

MTH 372

Hw 7

Due Thursday, 11/4/2021.

Read Chapters 14,15 of *Huber*.

A. (We began this problem in class on 10/19.) Flip 3 fair coins, A,B,C.

Let  $X$  be the total numbers of heads on coins A and B. Let  $Y$  be the total number of heads on coins B and C.

- (a) Write out the table of the joint pmf  $p_{X,Y}(x,y)$ .
- (b) Compute  $\sigma_X^2$ ,  $\sigma_Y^2$ .
- (c) Compute  $\text{Cov}(X,Y)$  and  $\rho_{X,Y}$ .

p.99 #14.4 Let  $Y$  have pmf  $p_Y(i) = \begin{cases} 1/4 & \text{for } i \in \{3, 5\} \\ 1/6 & \text{for } i \in \{7, 9, 11\} \end{cases}$ .

- (a) Find  $E[Y]$ .
- (b) Find  $\sigma_Y$ .

#14.8 (modified)

Suppose  $(X,Y)$  have joint density  $f_{X,Y}(x,y) = (2/5)(3x+2y)$  for  $(x,y) \in [0,1]^2$

- (a) Compute  $P(X > .5 \text{ and } Y < .6)$ .
- (b) Find the marginal pdf's  $f_X(x)$  and  $f_Y(y)$ .
- (b) What is  $\text{Cov}(X,Y)$ ?

p.104 #15.1 For  $(X,Y) \sim \text{Unif}(\{(0;0); (0;2); (1;2)\})$ , find the correlation between  $X$  and  $Y$ .

#15.2 For  $(X,Y)$  with density  $f_{X,Y}(x,y) = 2\exp(-x-2y)$  for  $x,y \geq 0$ , find  $\rho_{X,Y}$ .  
(Hint: You can solve this problem without any integration.)

#15.3 (modified) Let  $f_{X,Y}(r,s) = \frac{1}{C} \cdot \frac{r^4 + s}{r^2}$  for  $r \in [1,3], s \in [0,3]$ .

- (a) Find the value of  $C$ .
- (b) Compute  $P(X > 2)$ ,  $P(Y > 1)$  and  $P(X > 2 \text{ and } Y > 1)$ . Are  $X,Y$  independent?
- (b) Find the density of  $Y$ ,  $f_Y(s)$ .
- (c) Find  $\rho_{X,Y}$ .