous coverage with the VLA. Four of those observations were simultaneous with bursts detected with the VLA and one of those observations detected the same VLA burst. During the first VLA burst with Arecibo coverage (MJD 57643), the PUPPI system failed so data were recorded with xx (Jason?) at C band. No detection was made in that Arecibo data. Overall, there were

See http://realfast.io.

<sup>&</sup>lt;sup>2</sup> See https://github.com/caseyjlaw/rtpipe

many more bursts detected at Arecibo and a more detailed analysis will be presented in a future paper.

# 2.3. Effelsberg

Observations were conducted at an observing frequency of 4.6 to 5.1 GHz. The S60mm receiver has a system equivalent flux density of 18 Jy and a full-width half-max (FWHM) beam size of 2.4'at 4.85 GHz. Pulsar search mode data were recorded with the PFFTS backend. Total intensity spectra were recorded with a time resolution of 65.5  $\mu$ s and a bandwidth of 500 MHz divided into 128 frequency channels. Note, the interchannel DM smearing time for 560 pc cm<sup>-3</sup> is ~0.2 msec at 4.6 GHz.

Five Effelsberg observations had some simultaneous coverage with the VLA, of which two were simultaneous with VLA bursts. Unfortunately, due to a configuration error, a 100 MHz bandwidth filter centered at 4.85 GHz was in place for both of these sessions. The sensitivity was about two times worse than the nominal value. No burst was detected in either observation.

## 2.4. AMI

# Kunal to provide description of AMI-LA

Six AMI-LA observations had some simultaneous coverage with the VLA, of which four covered VLA bursts. The upper limit on burst flux density limits any significant "afterglow". Deep image sensitivity is limited by confusion and is approximately equal to the flux density observed by VLA (CITE: RADIO CPART). Details from Kunal

# 3. RESULTS

# 3.1. Multi-Telescope Burst Spectrum

Of the four VLA burst detections from FRB 121102with simultaneous observations FRB 121102(Figure 1), one was detected with a consistent dedispersed time. The VLA burst on 57648 was detected at Arecibo with a significance of  $xx\sigma$  (Jason) The relative time delay between the VLA and Arecibo is xx (Jason) ms...

Figure \*\*to do\*\* shows the dynamic spectrum formed from the phased VLA and Arecibo data... This simultaneous detection of a burst from roughly 1 to 4 GHz shows that some bursts cover more than an octave of frequency. This is one of three bursts with similar spectral coverage at Arecibo, so the other nondetections imply that those bursts had a smaller spectral coverage. In fact, as described in §3.2.1, most of the VLA bursts appear to be fully contained in the band from 2.5 to 3.5 GHz, which implies a much smaller spectral coverage for typical bursts.

\*\*Insert figure of VLA/AO dynamic spectrum on 57648\*\*

### 3.2. VLA Bursts

## 3.2.1. Dynamic Spectra

Figure 2 shows the spectrograms of all nine bursts detected by the VLA. We improved on the initial analysis presented in (CITE: LOC) by using a better calibration scheme and optimizing the image SNR over a fine DM grid. Table 1 shows the improved burst parameters using this new scheme.

## 3.2.2. Dispersion Meausres

The initial VLA detections were made by searching a DM grid that allowed inter-DM sensitivity losses up to roughly 10%. For the VLA 3 GHz observing band, we estimated that trials could be separated by at most 10 pc cm<sup>-3</sup> (Cordes & McLaughlin 2003). We refined that analysis by maximizing the image SNR for DMs spaced by 1 pc cm<sup>-3</sup>. The optimal DM values range from 552 to 572 pc cm<sup>-3</sup> for all bursts and from 552 to 561 pc cm<sup>-3</sup> for bursts with SNR> 30.

The uncertainty in the peak DM measurement is defined by the DM sensitivity loss curve and the significance of the burst. We tested this model by simulating a burst with SNR= 30 and measuring its detection significance as a function of DM. The simulation parameters were reproduced at the known DM with a precision of roughly 1 pc cm<sup>-3</sup>. This suggests that the measured variation in DM for FRB 121102is intrinsic to the bursts, rather than due to measurement uncertainty. This is consistent with the observation of intrinsic burst spectrotemporal structure that varies between bursts (CITE: WEIRD).

## 3.2.3. Spectral modeling

After finding an optimal burst DM, we extract a spectrum from the integration with peak SNR (Figure 3). After DM optimization, all bursts appear unresolved at the 5 ms time resolution of the VLA data (except maybe 57633.68, brightest burst).

The burst spectra are generally characterized by a broad, Gaussian shape that with strong modulation between channels. We fit a Gaussian shape to each burst to estimate their characteristic width and peak flux, as summarized in Table 1. The channel-scale modulation is as high as 100% (see §3.2.4) and is consistent with an exponential distribution. While this introduces a strong bias to the best-fit Gaussian, the typical burst spectral width has a characteristic width of 500 MHz.

All but two of the best-fit Gaussians are centered inside the 3 GHz band and most are fully contained by the 1 GHz wide band. This is consistent with previous detections of FRB 121102by Arecibo, which showed quasi-broadband structure (?) and large variation in the

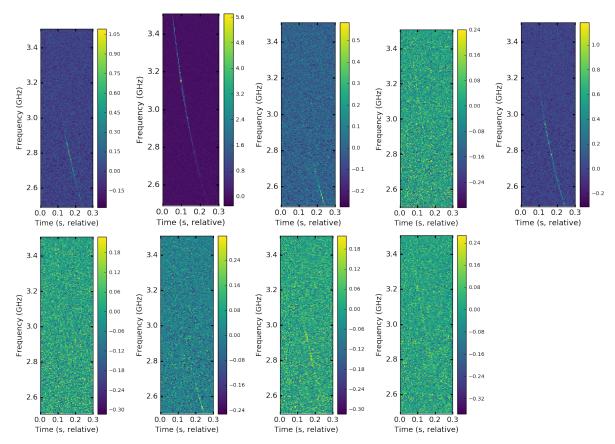


Figure 2. Spectrograms (time vs frequency intensity maps) for the nine VLA bursts. Starting at the top left, the correspond to bursts 57623, 57633.68, 57633.70, 57638, 57643, 57645, 57646, 57648, and 57649. Note that bursts are detected in 5 ms images generated from dedispersed visibilities.

implied spectral index (Spitler et al. 2014). A detailed discussion of FRB 121102 burst spectra is presented in (CITE: WEIRD).

# 3.2.4. Spectral Autocorrelation

Autocorrelation of the burst signal (both temporal and spectral) can be used to infer both intrinsic properties and modulation due to scintillation (CITE: Cordes et al?). The VLA data have a channel resolution of 4 MHz, which is relatively coarse compared to single-dish data (e.g., CITE: WEIRD). However, diffractive scintillation observed for other FRBs () could/could not (Jim?) induce structure on this scale near 3 GHz.

Figure 4 shows the spectral autocorrellation for the strongest burst (MJD 57633.68). (Marginal evidence of spectral correlation on the scale of 4 MHz) Comment, Jim?

### 3.2.5. Circular Polarization

The VLA S-band recievers natively measure circular polarization, although observations did not include polarization calibration procedures. Crude constraints on circular polarization are possible by comparing the

burst intensity in right and left-hand polarized data products. The apparent circular polarization fraction ((RR-LL)/(RR+LL)) for the most significant bursts are all less than 3%. FRB121102 was located 2.3 arcmin away from pointing center, where systematic effects have been measured as large as 3% (Perley et al 2016, VLA memo). We conclude that the S-band bursts seen by the VLA have a circular polarization of less than 3%.

### 3.3. Temporal Statistics

Periodicity search... Figure 5 shows a Lomb-Scargle periodogram... Lots of excess power corresponding to periods shorter than 1 hour.

Burst detections were made very inhomogenously through the roughly 63 hours of observing toward FRB 121102. In the first 30 hours of observing at S-band no bursts were detected, while nine bursts were detected in the last 27 hours of S-band observing. The data quality is high and RFI did not significantly impact sensitivity, so the inhomogeneous burst distribution is not an observational artifact, but rather an indication of a non-stationary burst detection probability. Assuming that the burst detection probability follows a Poisson

Date	$S_{\mathrm{int}}$	Image SNR	$\mathcal{L}_{\mathrm{int}}$	$\mathrm{DM}_{\mathrm{opt}}$	$S_{\mathrm{peak}}$	Center	FWHM
(MJD)	(mJy)		(ergs?)	$(pc cm^{-3})$	(mJy?)	(GHz)	(MHz)
57623	258	38		561	0.41	2.8	300
57633.68	2000	179		554	1.90	3.2	520
57633.70	105	15		559	>0.188	< 2.5	>350
57638	65	12		556	0.07	3.1	410
57643	375	100		560	0.39	2.8	520
57645	38	13		572	0.06	2.8	210
57646	69	20		555	>0.16	< 2.5	>400
$57648^{\rm a}$	97		25	559	0.11	2.9	420
57649	110	36		552	0.07	2.9	880

**Table 1.** Properties of Bursts from FRB 121102

distribution, the nondetection in the first half of S-band limits the FRB rate to  $R < 0.1 \; hour^{-1}$  (95% confidence limit). The mean detection rate for the last part of the campaign was  $R = 0.3 \; hour^{-1}$ .

Moreover, there is weak evidence that the FRB 121102 burst rate changes during the last part of the campaign. We modeled the event detection probability as a Poisson probability with a rate parameter that scales linearly with time (relative to first burst detection) as  $\lambda = a + b*(MJD-57623)$ . We then calculated the probability of measuring the observed event rate as  $\prod_i P_i(R)$ . Figure 6 shows the (a, b) parameter space with contours of 50, 90, and 95% confidence contours.

### 3.4. Brightness Distribution

Table 1 shows burst luminosities... The significance of the nine bursts span more than an order of magnitude (12 to  $179\sigma$ ). This highlights the fact that the bursts have a relatively flat luminosity distribution.

Figure 7 shows the flux distribution of the nine VLA bursts. Quantify flatness...

Compare luminosity distribution to flux distribution measured by (Vedantham et al. 2016)...

# 4. DISCUSSION

### 4.1. Luminosity Distribution

Doubts were cast on the first FRB detection ("Lorimer burst") due to its unusually high brightness. The lack of lower-significance detections suggested that this burst was unlikely to be part of any astrophysical population. With more detections, it has become clear that the FRB population has a relatively flat flux distribution (Vedantham et al. 2016; Lawrence et al. 2016). This fact was demonstrated with yet another detection of an extremely bright FRB (Ravi et al. 2016).

Discuss comparison FRB 121102 luminosity distribution to that of FRB population... Imagine physical log N/log S with cut-offs and scattering can bias the intrinsic into the observed distribution (Macquart and Johnston)...

## 4.2. Repetition

Discussion of "red spectrum" and Connor et al. (2016). Bursts predict bursts therefore repetition constraints of other FRBs are likely weaker than claimed...

Constraints on repetition assuming "red spectrum" for whole population. Simulation using observed burst temporal statistics...

Intrinsic versus refractive scintillation...

Fewer FRBs out there...

## 4.3. Emission Physics and Burst Energetics

For a nominal Gpc distance D corresponding to redshifts  $z \lesssim 0.3$ , the received fluence  $A_{\nu}$  from each burst implies a burst energy

$$E_{\rm burst} = 4\pi D^2 (\delta\Omega/4\pi) A_\nu \Delta\nu \approx 10^{38}\,{\rm erg}\,(\delta\Omega/4\pi) D_{\rm Gpc}^2(A_\nu/0.1\,{\rm Jy~m})$$

The unknown emission solid angle  $\delta\Omega$  could be very small due to relativistic beaming, and together with a distance possibly much smaller than 1 Gpc, could reduce the energy requirement significantly. However, the total energy emitted could be larger depending on the duration of the emission in the source frame and other model-dependent details. Either way, the burst energies from FRB 121102 are not inconsistent with those that might be expected from the magnetosphere of a compact objectCordes & Wasserman (2016).

# 4.4. Observing Strategies

<sup>&</sup>lt;sup>a</sup>Detected simultaneously with Arecibo between 1.15 and 1.73 GHz.

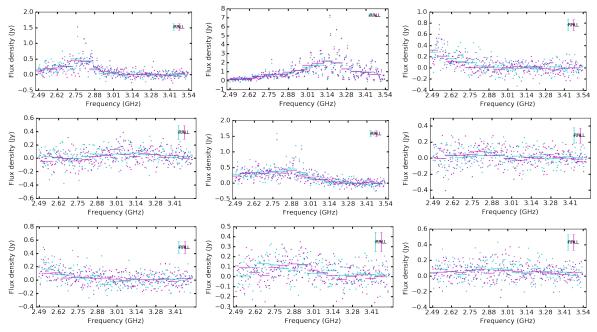
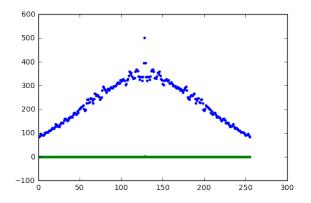
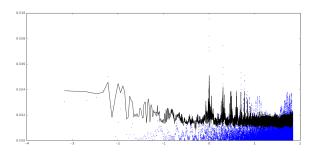


Figure 3. Spectra of nine bursts seen by the VLA from 2.5 to 3.5 GHz. Orthongonal circular polarizations (RR and LL) are plotted separately. \*\*LABELS ALL SAME FREQ. SOME SHOULD START HIGHER FOR DROPPED CHANNELS\*\*



**Figure 4.** The spectral autocorrelation for the burst from FRB 121102 at MJD 57633.68. Blue shows the autocorrelation for the burst and green shows an autocorrelation of a representative spectrum with no burst.



**Figure 5.** Lomb-Scargle periodogram with 95% limit on power from last observing campaign

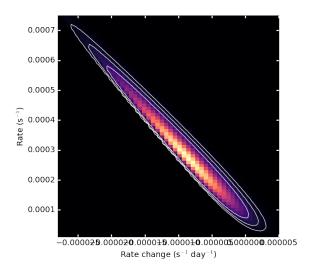


Figure 6. Rate versus rate change during last campaign.

Repetition implies that targeting known FRBs is optimal.

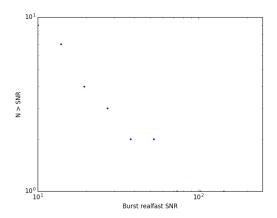


Figure 7. Log N – Log SNR distribution of real-time detections of FRB 121102. \*\*Update to luminosity distribution\*\*

Repetition and shallow luminosity distribution show that shallow and wide is the best way to blindly find FRBs.

Given that bursts have < 1 GHz-scale spectra, wide bandwidths improve odds of detection.

## 5. CONCLUSIONS

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