CSE 252A Computer Vision I Fall 2018 - Assignment

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Due On: Tuesday, October 23, 2018 11:59 pm ¶

Instructions

• Review the academic integrity and collaboration policies on the course website.

- This assignment must be completed individually.
- This assignment contains theoretical and programming exercises. If you plan to submit hand written
 answers for theoretical exercises, please be sure your writing is readable and merge those in order with
 the final pdf you create out of this notebook. You could fill the answers within the notebook iteself by
 creating a markdown cell.
- Programming aspects of this assignment must be completed using Python in this notebook.
- If you want to modify the skeleton code, you can do so. This has been provided just to provide you with a framework for the solution.
- You may use python packages for basic linear algebra (you can use numpy or scipy for basic operations), but you may not use packages that directly solve the problem.
- If you are unsure about using a specific package or function, then ask the instructor and teaching assistants for clarification.
- You must submit this notebook exported as a pdf. You must also submit this notebook as .ipynb file.
- You must submit both files (.pdf and .ipynb) on Gradescope. You must mark each problem on Gradescope in the pdf.
- Late policy 10% per day late penalty after due date up to 3 days.

HW1 10/23/2018

Problem 1: Perspective Projection [5 pts]

Consider a perspective projection where a point

$$P = [x y z]^T$$

is projected onto an image plane Π' represented by k = f' > 0 as shown in the following figure.

The first second and third coordinate axes are denoted by i, j, k respectively.

Consider the projection of two rays in the world coordinate system

$$Q1 = [7 -3 1] + t[8 2 4]$$

$$Q2 = [2 - 5 9] + t[8 2 4]$$

where $-\infty \le t \le -1$.

Calculate the coordinates of the endpoints of the projection of the rays onto the image plane. Identify the vanishing point based on the coordinates.

Problem 2: Thin Lens Equation [5 pts]

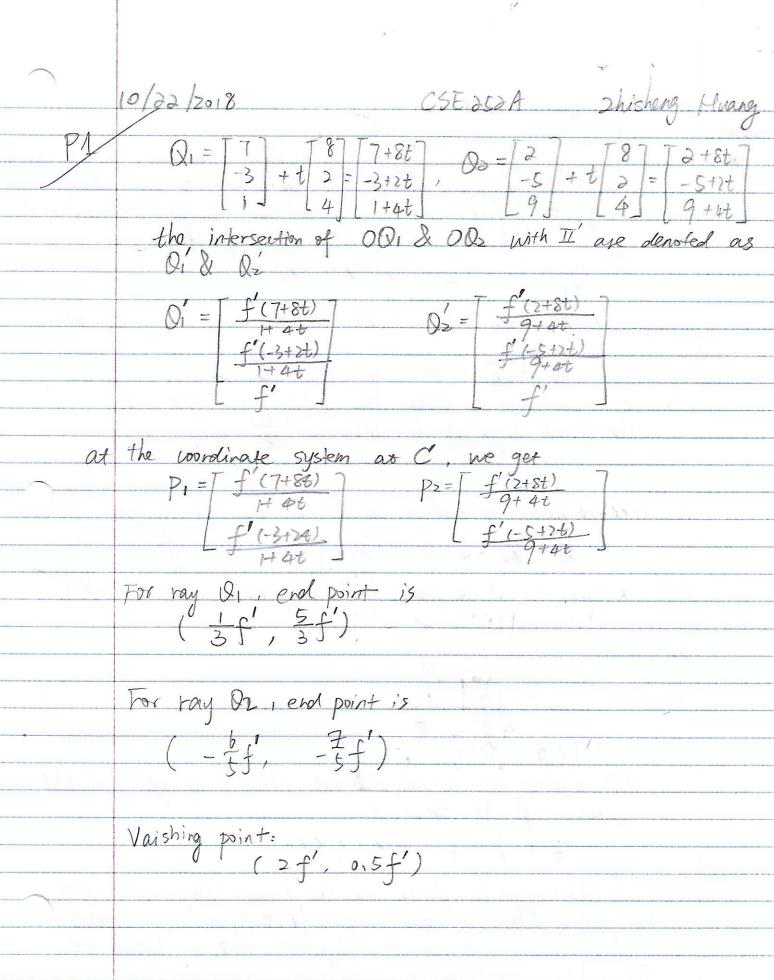
An illuminated arrow forms a real inverted image of itself at a distance of w = 60 cm, measured along the optical axis of a convex thin lens as shown above. The image is half the size of the object

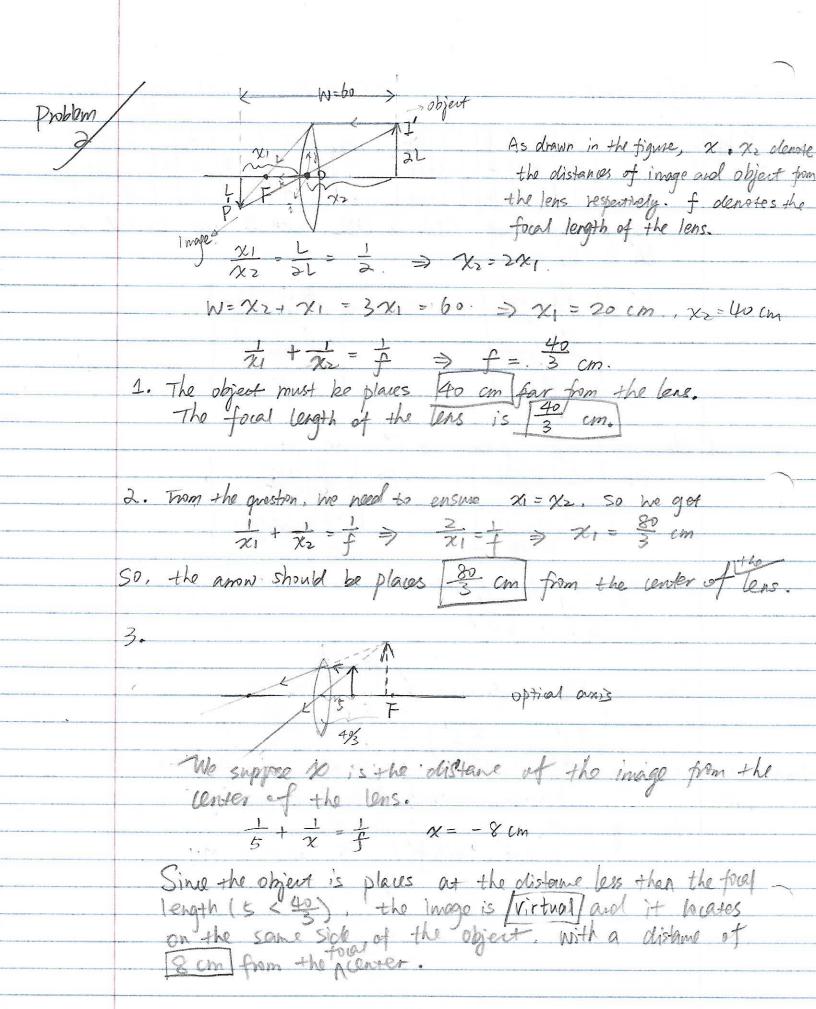


- I How far from the object must the lens be placed? Whats is the focal length of the lens?
 - 2. At what distance from the center of the lens should the arrow be placed so that the height of the image is the same?
 - 3. What would be the type and location of image formed if the arrow is placed at a distance of 5 cm along the optical axis from the optical center?

Problem 3: Affine Projection [3 pts]

Show that the image of a pair of parallel lines in 3D space is a pair of parallel lines in an affine camera.





problem 3 We suppose Li & Lz are parallel lines in a 3-D Space, which are denoted as: Li: p+tû, Lz: q+tv, teR [12] = A(q+ tv)+ b $= \overrightarrow{Aq} + \overrightarrow{b} + t\overrightarrow{Av} = \overrightarrow{q_1} + t\overrightarrow{Av}$ $= \overrightarrow{q_1} + t A S \overrightarrow{u} = \overrightarrow{q_1} + t (S A \overrightarrow{u})$ $= \overrightarrow{q_1} + t (S \overrightarrow{u})$ Thus, m, & mz are parallel in an affine plane

Problem 4: Image Formation and Rigid Body Transformations [10 points]

In this problem we will practice rigid body transformations and image formations through the projective and affine camera model. The goal will be to photograph the following four points

$$^{A}P_{1} = [-1 -0.5 \ 2]^{T}$$

 $^{A}P_{2} = [1 - 0.5 \ 2]^{T}$

 $^{A}P_{3} = [1 \ 0.5 \ 2]^{T}$

 $^{A}P_{4} = [-1 \ 0.5 \ 2]^{T}$

To do this we will need two matrices. Recall, first, the following formula for rigid body transformation $^BP=\ ^B_AR\ ^AP+\ ^BO_A$

Where BP is the point coordinate in the target (B) coordinate system. AP is the point coordinate in the source (A) coordinate system. BA is the rotation matrix from A to B, and BO_A is the origin of the coordinate system A expressed in B coordinates.

The rotation and translation can be combined into a single 4 \times 4 extrinsic parameter matrix, P_e , so that $^BP=P_e\cdot ^AP$.

Once transformed, the points can be photographed using the intrinsic camera matrix, P_i which is a 3 \times 4 matrix.

Once these are found, the image of a point, AP , can be calculated as $P_i \cdot P_e \cdot {}^AP$.

We will consider four different settings of focal length, viewing angles and camera positions below. For each of these calculate:

- a) Extrinsic transformation matrix,
- b) Intrinsic camera matrix under the perspective camera assumption.
- c) Intrinsic camera matrix under the affine camera assumption. In particular, around what point do you do the taylor series expansion?
- d) Calculate the image of the four vertices and plot using the supplied functions

Your output should look something like the following image (Your output values might not match, this is just an example)

- 1. [No rigid body transformation]. Focal length = 1. The optical axis of the camera is aligned with the z
 - axis.

 2. [Translation]. ${}^BO_A = [0 \ 0 \ 1]^T$. Focal length = 1. The optical axis of the camera is aligned with the z-
 - 2. [Translation]. $O_A = [0 \ 0 \ 1]$. Focal length = 1. The optical axis of the carriera is aligned with the 2-axis.
 - 3. [Translation and Rotation]. Focal length = 1. $_A^BR$ encodes a 30 degrees around the z-axis and then 60 degrees around the y-axis. $_A^BO_A = [0\ 0\ 1]^T$.
 - 4. [Translation and Rotation, long distance]. Focal length = 5. $_A^B R$ encodes a 30 degrees around the z-axis and then 60 degrees around the y-axis. $_A^B O_A = [0\ 0\ 13]^T$.

You can refer the Richard Szeliski starting page 36 for image formation and the extrinsic matrix.

Intrinsic matrix calculation for perspective and affine camera models was covered in class and can be referred in slide 3 http://cseweb.ucsd.edu/classes/fa18/cse252A-a/lec3.pdf http://cseweb.ucsd.edu/classes/fa18/cse252A-a/lec3.pdf)

We will not use a full intrinsic camera matrix (e.g. that maps centimeters to pixels, and defines the coordinates of the center of the image), but only parameterize this with f, the focal length. In other words: the only parameter in the intrinsic camera matrix under the perspective assumption is f, and the only ones under the affine assumption are: f, x_0 , y_0 , z_0 , where x_0 , y_0 , z_0 is the center of the taylor series expansion.

Note that the axis are the same for each row, to facilitate comparison between the two camera models. Also include:

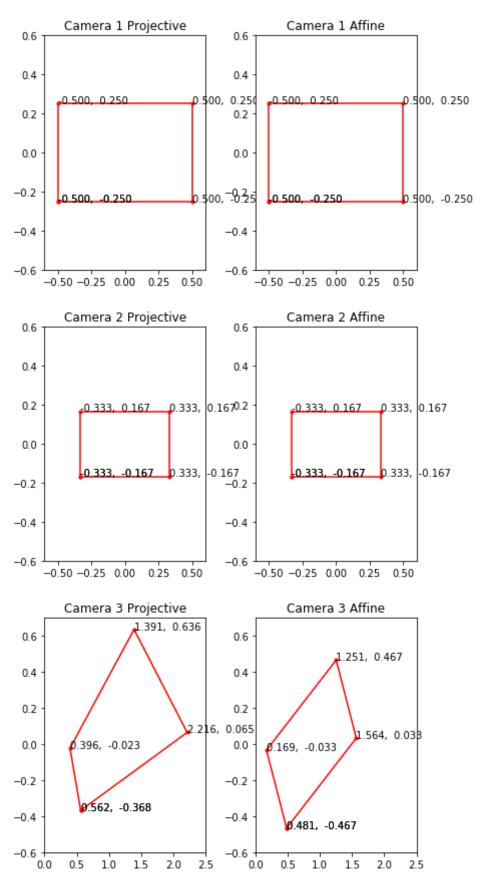
- 1. The actual points around which you did the taylor series expansion for the affine camera models.
- 2. How did you arrive at these points?
- 3. How do the projective and affine camera models differ? Why is this difference smaller for the last image compared to the second last?

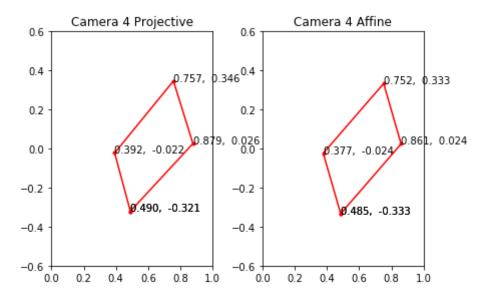
```
In [42]: | import numpy as np
         import matplotlib.pyplot as plt
         import math
         # convert points from euclidian to homogeneous
         def to homog(points):
             if len(points) == 0 or points is None:
                 return None
             if len(points.shape) == 1:
                 oneLine = np.array([1]).T # add '1'
                 return np.append(points, oneLine)
             else:
                 oneLine = np.ones(points.shape[1])
                 return np.vstack((points, oneLine)) # add a line of '1's if usin
         g matrices
         # convert points from homogeneous to euclidian
         def from homog(points homog):
             if len(points_homog) == 0 or points_homog is None:
                 return None
             return points homog[:-1]/points homog[-1] # [x/z, y/z]
         # project 3D euclidian points to 2D euclidian
         def project points(P int, P ext, pts):
             # write your code here
             return from homog(np.matmul(P int, np.matmul(P ext, to homog(pts))))
          # results : Pi * Pe * points
         # Change the three matrices for the four cases as described in the probl
         # in the four camera functions geiven below. Make sure that we can see t
         he formula
         # (if one exists) being used to fill in the matrices. Feel free to docum
         ent with
         # comments any thing you feel the need to explain.
         def camera1():
             # write your code here
             f = 1.0 # focal length
             P = np.array([0, 0, 2, 1]) # original points
             P int proj = np.eye(3,4)
             P int affine = np.eye(3,4)
             P = xt = np.eye(4,4)
             P ext = np.vstack((np.hstack((np.eye(3,3), np.zeros((3, 1)))), np.ar
         ray([0, 0, 0, 1]))) # modify P ext matrix by adding
                              # translation information
             P = np.matmul(P ext, P) # perform P ext matrix to remove camera art
```

```
ifacts
    x0 = P_[0]
   y0 = P[1]
    z0 = P[2]
    #print("Point: ", x0, y0, z0) # actual point for affine camera model
    # generate the Pi proj matrix
   P_int_proj[0, 0], P_int_proj[1, 1] = f, f
    # generate the Pi affine matrix
    P int affine[0, 0], P int affine[1, 1], P int affine[2, 2], P int af
fine[2, 3] = f/z0, f/z0, 0, 1
    P_{int_affine[0:2, 2:]} = np.array([[-f*x0 / (z0)**2, f*x0/z0], [-f*y0])
 / (z0)**2, f*y0/z0]])
    return P_int_proj, P_int_affine, P_ext
def camera2():
    # write your code here
    f = 1.0 # focal length
    P = np.array([0, 0, 2, 1]) # original points
    P_{int\_proj} = np.eye(3,4)
    P_{int\_affine} = np.eye(3,4)
   P = xt = np.eye(4,4)
    # generate P ext matrix
   P = ext[2, 3] = 1.0
   P_ = np.matmul(P_ext, P) # perform P_ext matrix on points
    x0 = P [0]
    y0 = P[1]
    z0 = P [2]
    #print("Point: ", x0, y0, z0) # actual point for affine camera model
    # generate the Pi proj matrix
    P_int_proj[0, 0], P_int_proj[1, 1] = f, f
    # generate the Pi affine matrix
    P int affine[0, 0], P int affine[1, 1], P int affine[2, 2], P int af
fine[2, 3] = f/z0, f/z0, 0, 1
    P int affine[0:2, 2:] = np.array([[-f*x0 / (z0)**2, f*x0/z0], [-f*y0
 / (z0)**2, f*y0/z0]])
    return P_int_proj, P_int_affine, P_ext
def camera3():
    # write your code here
   f = 1.0 # focal length
   P = np.array([0, 0, 2, 1]) # original point in world coordinate syst
em
    P int proj = np.eye(3,4)
    P int affine = np.eye(3,4)
   P = xt = np.eye(4,4)
    # rotation around z-axis
    Rz = np.array([[np.cos(np.deg2rad(30)), -np.sin(np.deg2rad(30)), 0],
 [np.sin(np.deg2rad(30)), np.cos(np.deg2rad(30)), 0], [0, 0, 1]])
```

```
# rotation around y-axi
    Ry = np.array([[np.cos(np.deg2rad(60)), 0, np.sin(np.deg2rad(60))],
[0, 1, 0], [-np.sin(np.deg2rad(60)), 0, np.cos(np.deg2rad(60))]])
    # generate rotation matrix
    R = np.matmul(Ry, Rz)
    #generate P ext matrix
    P_{ext[0:3, 0:3]} = R
    P = xt[2, 3] = 1.0
    P = np.matmul(P ext, P)
    x0 = P [0]
    y0 = P_[1]
    z0 = P[2]
    #print("Point: ", x0, y0, z0) # actual point for affine camera model
    # generate P int proj matrix
    P_{int} proj[0, 0], P_{int} proj[1, 1] = f, f
    # generate P int affine matrix
    P_int_affine[0, 0], P_int_affine[1, 1], P_int_affine[2, 2], P_int_af
fine[2, 3] = f/z0, f/z0, 0, 1
    P int affine[0:2, 2:] = np.array([[-f*x0 / (z0)**2, f*x0/z0], [-f*y0
 / (z0)**2, f*y0/z0]])
    return P int proj, P int affine, P ext
def camera4():
    # write your code here
    f = 5.0 # focal length
    P = np.array([0, 0, 2, 1]) # original point in world cooridates sys
tem
   P int proj = np.eye(3,4)
    P int affine = np.eye(3,4)
    P = xt = np.eye(4,4)
    Rz = np.array([[np.cos(np.deg2rad(30)), -np.sin(np.deg2rad(30)), 0],
 [np.sin(np.deg2rad(30)), np.cos(np.deg2rad(30)), 0], [0, 0, 1]])
    Ry = np.array([[np.cos(np.deg2rad(60)), 0, np.sin(np.deg2rad(60))],
[0, 1, 0], [-np.sin(np.deg2rad(60)), 0, np.cos(np.deg2rad(60))]])
    # generate rotation matrix
    R = np.matmul(Ry, Rz)
    P = ext[0:3, 0:3] = R
    P ext[2, 3] = 13.0 # translation information
    P = np.matmul(P ext, P)
    x0 = P [0]
    y0 = P_[1]
    z0 = P_[2]
    #print("Point: ", x0, y0, z0) # actual point for affine camera model
    # generate p_int perspective projection
    P int proj[0, 0], P int proj[1, 1] = f, f
    # generate p int in affine camera model
    P_int_affine[0, 0], P_int_affine[1, 1], P_int_affine[2, 2], P_int_af
fine[2, 3] = f/z0, f/z0, 0, 1
    P_{int_affine[0:2, 2:]} = np.array([[-f*x0 / (z0)**2, f*x0/z0], [-f*y0])
 / (z0)**2, f*y0/z0]])
```

```
return P_int_proj, P_int_affine, P_ext
# Use the following code to display your outputs
# You are free to change the axis parameters to better
# display your quadrilateral but do not remove any annotations
def plot points(points, title='', style='.-r', axis=[]):
    inds = list(range(points.shape[1]))+[0]
    plt.plot(points[0,inds], points[1,inds],style)
    for i in range(len(points[0,inds])):
        plt.annotate(str("{0:.3f}".format(points[0,inds][i]))+", "+str(
"{0:.3f}".format(points[1,inds][i])),(points[0,inds][i], points[1,inds][
i]))
    if title:
        plt.title(title)
    if axis:
        plt.axis(axis)
    plt.tight_layout()
def main():
    point1 = np.array([[-1, -.5, 2]]).T
    point2 = np.array([[1,-.5,2]]).T
    point3 = np.array([[1,.5,2]]).T
    point4 = np.array([[-1,.5,2]]).T
    points = np.hstack((point1,point2,point3,point4))
    axis = [[-.6, .6, -.6, .6], [-.6, .6, -.6, .6], [0, 2.5, -.6, .7], [0, 1, -.6,
.6]]
    for i, camera in enumerate([camera1, camera2, camera3, camera4]):
        P int proj, P int affine, P ext = camera()
        plt.subplot(1, 2, 1)
        plot points(project points(P int proj, P ext, points), title='Ca
mera %d Projective'%(i+1), axis = axis[i])
        plt.subplot(1, 2, 2)
        plot points(project points(P int affine, P ext, points), title=
'Camera %d Affine'%(i+1), axis = axis[i])
        plt.show()
main()
```





Written answers:

Actual points for affine camera model for each camera: i choose P = [0, 0, 2] in world coordinate system as the original point. But before points being photographed with intrinsic camera matrix, they need to be transformed with extrinsic matrix. So, the actual points for affine camera model are camera 1: P' = [0, 0, 2]; camera 2: P' = [0, 0, 3]; camera 3: P' = [1.732, 0, 2]; camera 4: P' = [1.732, 0, 14]

Affine projection is an approximation of perspective projection. So, in most cases, it is sililar to perspective projection. The results for camera 1 and camear 2 show that there is no difference between these two projection since there are no rotations. Affine projection preserves parallism. All the results for affine camera model show this property. For camera 3, the translation is small for the local length and rotation matrix. The points with affine projection looks very differnt from those with perspective projection. The values of focal length, rotation matrix and translation matrix affect the performation of affine projection.

Problem 5: Homography [12 pts]

You may use eig or svd routines in python for this part of the assignment.

Consider a vision application in which components of the scene are replaced by components from another image scene.

In this problem, we will implement partial functionality of a smartphone camera scanning application (Example: CamScanner) that, in case you've never used before, takes pictures of documents and transforms it by warping and aligning to give an image similar to one which would've been obtained through using a scanner.

The transformation can be visualized by imagining the use of two cameras forming an image of a scene with a document. The scene would be the document you're trying to scan placed on a table and one of the cameras would be your smart phone camera, forming the image that you'll be uploading and using in this assignment. There can also be an ideally placed camera, oriented in the world in such a way that the image it forms of the scene has the document perfectly algined. While it is unlikely you can hold your phone still enough to get such an image, we can use homography to transform the image you take into the image that the ideally placed camera would have taken.

This digital replacement is accomplished by a set of corresponding points for the document in both the source (your picture) and target (the ideal) images. The task then consists of mapping the points from the source to their respective points in the target image. In the most general case, there would be no constraints on the scene geometry, making the problem quite hard to solve. If, however, the scene can be approximated by a plane in 3D, a solution can be formulated much more easily even without the knowledge of camera calibration parameters.

To solve this section of the homework, you will begin by understanding the transformation that maps one image onto another in the planar scene case. Then you will write a program that implements this transformation and use it to warp some document into a well aligned document (See the given example to understand what we mean by well aligned).

To begin with, we consider the projection of planes in images. imagine two cameras C_1 and C_2 looking at a plane π in the world. Consider a point P on the plane π and its projection $p = [u1, v1, 1]^T$ in the image 1 and $q = [u2, v2, 1]^T$ in image 2.

There exists a unique, upto scale, 3×3 matrix H such that, for any point P:

$$q \approx Hp$$

Here \approx denotes equality in homogeneous coordinates, meaning that the left and right hand sides are proportional. Note that H only depends on the plane and the projection matrices of the two cameras.

The interesting thing about this result is that by using H we can compute the image of P that would be seen in the camera with center C_2 from the image of the point in the camera with center at C_1 , without knowing the three dimensional location. Such an H is a projective transformation of the plane, called a homography.

In this problem, complete the code for computeH and warp functions that can be used in the skeletal code that follows.

There are three warp functions to implement in this assignment, example ouputs of which are shown below. In warp1, you will create a homography from points in your image to the target image (Mapping source points to target points). In warp2, the inverse of this process will be done. In warp3, you will create a homography between a given image and your image, replacing your document with the given image.

- 1.
 - 2.
 - 3.

2. In the context of this problem, the source image refers to the image of a document you take that needs to be replaced into the target.

- 3. The target image can start out as an empty matrix that you fill out using your code.
- 4. You will have to implement the computeH function that computes a homography. It takes in the point correspondences between the source image and target image in homogeneous coordinates respectively and returns a 3 × 3 homography matrix.
- 5. You will also have to implement the three warp functions in the skeleton code given and plot the resultant image pairs. For plotting, make sure that the target image is not smaller than the source image.

Note: We have provided test code to check if your implementation for computeH is correct. All the code to plot the results needed is also provided along with the code to read in the images and other data required for this problem. Please try not to modify that code.

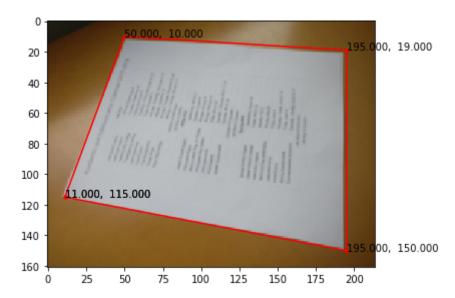
You may find following python built-ins helpful: numpy.linalg.svd, numpy.meshgrid

```
In [43]: | import numpy as np
         from scipy.misc import imread, imresize
         from scipy.io import loadmat
         import matplotlib.pyplot as plt
         # load image to be used - resize to make sure it's not too large
         # You can use the given image as well
         # A large image will make testing you code take longer; once you're sati
         sfied with your result,
         # you can, if you wish to, make the image larger (or till your computer
          memory allows you to)
         source image = imresize(imread("photo.jpg"),.1)[:,:,:3]/255.
         # display images
         plt.imshow(source image)
         # Align the polygon such that the corners align with the document in you
         r picture
         # This polygon doesn't need to overlap with the edges perftectly, an app
         roximation is fine
         # The order of points is clockwise, starting from bottom left.
         x_{coords} = [11, 50, 195, 195]
         y_{coords} = [115, 10, 19, 150]
         # Plot points from the previous problem is used to draw over your image
         # Note that your coordinates will change once you resize your image agai
         source points = np.vstack((x coords, y coords))
         plot points(source_points)
         plt.show()
```

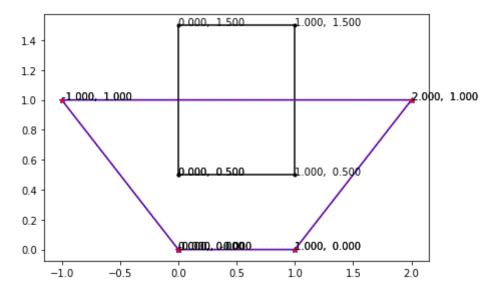
/Users/huangzhisheng/anaconda2/lib/python2.7/site-packages/ipykernel_la uncher.py:10: DeprecationWarning: `imread` is deprecated!
 `imread` is deprecated in SciPy 1.0.0, and will be removed in 1.2.0.
 Use ``imageio.imread`` instead.

Remove the CWD from sys.path while we load stuff.
/Users/huangzhisheng/anaconda2/lib/python2.7/site-packages/ipykernel_la
uncher.py:10: DeprecationWarning: `imresize` is deprecated!
`imresize` is deprecated in SciPy 1.0.0, and will be removed in 1.2.0.
Use ``skimage.transform.resize`` instead.

Remove the CWD from sys.path while we load stuff.

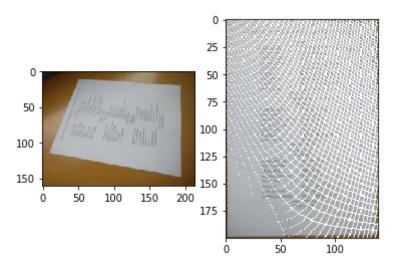


```
In [44]: def computeH(source points, target points):
            # returns the 3x3 homography matrix such that:
            # np.matmul(H, source points) ~ target points
            # where source points and target points are expected to be in homoge
         neous
            # Please refer the note on DLT algorithm given at:
            # https://cseweb.ucsd.edu/classes/wi07/cse252a/homography estimatio
         n/homography estimation.pdf
            # make sure points are 3D homogeneous
            assert source points.shape[0]==3 and target points.shape[0]==3
            x1, y1, z1 = source points[0, :], source points[1, :], source points[2
         , :] # get x1, y1,z1 from source points
            x2, y2, z2 = target points[0, :],target points[1, :],target points[2
         , :] # get x2, y2, z2 from target points
            x2 , y2 = x2 / z2 , y2 / z2 # generate x2' and y2'
            m = source_points.shape[1] # get the number of points
            A1 = np.vstack((-x1, -y1, -1*np.ones(m), np.zeros(m), np.zeros(m), np.
         zeros(m), x2_*x1, x2_*y1, x2_)).T
            #print(A1)
            A2 = np.vstack((np.zeros(m), np.zeros(m), np.zeros(m), -1*x1, -1*y1,
          -1*np.ones(m), y2_*x1,y2_*y1, y2_)).T
            #print(A2)
            A = np.vstack((A1, A2)) # generate A matrix to perform SVD on
            #print(A)
            u, s, vh = np.linalg.svd(A) # perform SVD on A matrix
            H = vh.T[:,-1] \# qet the eigenvector for sigma 9
            return H.reshape((3, 3)) # reshape the eigenvector to 3x3 matrix
         # test code. Do not modify
         def test computeH():
            source points = np.array([[0,0.5],[1,0.5],[1,1.5],[0,1.5])).T
            target points = np.array([[0,0],[1,0],[2,1],[-1,1]]).T
            H = computeH(to_homog(source_points), to_homog(target_points))
            mapped points = from homog(np.matmul(H, to homog(source points)))
            plot points(source points,style='.-k')
            plot points(target points,style='*-b')
            plot points(mapped points, style='.:r')
            plt.show()
            print('The red and blue quadrilaterals should overlap if ComputeH is
          implemented correctly.')
         test computeH()
```



The red and blue quadrilaterals should overlap if ComputeH is implement ed correctly.

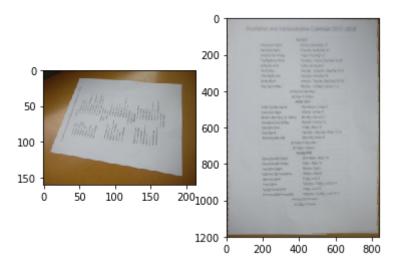
```
In [45]: def warp(source img, source points, target size):
             # Create a target image and select target points to create a homogra
         phy from source image to target image,
             # in other words map all source points to target points and then cre
         ate
             # a warped version of the image based on the homography by filling i
         n the target image.
             # Make sure the new image (of size target size) has the same number
          of color channels as source image
             assert target_size[2]==source_img.shape[2]
             m = target size[0]
             n = target size[1]
             target_points = np.array([[0,0],[n-1, 0],[n-1, m-1],[0, m - 1]]).T #
          get the target points
             H = computeH(to homog(source points), to homog(target points)) # gen
         erate the homegraphy matrix
             x = np.linspace(0, source_img.shape[1] - 1, source_img.shape[1])
             y = np.linspace(0, source img.shape[0] - 1, source img.shape[0])
             xv1, yv1 = np.meshgrid(x, y)
             xv = xv1.reshape((1,-1))
             yv = yv1.reshape((1, -1))
             sourceMatrix = np.vstack((xv, yv))
             mappedPoints = from homog(np.matmul(H,to homog(sourceMatrix))) # map
         ping from source to target
             xNew = mappedPoints[0, :].reshape(source img.shape[0], -1)
             yNew = mappedPoints[1, :].reshape(source img.shape[0], -1)
             targetImg = np.ones((m, n, 3)) # create a target image with all-whit
         e pixels
             # filling in the target image
             for i in xrange(source img.shape[0]):
                  for j in xrange(source img.shape[1]):
                      if 0 \le \text{np.ceil}(x\text{New[i, j]}) \le \text{n - 1} and 0 \le \text{np.ceil}(y\text{New[}
         i, j]) \le m - 1:
                          targetImg[np.int(np.ceil(yNew[i, j])), np.int(np.ceil(xN
         ew[i, j])), :] = source img[i, j, :]
             return targetImg
         # Use the code below to plot your result
         result = warp(source image, source points, (200,140,3))
         plt.subplot(1, 2, 1)
         plt.imshow(source image)
         plt.subplot(1, 2, 2)
         plt.imshow(result)
         plt.show()
```



The output of warp1 of your code probably has some striations or noise. The larger you make your target image, the less it will resemble the document in the source image. Why is this happening?

To fix this, implement warp2, by creating an inverse homography matrix and fill in the target image.

```
In [46]: def warp2(source img, source points, target size):
             # Create a target image and select target points to create a homogra
         phy from target image to source image,
             # in other words map each target point to a source point, and then c
         reate a warped version
             # of the image based on the homography by filling in the target imag
             # Make sure the new image (of size target size) has the same number
          of color channels as source image
             assert target_size[2] == source_img.shape[2]
             m = target size[0]
             n = target size[1]
             target_points = np.array([[0,0],[n-1, 0],[n-1, m-1],[0, m - 1]]).T #
          get the target points
             targetImg = np.ones((m, n, 3))
             sourceImg = source_image
             x = np.linspace(0, n - 1, n)
             y = np.linspace(0, m - 1, m)
             xv1, yv1 = np.meshgrid(x, y)
             H = computeH(to homog(target points), to homog(source points)) # gen
         erate the homegrapy matrix for target to source
             xv = xv1.reshape((1,-1))
             yv = yv1.reshape((1, -1))
             targetMatrix = np.vstack((xv, yv))
             mappedPoints = from homog(np.matmul(H, to homog(targetMatrix))) # ge
         nerate the transformed coordinates
             xNew = mappedPoints[0, :].reshape(m, -1)
             yNew = mappedPoints[1, :].reshape(m, -1)
             # filling the target image
             for i in xrange(m):
                 for j in xrange(n):
                     targetImg[i,j, :] = source image[np.int(np.ceil(yNew[i, j
         ])), np.int(np.ceil(xNew[i, j])), :]
             return targetImg
         # Use the code below to plot your result
         size factor = 2
         result = warp2(source image, source points, (600*size factor,420*size fa
         ctor,3))
         plt.subplot(1, 2, 1)
         plt.imshow(source image)
         plt.subplot(1, 2, 2)
         plt.imshow(result)
         plt.show()
```



Try playing around with the size of your target image in warp1 versus in warp2, additionally you can also implement nearest pixel interpolation or bi-linear interpolations and see if that makes a difference in your output.

In warp3, you'll be replacing the document in your image with a provided image. Read in "ucsd_logo.png" as the source image, keeping your document as the target.

```
In [47]: # Load the given UCSD logo image
         source image2 = imread('ucsd logo.png')[:,:,:3]/255.
         def warp3(target_image, target_points, source_image):
             m = source image.shape[0]
             n = source image.shape[1]
             source points = np.array([[0,0],[0,n-1],[m-1, n-1],[m-1, 0])).T # qe
         t the points of source
             sourceImg = source image
             x = np.linspace(0, sourceImg.shape[1]-1, sourceImg.shape[1])
             y = np.linspace(0, sourceImg.shape[0]-1, sourceImg.shape[0])
             xv1, yv1 = np.meshgrid(y, x)
             H = computeH(to homog(source points), to homog(target points)) # gen
         erate the homegrapy matrix from source to target
             xv = xv1.reshape((1,-1))
             yv = yv1.reshape((1, -1))
             sourceMatrix = np.vstack((xv, yv))
             mappedPoints = from homog(np.matmul(H, to homog(sourceMatrix))) # ge
         t the transformed coordinated from source to target
             xNew = mappedPoints[0, :].reshape(sourceImg.shape[0], -1)
             yNew = mappedPoints[1, :].reshape(sourceImg.shape[0], -1)
             # filling the desire parts
             for i in xrange(sourceImg.shape[0]):
                 for j in xrange(sourceImg.shape[1]):
                    # if 19<= np.ceil(yNew[i, j]) <= 195 and 10 <= np.ceil(xNew
         [i, j]) <= 150:
                     target_image[np.int(np.ceil(yNew[i, j])), np.int(np.ceil(xNe
         w[i, j])), :] = sourceImg[j, i, :]
                     #source image[j, i, :]
             return target image
         # Use the code below to plot your result
         result = warp3(source image, source points, source image2)
         plt.subplot(1, 2, 1)
         plt.imshow(source image2)
         plt.subplot(1, 2, 2)
         plt.imshow(result)
         plt.show()
```

/Users/huangzhisheng/anaconda2/lib/python2.7/site-packages/ipykernel_la uncher.py:2: DeprecationWarning: `imread` is deprecated!
 `imread` is deprecated in SciPy 1.0.0, and will be removed in 1.2.0.
 Use ``imageio.imread`` instead.

