MTH 385 Homework due 2022-03-21

Exercise 1 (5.5.2). Use Cardano's formula to solve $y^3 = 2$. Do you get the obvious solution?

Exercise 2 (5.5.3). Use Cardano's formula to solve $y^3 = 6y + 6$, and check your answer by substitution.

Exercise 3 (5.6.2). Use (3) and $\sin \alpha = \cos(\pi/2 - \alpha)$, $\cos \alpha = \sin(\pi/2 - \alpha)$ to show that

$$(\sin \theta + i \cos \theta)^n = \begin{cases} \sin n\theta + i \cos n\theta & when \ n = 4m + 1 \\ -\sin n\theta - i \cos n\theta & when \ n = 4m + 3. \end{cases}$$

Exercise 4 (5.6.3). Deduce from Exercise 5.6.2 that (2) is correct for n = 4m + 1 and false for n = 4m + 3, and hence that (1) is a correct relation between $y = \sin n\theta$ and $x = \sin \theta$ only when n = 4m + 1.

Exercise 5 (5.6.4). Show that (1) is a correct relation between $y = \cos n\theta$ and $x = \cos \theta$ for all n (de Moivre (1730)).