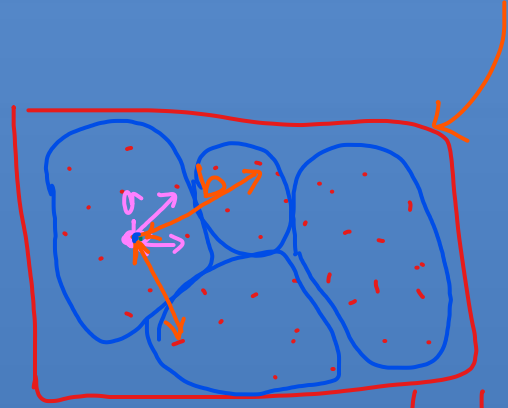




**BITS Pilani**  
**WILP**

*AMLCCLZG516*  
**ML System Optimization**  
Murali Parameswaran





Silhouette Score (-1 to +1)  
Cohesion (a)  
Separation (b)

$$S_i = \frac{b_i - a_i}{\max(a_i, b_i)}$$
$$\text{Score} = \frac{\sum S_i}{n}$$

## AIML CLZG516 ML System Optimization

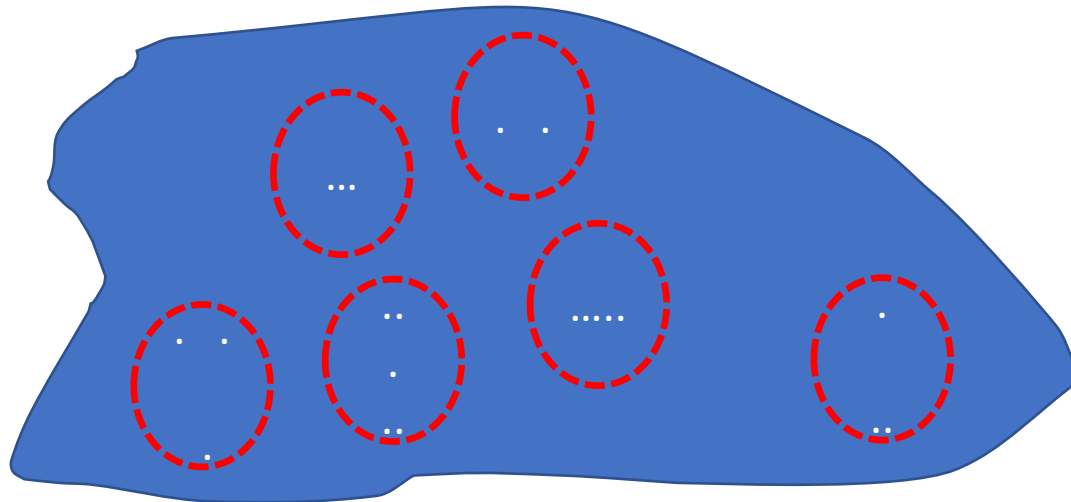
### Parallelization of ML Algorithms

- ✓ - Example: k-Means
- Issues with Large Data Size

Scale-out Clusters - Distributed Memory Programming

# Example: Data Clustering using k-Means

- Data Clustering is a classic data analytics problem:
  - Given a set of data points group them into disjoint subsets - clusters - such that:
    - Each cluster is cohesive ✓
    - Different clusters are well-separated ✓



Points are in Euclidean space


# K - means Clustering

✓ Inputs: Dataset  $D$ , A positive integer  $k$

Output: A partition  $C_s$  of  $D$  with size  $k$

(i.e.,  $k$  disjoint clusters covering all points in  $D$ )

Approach:

- ✓ 1. Chose  $k$  data points (as representatives) from  $D$ , say  $c_1, c_2, \dots, c_k$
- ✓ 2. Assign each point  $x$  in  $D$  to the cluster  $C_j$  :  
whose that has the closest center  $c_j$  
- ✓ 3. Choose  $k$  new representatives based on  
minimizing local average distance within each cluster [Notion of *cohesion*]
- ✓ 4. Iterate steps 2 and 3 until (the cluster centers converge)

# K - means Clustering using map-reduce

1. MapReduce  
2. Spark implements

- Step 1: "select representative points" for clusters  $C_j = \{ c_j \}$  for  $j=1$  to  $k$
- Step 2:
  - map "compute distance" on  $D \times Cs$  where  $Cs$  is the set of clusters
  - map "assign point to the closest cluster" on  $D$ 
    - This requires: reduce min on point-cluster distances
- Step 3: for each cluster  $C_j$  compute its centroid (i.e., mean)
  - map on  $Cs$ :
    - $c_j = (\text{reduce} + C_j) / |C_j|$
- Repeat Steps 2 and 3 until all  $c_j$  converge

$D \times Cs = \{ (x, c_j) \dots \}$   
map comp\_dist  $D \times Cs$

# K - means Clustering using map-reduce

- Step 1: "select representative points" for clusters
- Step 2:
  - map "compute distance" on  $D \times C_s$  where  $C_s$  is the set of clusters
  - map "assign point to the closest cluster" on  $D$ 
    - This requires: reduce min on point-cluster distances
- Step 3: for each cluster  $C_j$  compute its centroid (i.e., mean)
  - map on  $C_s$ :
    - $c_j = (\text{reduce} + C_j) / |C_j|$
- Repeat Steps 2 and 3 until all  $c_j$  converge

$\{ (x_i, d_{1j}) \}$   
= map comp\_dist  $D$   
 $x_i$  is a point in  $D$   
 $d_{ij}$  = distances of  $x_i$  to  
clusters

reduce min  $d_{ij}$

This reduce is required to return the cluster (with the min distance)  
and not the min distance:

*Refer to reduce-key vs. reduce-val in Spark!*

# K - means Clustering

- Exercise: Implement k-means clustering using map and reduce.
- [Hints:
  - Step 1: "select k representative points" for clusters (randomly)
  - Step 2
    - map "compute distance" on  $D \times C_s$  where  $C_s$  is the set of clusters
    - map "assign point to the closest cluster" on  $D$ 
      - This requires: reduce min on point-cluster distances
  - Step 3b: compute the centroid (i.e., mean of)  $C_j$ 
    - $c_j = (\text{reduce} + C_j) / |C_j|$

This follows a programming pattern named ***iterative map-reduce*** where map-reduce programming steps applied inside a loop.

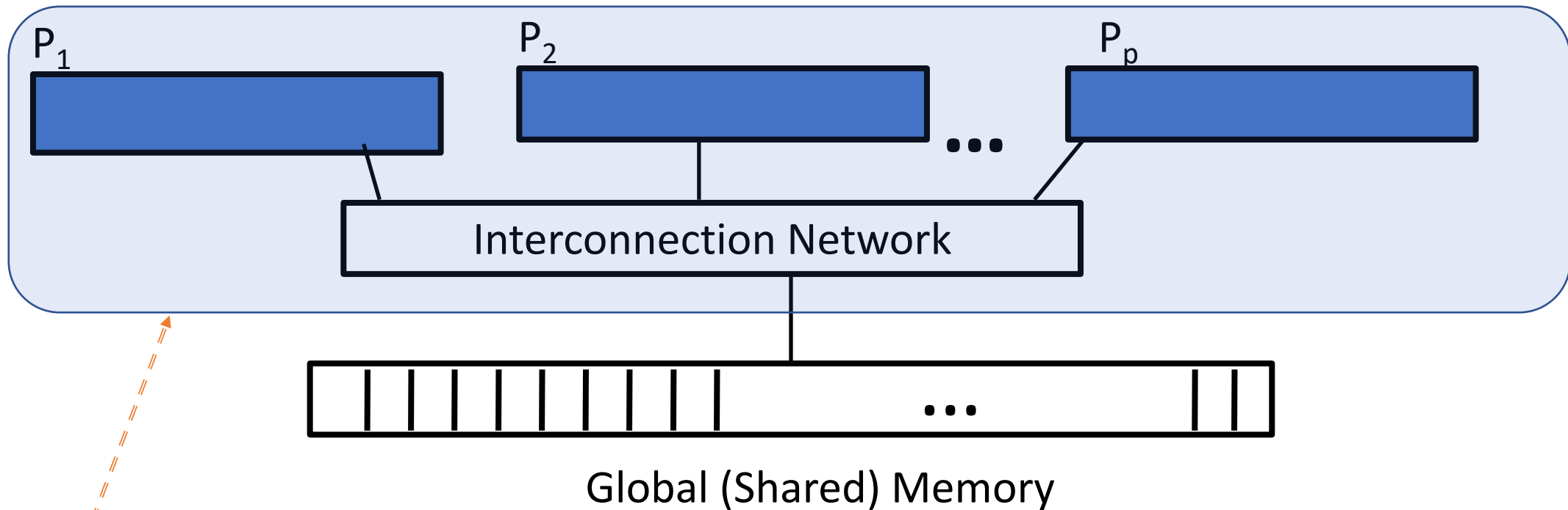
# Exercise: Speedup of k-means using map-reduce

- For each of the steps:
  - Calculate the speedup (and the number of processors)
- $T_{seq} = I * (|D| * (k+k) + (k * |C|))$  [Step 2: k distances req. k steps;  
min. computation req k-1 steps;
- I is number of iterations
- $T_{par}(p) = I * (|D|/p * (k+k) + |C|)$  - assuming step 3 is done with only k processors;  $|D|/p$  points per processor in step 2
- p processors;  $k < p$
- $Speedup(p) = T_{seq} / T_{par} = (|D| * 2 * k + k * |C|) / ((|D|/p) * (k+k) + |C|)$
- $\sim p$  (close to ideal)



# Parallel Programming: Shared Memory Model

So far we have looked at a target environment that uses a shared memory model:



e.g. a multi-core chip

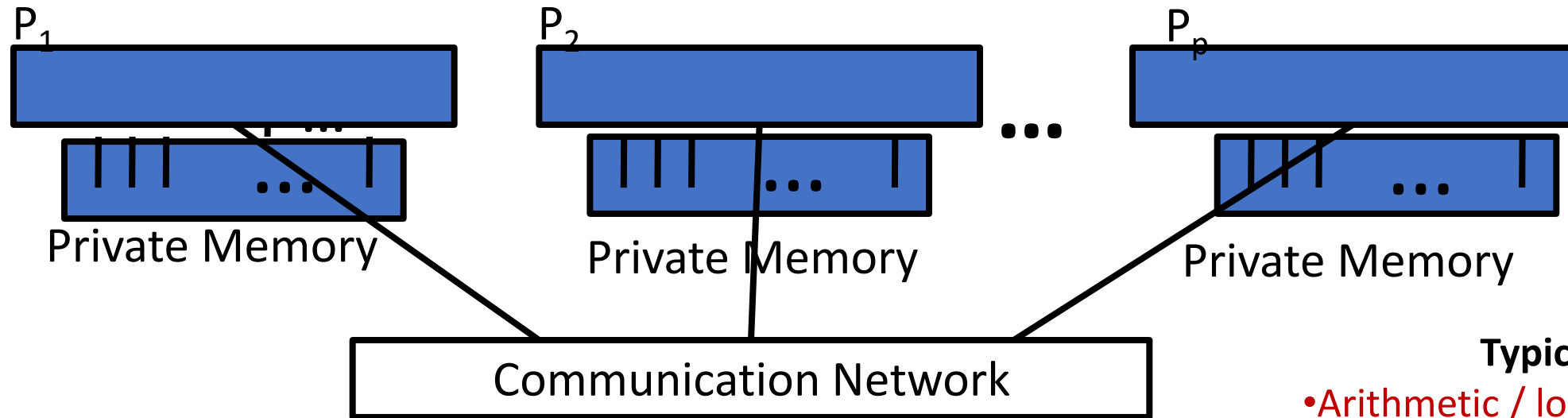
Multi-threaded Programming:  
*each thread runs on a separate core*

# Large volumes of Data

- When the volume of data that we have to process is in 100s of GB if not in TB,
  - Then all the data cannot be kept in one computer
  - And brought into memory for processing
- We a model where data can be stored on multiple computers (i.e., their hard disks)
  - All of which participate in computing.
- This leads us to a distributed computing model (aka message passing model)

# Algorithm Design - Parallel: Distributed Memory Model

Target environment:



## Typical Instructions

- Arithmetic / logic operations,
- Load / Store, and
- Jump / Branch
- **Send / receive**

## Distributed Programming:

- a program is made of multiple processes
- *each process runs on a separate computer*
- *processes exchange messages (i.e., data for collaboration)*

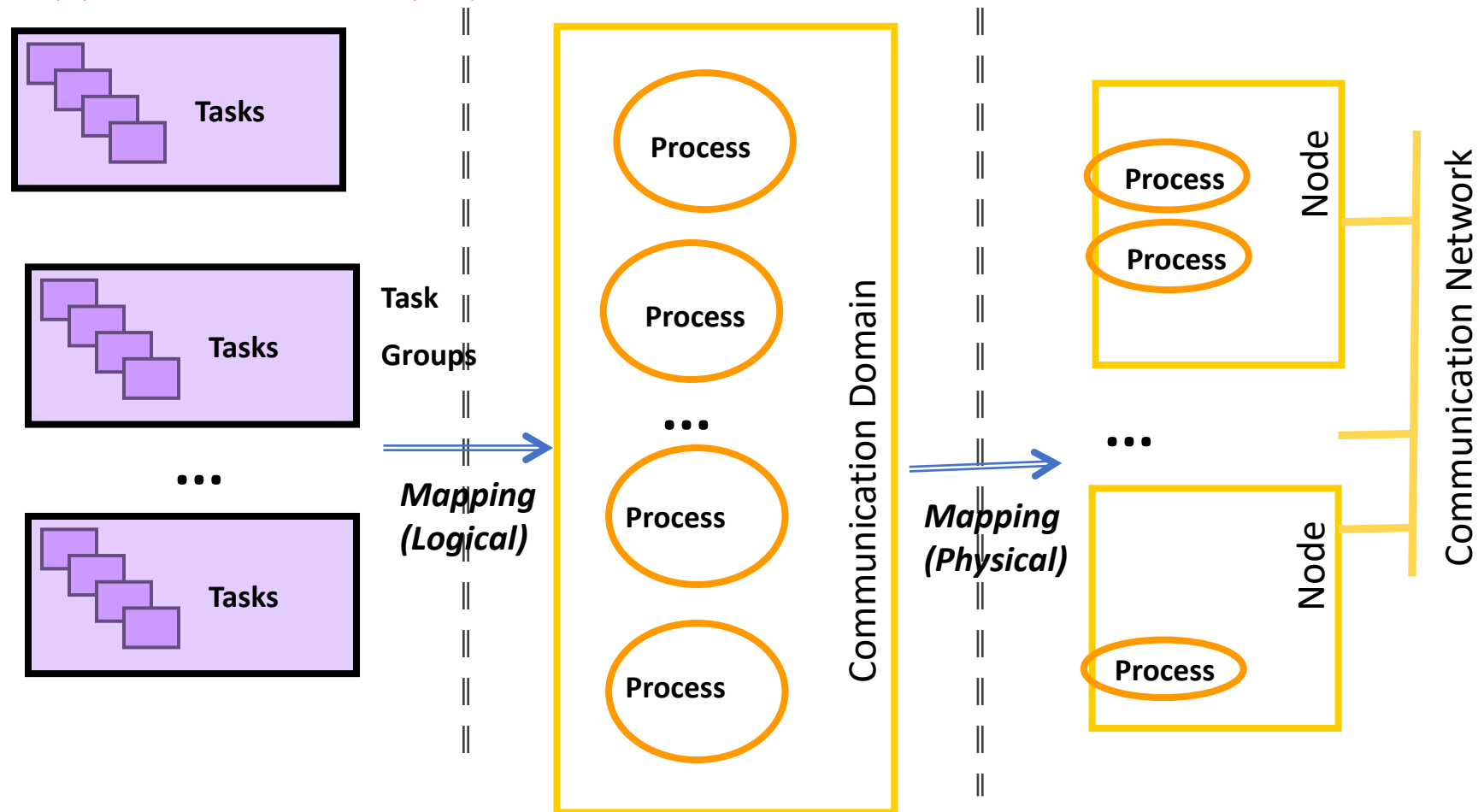
**e.g. a cluster**

# Parallel / Distributed Computing

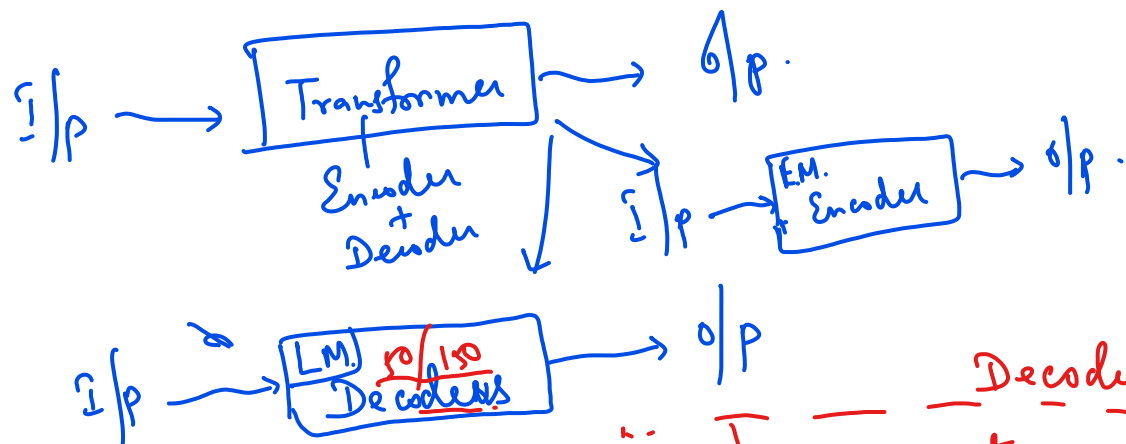
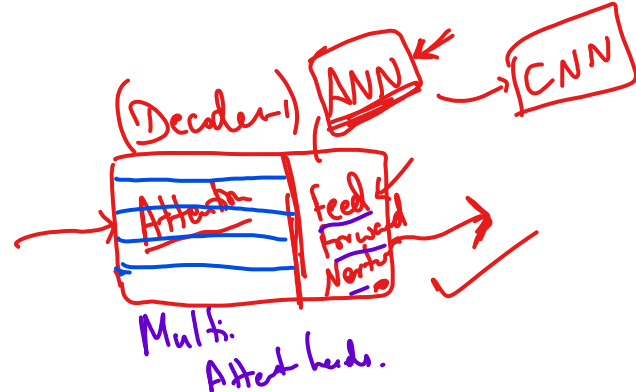
- A parallel or distributed program is made of multiple tasks that *collaborate* (to achieve a common outcome).
- Collaboration is achieved by communication:
  - exchange data using shared memory
    - i.e. Task A writes to location L; Task B reads from location L
  - exchange data by passing messages
    - i.e. Task A sends a message to Task B; Task B receives the message from Task A

- Multiple processes each with its own address space:

E.g. processes run on nodes connected in a network : (i) each node runs its own OS and (ii) each process is allocated its own (logical) address space that is mapped onto the (physical) resources of that node



# Exercise



Streaming response

- Implement k-means on Spark

- Calculate - on paper - speedup of k-means using a cluster:

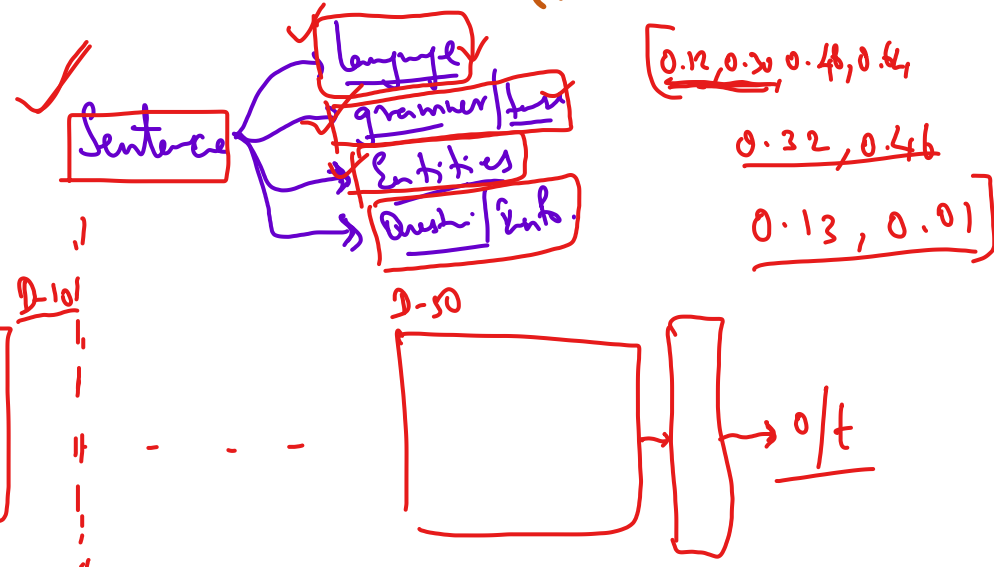
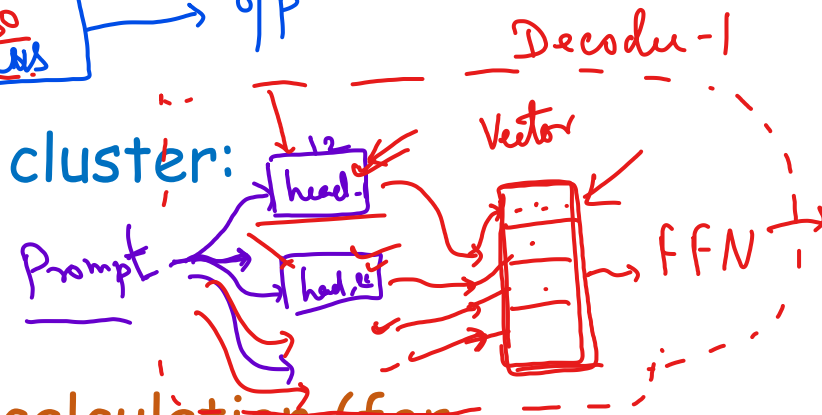
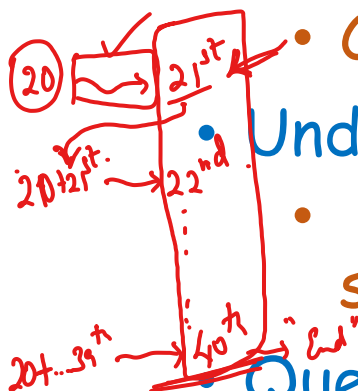
- Calculate communication cost

Understand:

- the difference between this and the previous calculation (for shared memory programming)

Questions:

- How do you distribute the data initially?
- Cost?
- Pattern?



✓ Tensor Parallelism.