

Exploring Machine Learning

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1. Introduction

Economists have long been interested in the discussion of what factors influence a person's income. In more recent times, machine learning techniques have become one tool

Machine learning race is a topic that has ... One of the uses of machine learning is it can be used to classify data.

This paper is split into two main parts: part 1 [3](#) applies machine learning techniques to the NIDS dataset [2](#) and part 2 [4](#) makes use of sequel to manipulate the NIDS dataset. The machine learning section first compares the effectiveness of linear regression and regularised regression on predicting people's incomes. Then 5 classification algorithms - Linear Discriminant Analysis, Classification and Regression Trees, k-Nearest Neighbors, Support Vector Machines with a linear kernel and Random Forest - are evaluated on their accuracy in predicting a person's race.

2. Data

NIDS discussion

3. Machine Learning

3.1. Predicting Income

Econometrics often makes use of regression analysis to model economic phenomena, test economic hypotheses and to forecast economic activity [Studenmund \(2014: 2\)](#). A popular method in econometric regression modeling is that of Ordinary Least Squares; however, advances in machine learning have

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presented alternative/augmenting methods that may be (more) useful. One such augmenting method is K-fold cross validation, which evaluates the skill of machine learning models. As [Rodriguez, Perez & Lozano \(2009: 569\)](#) explain, in K-fold cross validation, a data set is randomly split into k number of groups, of similar sizes. The first group is considered a validation set and the method is fitted to the other $k - 1$ groups.

Below, [3.1](#) displays 3 different linear regressions of log of income using K-fold cross validation. For these regressions I built a function “linreg”, which takes in a data frame, cleans and splits the data into a training (70% of the full data set) and a test set (30% of the full data set) and runs 3 different linear regressions, applying K-fold cross validation. The results of the regressions are then collected and stored in a list, which is returned by the function. I used $k = 10$, because empirically $k=10$ has been shown have test error rate estimates that have relatively low bias and variance ([Kassambara \(2018a\)](#)). I have also set seed in the function for reproducibility.

Based on the Mincerian wage equation, Regression 1 [3.1](#) regresses log of income on age, years of schooling and a dummy variable for if a person has a tertiary qualification or not. Regression 2 includes a variable for age-squared and the categorical variable race. Regression 3 includes a variable each for gender and marriage. The signs of the coefficients of the three regressions look fairly standard¹ and most of the coefficients are statistically significant at 1% and lower.

¹This at least is a good indication that the data is fairly well cleaned and is usable for testing the machine learning techniques

Table 3.1: Log-Income Regression Output

| | Reg 1 | Reg 2 | Reg 3 |
|--------------------|----------------------|----------------------|----------------------|
| (Intercept) | 6.097 *** (0.145) | 5.791 *** (0.367) | 5.526 *** (0.354) |
| age | 0.019 *** (0.002) | 0.041 ** (0.015) | 0.040 ** (0.015) |
| school | 0.127 *** (0.009) | 0.109 *** (0.009) | 0.104 *** (0.008) |
| tertiary | 0.691 *** (0.048) | 0.624 *** (0.046) | 0.594 *** (0.044) |
| age2 | | -0.000 (0.000) | -0.000 * (0.000) |
| ‘raceAsian/Indian’ | | 0.575 *** (0.123) | 0.554 *** (0.117) |
| raceColoured | | 0.023 (0.048) | 0.008 (0.046) |
| raceWhite | | 0.767 *** (0.070) | 0.777 *** (0.066) |
| married | | | 0.317 *** (0.045) |
| male | | | 0.477 *** (0.039) |

*** $p < 0.001$; ** $p < 0.01$; * $p < 0.05$.

Typically, economists are interested in evaluating the performance of a model, which can be done by assessing how well the model predicts the outcome variable. A useful statistical metric for measuring the performance of a regression model is the Root Mean Squared Error (RMSE) ([Kassambara \(2018b\)](#)). The RMSE measures the average error performed by the model in predicting the outcome

for an observation. The mathematical formula for the RMSE is given by

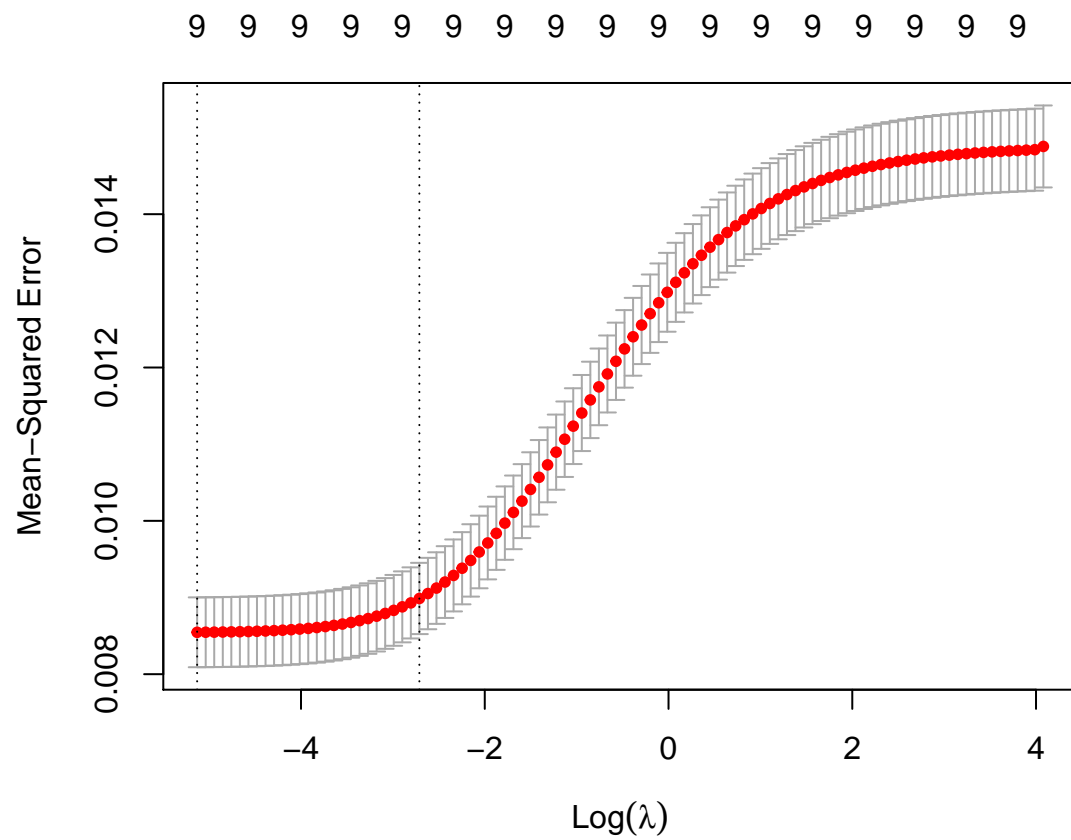
$$RMSE = \sqrt{((observeds - predicted)s^2)/N}$$

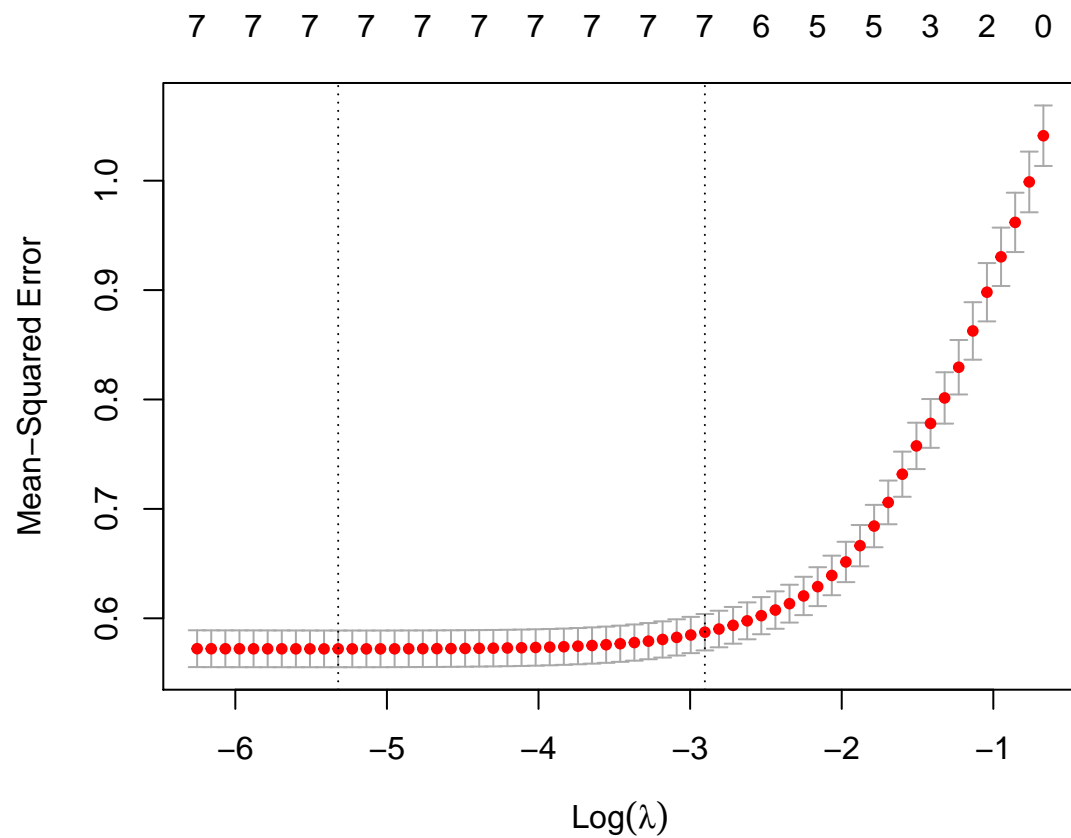
This implies lower the RMSE, the better the model performs.

3.2 reports the RMSES for both the training data and the test data. We can see that the RMSEs decreased from regression 1 to regression 3 for both the training and test data. This indicates that regression 3 is a better model than both regressions 1 and 2 (and that regression 2 has better predictive power than regression 1). The RMSEs

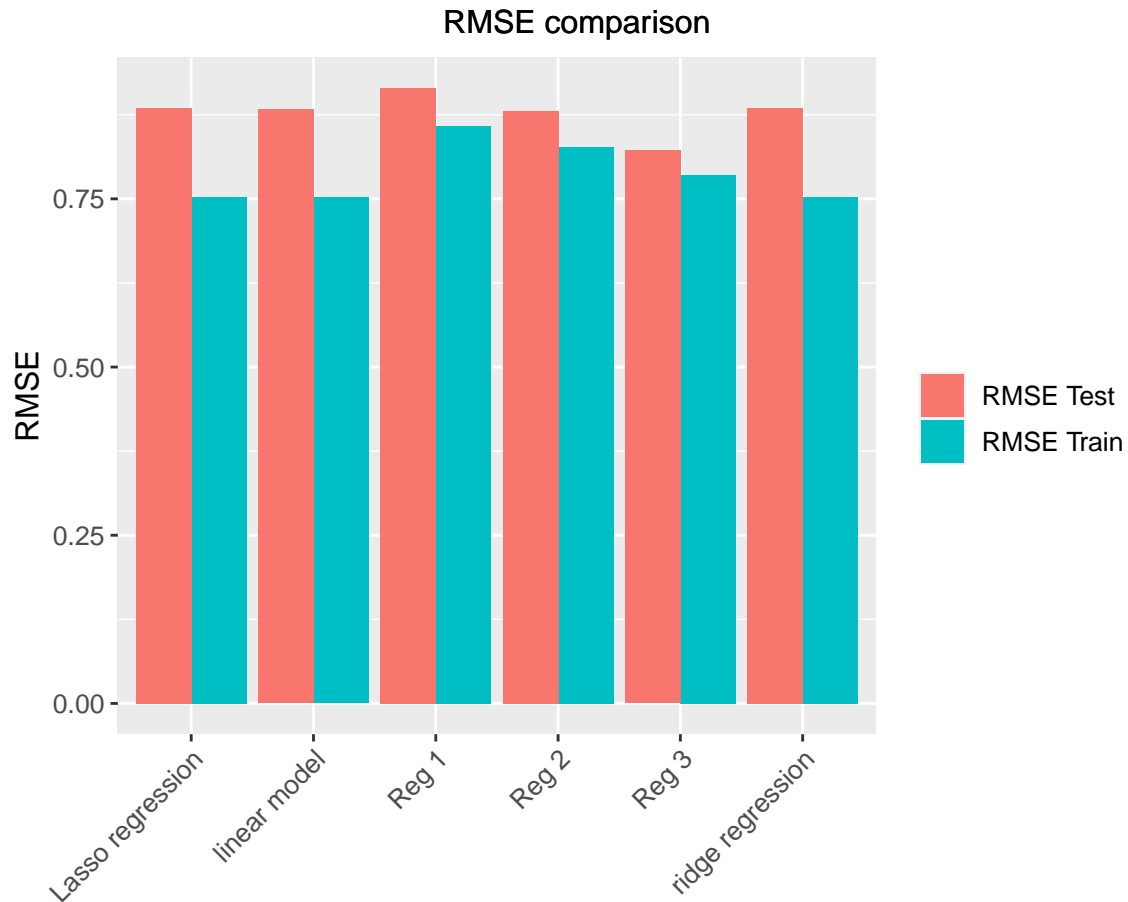
Table 3.2: Regression RMSEs and Observations

| Regression | RMSE Train | RMSE Test |
|------------|------------|-----------|
| Reg 1 | 0.86 | 0.91 |
| Reg 2 | 0.83 | 0.88 |
| Reg 3 | 0.79 | 0.82 |





```
## [1] "RMSE on training set: 0.752131288720079"
## [1] "RMSE on test set: 0.882932895421073"
## [1] "RMSE on training set: 0.752842149603987"
## [1] "RMSE on test set: 0.88481632436016"
## [1] "RMSE on training set: 0.752681521998011"
## [1] "RMSE on test set: 0.885305140817852"
```



```
## NULL
```

```
## [1] "RMSE on training set: 0.752131288720079"
## [1] "RMSE on test set: 0.882932895421073"
## [1] "RMSE on training set: 0.752842149603987"
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## [1] "RMSE on training set: 0.752681521998011"
## [1] "RMSE on test set: 0.885305140817852"
```

```
## \begin{table}[H]
## \centering
## \caption{Model RMSEs}
## \label{RMSE}
## \begin{tabular}{rrrrrr}
```

```

## \hline
## Lasso regression & linear model & Reg 1 & Reg 2 & Reg 3 & ridge regression \\
## \hline
## 0.89 & 0.88 & 0.91 & 0.88 & 0.82 & 0.88 \\
## 0.75 & 0.75 & 0.86 & 0.83 & 0.79 & 0.75 \\
## \hline
## \end{tabular}
## \end{table}

```

3.2. Predicting Race

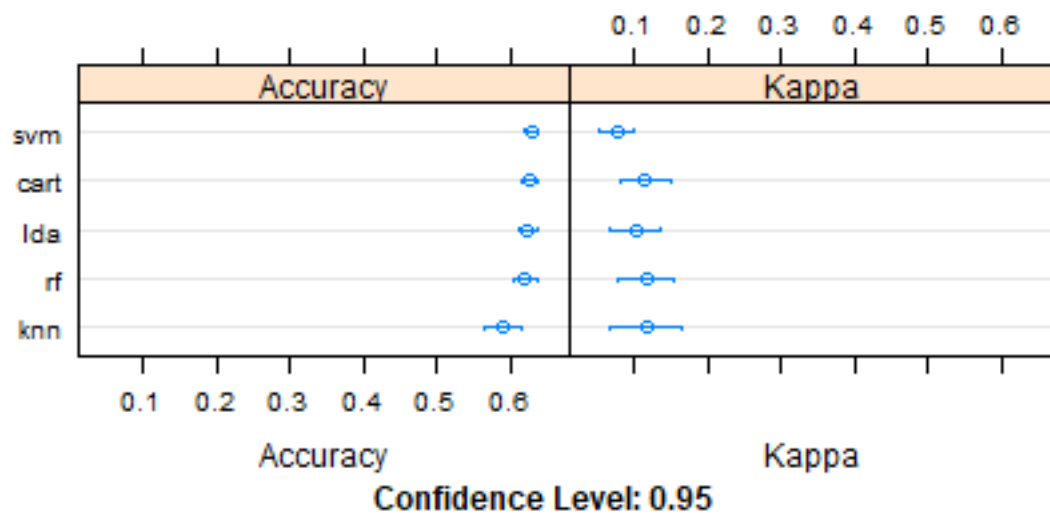


Figure 3.1: ML on

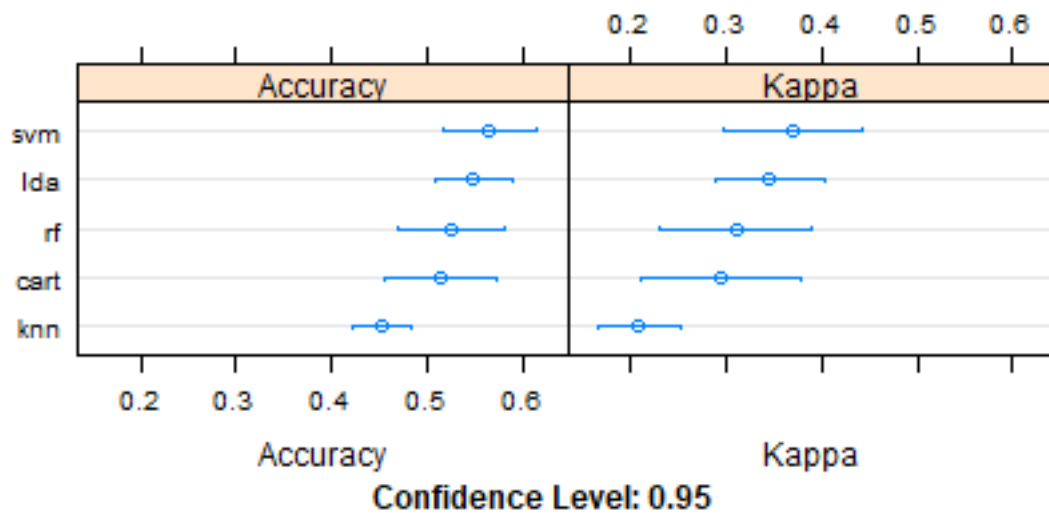


Figure 3.2: ML on

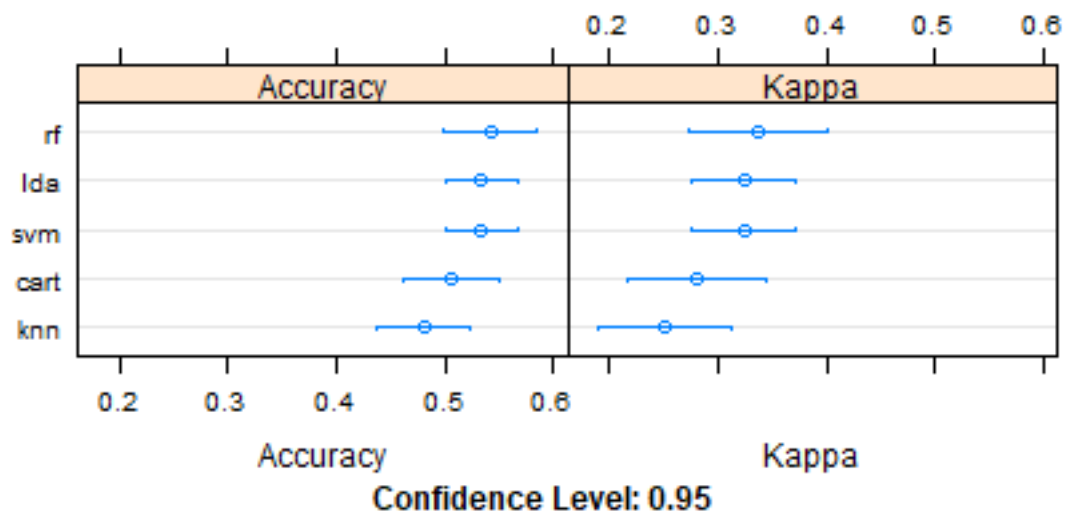
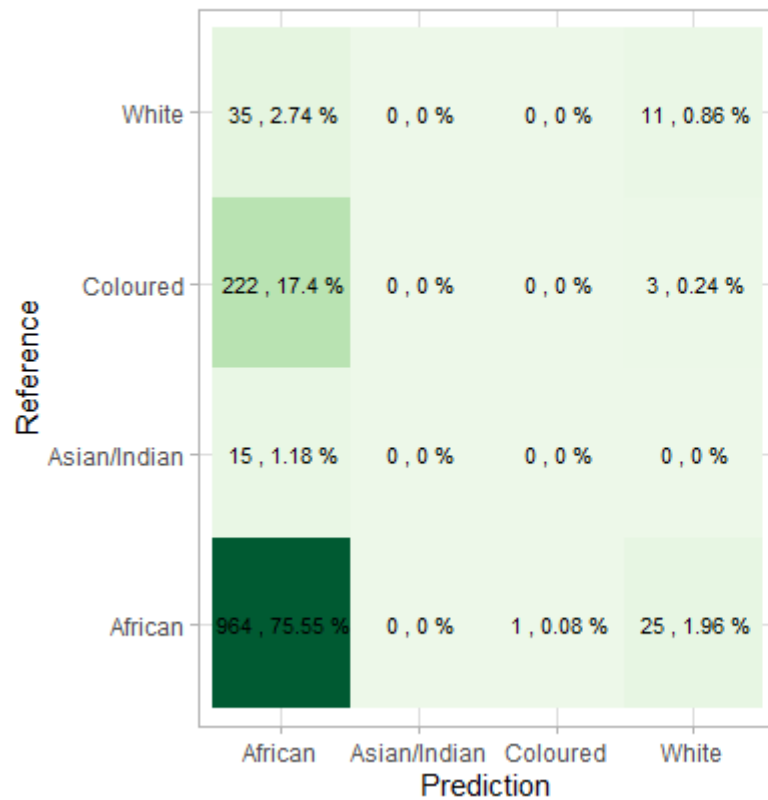


Figure 3.3: ML on balanced data

Confusion Matrix



| | cm.overall |
|----------------|------------|
| Accuracy | 0.76 |
| Kappa | 0.05 |
| AccuracyLower | 0.74 |
| AccuracyUpper | 0.79 |
| AccuracyNull | 0.78 |
| AccuracyPValue | 0.85 |
| McnemarPValue | NaN |

Statistics

| | Sen | Spec | Pos | Neg | Prec |
|---------------------|------|------|------|------|------|
| Class: African | 0.97 | 0.05 | 0.78 | 0.35 | 0.78 |
| Class: Asian/Indian | 0 | 1 | NaN | 0.99 | NA |
| Class: Coloured | 0 | 1 | 0 | 0.82 | 0 |
| Class: White | 0.24 | 0.98 | 0.28 | 0.97 | 0.28 |

| | Rec | F1 | Prev | DetRat | DetPrev | BalAcc |
|---------------------|------|------|------|--------|---------|--------|
| Class: African | 0.97 | 0.87 | 0.78 | 0.76 | 0.97 | 0.51 |
| Class: Asian/Indian | 0 | NA | 0.01 | 0 | 0 | 0.5 |
| Class: Coloured | 0 | NaN | 0.18 | 0 | 0 | 0.5 |
| Class: White | 0.24 | 0.26 | 0.04 | 0.01 | 0.03 | 0.61 |

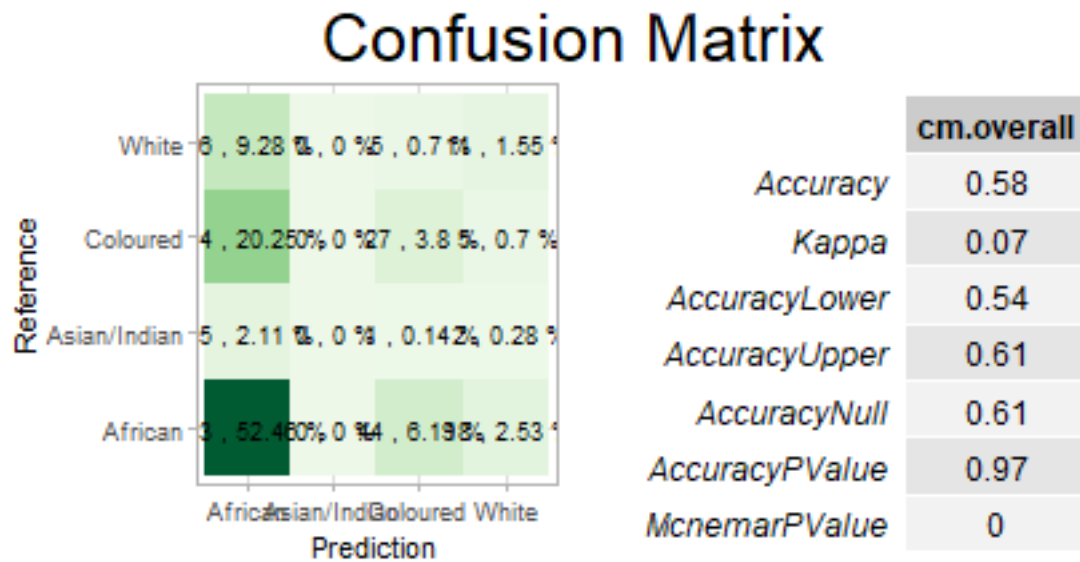


Figure 3.4: Confusion Matrices

4. Sequel

5. Conclusion

[Katzke \(2017\)](#)

References

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Appendix

Appendix A

Some appendix information here

Appendix B