Long Title

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FLINT

Introduction

Simple List

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- Item.

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  - Sub Item.

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Image

Allignment 1

$$\sum_{i,j}^{n} \mathbb{E}_{i,j} = \sum_{i,j \neq i}^{n} \mathbb{E}_{i,j} + \sum_{i}^{n} \mathbb{E}_{i,i}$$

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&= \frac{1}{s-1}\left[\sum_{i}^{n} k_i \sum_{j\neq i}^{n} k_j + \sum_{i}^{n} k_i \sum_{i}^{n} k_i - \sum_{i}^{n} k_i\right] \\
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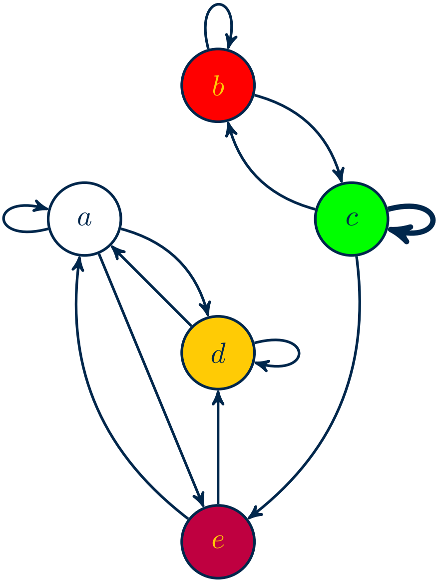
- Note: $\delta(c_i, c_i) = 1$.

$$Q = \frac{1}{s}\left[\sum_{i,j\neq i}^{n}\left(A_{i,j} - \frac{k_i k_j}{s-1}\right)\delta(c_i, c_j) \right.$$
$$\left. + \sum_{i}^{n}\left(A_{i,i} - \frac{k_i(k_i-1)}{s-1}\right)\right].$$

Algorithms

TikZ



Matrix

$\vec{A}$	a	b	c	d	e
a	1	0	0	1	1
b	0	1	1	0	0
c	0	1	2	0	1
d	1	0	0	1	0
e	1	0	0	1	0

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The adjacency matrix is the expected form computers will store networks in.

Colored Table

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$merge$	$\partial\vec{Q}_i$	$\partial\vec{Q}_j$	$\partial\vec{Q}_{i'}$	$\Delta\vec{Q}$
$\{a, d\}$	$4/13$	$7/13$	$22/13$	$11/169$
$\{a, e\}$	$4/13$	$-4/13$	$14/13$	$14/169$
$\{b, c\}$	$9/13$	$14/13$	$35/13$	$12/169$
$\{c, e\}$	$14/13$	$-4/13$	$9/13$	$-1/169$
$\{d, e\}$	$7/13$	$-4/13$	$6/13$	$3/169$

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$\{c,e\}$	$14/13$	$-4/13$	$9/13$	$-1/169$
$\{d,e\}$	$7/13$	$-4/13$	$6/13$	$3/169$

The best merge for nodes a, and e, is to merge them together, similarly, the best for b, and c, is to merge them together, last, the best merge for d is to merge it with a.

Conclusion

We truly covered a lot, and yet this is only a glimpse.

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QUESTIONS?

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References [1/4]

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