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ARE THEORIES OF RATIONALITY EMPIRICALLY TESTABLE?

ABSTRACT. Since rationality is a normative ideal, it is difficult to see how a theory of rationality might be subjected to empirical evaluation. This paper explores various aspects of this problem in relation to the work of L. J. Cohen, Amos Tversky and Daviel Kahneman, Ellery Eells, Isaac Levi, and Henry Kyburg. Special consideration is given to its significance for testing systems of inductive logic.

If rationality is only a normative ideal, then it is difficult to imagine how theories of rationality can be empirically tested so as to be confirmed or disconfirmed. How we should think and act is constrained only in the loosest sense by the ways in which we do act and think. On the other hand it is entirely possible to describe the patterns of thought and action manifested by human populations which these populations characterize as rational, and even to give an explanatory account of why these patterns of thought and action are manifested. Hence it is possible to test the empirical adequacy of theories of this second sort.

Two kinds of theories of rationality are distinguishable. The first kind provides an answer to the question:

(1)   How should we act or think?

while the second kind provides an answer to the question:

(2)   How do we act or think?

Received doctrine states that while theories of the first kind are not accepted or rejected on the basis of experimentally determined data, theories of the second kind can be so accepted or rejected.

Is there any way in which normative theories of rationality are subject to empirical testing? I claim not only that this is possible but desirable. I claim that this is the case when normative theories are conceived of as answers to the question:

(3)   How should we think about how we think?

and that the resulting theory of rationality can be confirmed or discon-
firmed by experimental data. Before considering the desirability of such
an approach, however, I shall discuss its possibility.

A pioneering attempt to formulate such a methodology is to be found
in a recent article by the philosopher L. J. Cohen.[1] This article gener-
ates many questions. Cohen advances the thesis that human irrationality
can be systematically investigated. If human behavior does not conform
to the normative set of standards which define rationality, then irration-
ality is experimentally demonstrated. These norms are arrived at by a
process which Cohen calls the establishment of a "narrow reflective
equilibrium". On this approach, which has been developed by Good-
man and Rawls,[2] one matches general norms against particular in-
tuitions to arrive at a set of normative principles in harmony with
intuitions. Corresponding to these normative theories, and in Cohen's
words "read off" from them, are theories of inductive competence.
Cohen makes use of the Chomskyian distinction between a person's
ideal competence (incorporated in a theory of ideal capacity) and a
person's actual performance. He assigns to human performance the
character of irrationality on the basis of empirical evidence, but ideal
capacity (competence) remains always rational. He does not envision
any empirical procedures which put to the test a theory of rational
competence. It is an a priori theory.

In fact, there are a number of normative theories of inference that
compete for acceptance as the most satisfactory. These theories can be
categorized along at least three independent dimensions: (1) they are
Bayesian or non-Bayesian theories;[3] (2) they incorporate a folk-psycho-
logical or a computational conception of acceptance and belief,[4] and (3)
they do or do not incorporate a notion of chance.[5] It is difficult to
imagine or specify how competing theories that claim a priori status can
vie for acceptance as the best theory. For the presentation of competing
a priori intuitions to form the basis of such a choice appears to involve
a commitment to false a priori intuitions, a notion which on its face is
absurd. Yet some such commitments seem to be at the basis of the
argument between adherents of these different theories. So Levi faults
Kyburg's system for violating a principle of confirmational conditionaliz-
ation that Levi claims is intuitively obvious. As a consequence, consensus
fails to emerge, though, in the dialectic that occurs, modifications of
systems do occur. It is sometimes claimed that theories are not really in
conflict because they are topic-specific. Cohen, in fact, has claimed that

his theory of non-Bayesian probabilities is applicable to legal rather than to scientific subject-matters. But it is difficult to think of a non-circular definition of subject matter that will facilitate this obvious strategy for avoiding conflict. Perhaps systematic psychological data is relevant to theory choice, after all.

Two immediate objections can be raised. A theory of inductive logic, goes the first objection, is a normative theory, and consequently no amount of data, systematically or casually arrived at, can falsify it.

There is a second objection. The charge of circularity can still be raised against the procedure of confirming a theory of induction. For if data is to be relevant (or irrelevant) to a theory, then that relationship can best be described as an inductive one, the subject matter of an inductive logic. So in order to test an inductive logic, a correct inductive logic must be presupposed. This difficulty is also encountered in the various attempts to justify induction. How should we deal with these objections?

Logical norms, including those we classify as inductive, are traditionally entertained as analytic statements, i.e., as true or false because of the meaning of their constituent terms. Carnap later characterized these inductive norms as based upon our intuitions. It is not difficult to consider the evidence garnered by psychologists as systematically expressing the intuitions of human populations. Psychologists can determine the inferences or estimations a population thinks should be made under determinate circumstances. Norms – generally those of a singular character, such as that 'the probability of *this* event should $= .N$' – are the subject matter of psychological inquiry. Yet these norms are themselves of the same logical character as the general principles that they test and are themselves in a dialectical relationship with those principles. This in fact is the process of finding a reflective equilibrium. There no longer exists a logical gap between statements that specify what ought to be the case and statements as to what is or is not the case.

What about the circularity that seems to accompany all our attempts to investigate the foundations of inductive logic? Many inductive logicians accept this circularity without considering it to be crippling. As Ellery Eells, for example, has remarked,

To the extent that a theory implies and explains what is already known or believed about its subject matter, the theory is confirmed. And this should hold true for theories about confirmation. Thus the Bayesian theory of confirmation will be confirmed if it can be shown that it is able to explain and justify accepted forms of inductive inference.[6]

From this point of view, a theory of confirmation can itself be con-
firmed. Eells endorses the thesis that a theory is confirmed to the extent
that it explains some underlying data not previously explained. The
theories of confirmation we consider as candidates for confirmation
themselves are presupposed as true; otherwise no confirmation could
be established for them. But in this context, this is not a relevant
objection. Consider the procedure as a bootstrapping process. If we
assume the correctness of some leading principles of confirmation, we
may subsequently have to modify our leading principles, but the situ-
ation is analogous to the situation of a naturalized epistemology. These
standards of knowledge are utilized by our sciences of nature. But the
knowledge they provide can only be justified in terms of our standards
of knowledge. The circuitous quality of the circle in this case is respon-
sible for the lack of a feeling of paradox. In the case of inductive
principles, these is also virtue in the circle. Only some rather general
principles are assumed *ab initio* in order to confirm the logic of induc-
tion. We do not know whether these principles are exactly those that are
to be confirmed or disconfirmed. In the strict case of vicious circularity,
exactly the proposition that is to be correctly inferred must be assumed
as a premise. As Black has shown in his defense of an inductive justifi-
cation of an inductive rule, even when the rule to be inferred is itself
employed as a rule of inference, the circularity is not of this strict kind.
Much less so is the circularity of confirmation in the case I am discussing
in this paper. Thus can we investigate empirically the adequacy of
logical theories of induction.

We do not know whether the use of psychological data will advance
the choice of a theory. But we know that the systematic collection of
empirical data has frequently been of value to indicate some possible
modes of inquiry. Yet two caveats ought to be acknowledged.

First, it should be stated that what we are attempting to confirm or
disconfirm are normative theories of inductive inference. Some writers
on this subject have claimed that inductive logic represent innate human
competencies and that, under determinate conditions, performances
can be lacking in competencies. Such a view is surely one to be estab-
lished or rejected empirically, but it is not the question at issue here.
Of course, if this theory is eventually accepted, then our views about
the normative interpretation of logic will be affected. But we need not
speculate on these matters now.

Second, the evidence elicited by psychological investigation consists

of individuals providing an inquirer with reports of their particular intuitions regarding inductively established beliefs or inferences. In a very well-known investigation conducted by Amos Tversky and Daniel Kahneman, persons were given the following information:[7]

A cab was involved in a hit and run accident at night. Two cab companies, the green and the blue, operate in the city. You are given the following data:

(A)   85% of the cabs in the city are green, and 15% are blue.
(B)   A witness identified the cab as blue. The court tested the reliability of the witness under the same circumstances that existed on the night of the accident and concluded that the witness correctly identified each one of the colors 80% of the time, and failed 20% of the time.

Then the subjects of the experiment are asked: "What is the probability that the cab involved in the accident was blue rather than green?"

A Bayesian analysis would sanction the particular inference,

$$(1) \ P(B/W) = 0.41.$$

Persons' intuition differed, however. The median and mode intuition was,

$$(2) \ P(B/W) = 0.8.$$

What psychologists are investigating, of course, are persons' particular intuitions. These may be compared with the judgments mandated by a system of logic, or even with the general intuitions that form the basis for that system.

The kind of experiment that I have described is only one of a series, dating back over thirty years, in which psychologists have "tested" persons' rationality by subjecting them to experiments. Ward Edwards, Amos Tversky, and Daniel Kahneman are perhaps the best-known of this group. Edwards confirmed that people were conservative Bayesian; Tversky and Kahneman revised this finding to show that people are not Bayesians at all. To Cohen this data is seen as relevant to the judgment of rationality. But there is another way to view these investigations, and that is to see these systematic studies of intuition as confirming or disconfirming theories of induction. Thus we may examine the experiment performed by Tversky and Kahneman. It seems to

refute naive Bayesianism. But does it support any alternative theory? As Tversky and Kahneman show, when (A) is replaced by the following: (A′) Although the two companies are roughly equal in size, 85% of the cab accidents in the city involve green cabs and 15% involve blue cabs, they report "The answers to this problem were highly variable, but the base rate was no longer ignored. The median answer was 0.60 which lies between the reliability of the witness (0.80) and the correct answer (0.41)".

Since (A′) involves a notion of chance, it seems that here is some evidence for a system of inductive logic that incorporates a notion of chance (like Levi's system) rather than one that makes no use of such a notion (like Kyburg's system). This is not positive proof that a theory incorporating a conception of chance must be chosen. But it suggests the relevance of psychological data to the choice of theory. Data not only can but should be used to test the comparative empirical adequacy of competing logical theories. The experiments that have been performed, therefore, offer the beginnings of a research program that to my knowledge has not yet been carried out. This research program may be successful or it may fail, for it may be impossible to differentiate between logical theories in terms of their empirical adequacy.

I have made the claim that there are competing theories of inductive logic, and I wish to say more about this claim at this time. It seems to me that there are at least two ways in which such theories can be compared:

(A)   In some cases theories license conflicting particular judgments. A case of this sort will subsequently be discussed.
(B)   In most cases, fundamentally different conceptions of the inductive process are made, at least by different classes of theories. Thus, among the fundamental ways in which inductive theories differ are the following:
        (1) As to whether associated with each person is a corpus of beliefs into which are accepted other beliefs in accordance with rules of acceptance that are part of the logic;
        (2) As to the correct measure of inductive support;
        (3) As to the assumption of chance.

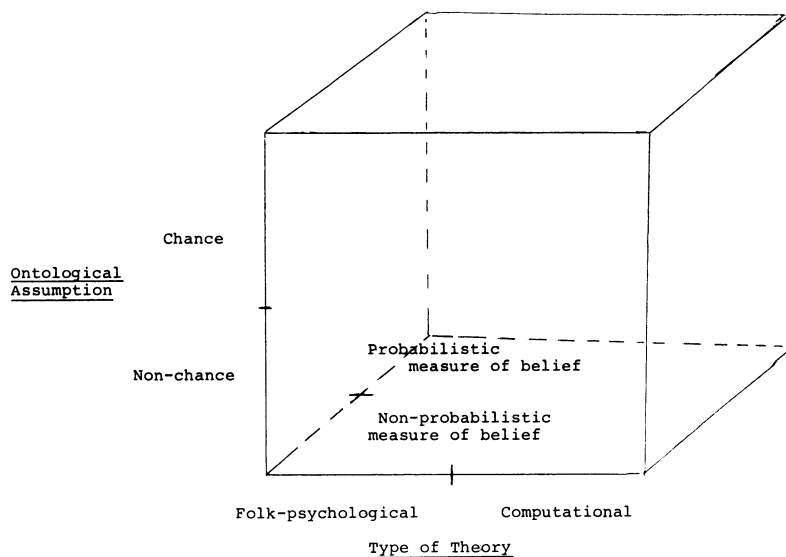There may be other factors as well. A three-fold table of theories

Fig. 1.

classified as to these three dimensions looks something like that shown in Figure 1.

If we call these notions the elements of a conceptual scheme, then inductive theories have different conceptual schemes.

(I)   The present situation in the field of inductive investigations is that a number of alternative theories have been proposed and compete for centrality. They are not notational variations of one another. And, at least for certain classes of problems, they warrant differing inferences. Disputes sometimes have been settled when:

(1) A contradiction is discovered in a system and the system is revised or is repaired (e.g., a contradiction in Kyburg's system pointed out by Schick led to some ad hoc repairs by Kyburg).

(2) Fundamental differing intuitions are compared. Levi thinks that a principle of confirmational conditionalization, as he calls it, is fundamental to any system of inductive logic. Kyburg disagrees. But no resolution is in sight.

An alternative methodology is called for. In effect I call for the replace-
ment of expert intuitions by both expert and inexpert ones. We should
assume that, if rationality is a universal human ability, then everyone
(excluding infants, the mentally deficient, and the senile) should serve
as the population to sample.

If we consider the kinds of ways that inductive theories differ from
one another, we have some ways in which to test their empirical ad-
equacy:

(A)   We may attempt to find conflicting predictions made by
        different theories and determine whether or not, in any
        systematic way, persons agree with the one prediction or its
        conflicting alternative.

(B)   In the absence of direct conflict in predictions based upon
        diverse theories, the systematic study of person intuitions
        about conceptual frameworks may support one theory better
        than another.

As an example that illustrates my approach, let me suggest the follow-
ing test between Levi and Kyburg's systems: Levi claims that probability
estimates are interval estimates. One can estimate the probability of
an event as being in the interval $[0.4, 0.6]$. The limit case is 0.1. (Kyburg
also accepts an interval conception of probability.) Both of them also
consider a principle of direct inference essential to an inductive logic,
i.e., a rule that assigns a degree of belief (an epistemic probability) to
a proposition that predicates of an individual a certain property, when
some systematic knowledge about all like individuals is known. But
while Levi requires a statement of chance as part of an argument
correctly employing a rule of direct inference Kyburg does not. Levi
asserts that in the following case:

(1)   90% of Swedes are Protestants.
(2)   Either 85% of Swedish residents of Malmo or 91% or 95%
        are Protestants.
(3)   Peterson is a Swedish resident of Malmo.

By direct inference.

Levi: Degree of belief (Peterson is a Protestant) $= 0.1$; but for
        Kyburg this is the case.
Kyburg: Degree of belief (Peterson is a Protestant) $= 0.90$.[8]

No statement regarding chance has been made. Yet conflicting inferences are warranted by these two theories. No one claims that results in favor of either theory definitively settle the matter of choice. But surely it would be relevant evidence to discover that people made point estimation judgments, of say, 0.9 in this case. More conflicts of this kind need to be investigated. In addition, intuitions about conflicting concept͗al schemes should be studied. Indeed, there has already been some unsystematic study of this in the Kahneman and Tversky experiment I have described. Other experiments by Kahneman and Tversky, moreover, show that the conjunction rule for independent probabilities is not adhered to. This may shed light upon the question of a proper metric for inductive support. I believe that this path offers much hope for understanding and testing systems of inductive logic.

NOTES

[1] L. J. Cohen (1981).
[2] Rawls (1972) and Goodman (1985).
[3] Jeffrey (1983) vs. Shaefer (1976).
[4] Levi (1984) vs. Jeffrey (1983).
[5] For example, Levi (1980) vs. Kyburg (1961)..
[6] Eells (1982).
[7] Kahneman and Tversky (1982).
[8] Levi (1984).

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