

# PyPandas: A data cleaning toolkits for Spark

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## ABSTRACT

Data cleaning is a huge challenge in data mining and machine learning tasks. In this paper, we propose PyPandas, a data cleaning toolkits running on Spark, to provide further solutions to data cleaning tasks. PyPandas provides advance cleaning features such as outlier detection, data scaling and text pattern searching and replacement. We have released PyPandas on GitHub and Python package manager pip.

## 1 INTRODUCTION

In recent years, as storage devices become cheaper, storing big data in thousands of computers is easier than before. People start thinking about how to extract useful information from the huge datasets. The term, Big Data, was created to describe this phenomenon[18]. As the result, data mining[13, 22] and machine learning[26] get popular nowadays. The quality of data is one of the key factors to successful data mining[3]. Hence, data cleaning becomes a challenge in the first step of data management and analysis[5, 14, 23].

To process huge datasets efficiently, distributed systems and parallel computing frameworks[7, 9, 27] were introduced. Spark[28] is one of the most popular open source projects for industry and academia. It is built on Hadoop[27] and provides a way to manage distributed memory. PySpark[20] is an extended library for Python programmers to work with Spark.

In the Python machine learning and data mining ecosystem, Pandas[19] is the most popular data management library. Pandas dataframe provides convenient ways to collect data and several data management methods for missing value filling, data indexing and data profiling. In PySpark SQL module, PySpark provides Pandas-like DataFrame to handle data indexing, data integration, and simple data cleaning tasks such as missing value handling and duplication removal.

However, PySpark DataFrame does not support advance data processing features like outlier detection and data scaling. Although there exists several clustering and scaling algorithms in the PySpark ML module, the integration with PySpark DataFrame is not helpful and can be difficult to use for data cleaning. User has to go back and forth to process their dataset.

In this paper, we propose PyPandas, a data cleaning toolkits built on top of PySpark, that integrates PySpark ML module to support user friendly data processing features such as outlier detection and numerical data scaling. These features are important for the machine learning tasks and are supported in Scikit-Learn[21], a mainstream machine learning library, as well.

Furthermore, text data is another common data type in our storage. Text data is hard to process because of different languages, newly invented words, typos, abbreviations, urls and emoji etc.

Although we have NLTK[1], a popular text cleaning library, there is no intergration with PySpark DataFrame. In this paper, we also intergate NLTK within our toolkits and provide customized tools for users to clean text data easily.

The features of our library are summarized below.

- User friendly data cleaning toolkits built on PySpark
- Outlier detection and numerical data scaling
- Text processing such as url detection, punctuation removing, pattern searching and replacement.

## 2 RELATED WORK

There exists a number of open-source library for data cleaning and parallel data computing.

- Optimus[15] is a framework that can perform distributed data cleaning and preprocessing. This framework works well with Spark and its DataFrame can scale in big cluster. Optimus comes with helpful tools such as removing special characters and replacing null values.
- Dask[24] is another open-source library that supports parallel analytic computing. It provides scalable parallel data structures that extend interfaces like Pandas. At the same time, it offers low latency and high responsiveness.
- SparklingPandas[17] attempts to combine the power of Spark and Pandas to scale data analysis. It provides a Pandas-like API that is built using Spark's DataFrame class. Unfortunately, it only support spark v1.4 and Python 2.7, and its development has ended.

## 3 PROBLEM FORMULATION

In this paper, we focus on three major tasks, outlier detection, data scaling, and text pattern searching and replacement.

### 3.1 Outlier Detection

Outlier or anomalies detection is a challenging task in the field of data cleaning[4]. In this paper, we define outlier as the data that is far away from the its cluster centroid. Hence, given a dataset  $X$ , a clustering algorithm  $A$ [22], a distance measurement  $d$ , and the user-defined threshold  $t$ , the outlier is defined as following.

$$outlier = \{x | x \in X, d(x, x_{A_X(x)}) > t\}$$

where  $A_X(x)$  assigns  $x$  into a cluster given the dataset  $X$  and  $x_{A_X(x)}$  is the centroid of cluster to which  $x$  belongs.

Our library implements the following clustering algorithms.

- K-Means and Bisecting K-Means Algorithm  
These two algorithms partition data points into  $k$  clusters, where each point belongs to the clusters that is closest to that point. In these two models, the distance measurement  $d$

is the Euclidean Distance.

$$d(x, x_{Kmeans_X(x)}) = d(x, c) = \sqrt{\sum_{i=1}^n (x_i - c_i)^2}$$

where  $c$  is the cluster centroid.

- Gaussian Mixture Model

The algorithm assumes a probabilistic model where data points are generated from some Gaussian distributions. The Gaussian distributions are parameterized by a mean  $\vec{\mu}$  and a covariance matrix  $S$ .

The distance measurement  $d$  is defined to be Mahalanobis Distance, which measures the distance between a point and a distribution.

$$d(x, x_{GM_X(x)}) = D_M(\vec{x}) = \sqrt{(\vec{x} - \vec{\mu})^T S^{-1} (\vec{x} - \vec{\mu})}$$

### 3.2 Scaling and Normalization

Scaling and normalization are common preprocess in data cleaning. It is crucial to several machine learning models and optimization methods. Scaling increases the convergence speed and chance to find good optimum[2]. The scaling problem could be formulated as below. Given an one dimensional numerical dataset  $X$ , we provide a scaling method  $S$  such that scaled elements are bounded in same reasonable range  $[a, b]$ .

$$S_X(x) \in [a, b]$$

where  $x \in X$  and  $|a - b|$  should not be large.

To define the problem formally, we consider and implement several specific scaling methods.

- Standard scale

$$S(X) = \frac{X - \mu}{\sigma} \in \text{proper deviation range}$$

where  $\mu$  is the mean of  $X$  and  $\sigma$  is the standard deviation of  $X$

- Min-Max scale

$$S(X) = \frac{X - \min(X)}{\max(X) - \min(X)} \in [0.0, 1.0]$$

- Max-Abs scale

$$S(X) = \frac{X}{\max(X)} \in [-1.0, 1.0]$$

- P-norm Normalization

$$S(X) = \frac{X}{\|X\|_p} \in [-1.0, 1.0]$$

### 3.3 Pattern Searching and Replacement

Pattern searching and replacement is a common technique in cleaning text data. Given a string  $t$  and a regular expression[25]  $re$ , we replace the matched pattern with a user-defined string  $s$ . The replacement function  $R$  could be defined as following. Consider  $t$  as a concatenation of non-overlapping substrings  $t = t_1 \dots t_n$ .

$$R(t) = r(t_1) \dots r(t_i) \dots r(t_n)$$

$$r(t) = \begin{cases} s & \text{if } M \text{ accept } t \\ t & \text{otherwise} \end{cases}$$

such that  $M$  does not accept any substring of  $R(t)$

where  $M$  is the generalized nondeterministic finite automaton[25] corresponding to the regular expression  $re$ . We do not define replacement order and simply ignore it.

## 4 METHODS, ARCHITECTURE AND DESIGN

In this project, we build our library on top of PySpark. We handle PySpark DataFrame and implement useful data cleaning functions in our library. We integrate PySpark ML module and customize user define functions to perform advanced cleaning features such as pattern searching and replacement with regular expression. We survey the PySpark[20], Pandas[19] and Scikit-Learn[21] libraries to find out key features and create Pandas-like and Scikit-Learn-like API to provide easy usage and seamless adaptation.

### 4.1 Outlier Detection

**4.1.1 Design.** Our goal in outlier detection is to integrate the existing clustering algorithms in PySpark ML module to provide user-friendly solution for outlier detection. Users are able to select existing clustering algorithms. Furthermore, users are given the power to decide their own threshold value based on their knowledge about the dataset to filter outliers. To help users identify outliers and pick a proper threshold, we provide statistics summary of the clustering. Possible future work on outlier detection is to provide framework to register user defined clustering algorithms or implementing popular clustering algorithms such as DBScan[8] in our library.

**4.1.2 Architecture.** The implementation of the outlier detection functionality integrates the PySpark ml package. Our architecture hides the complexity of training and tuning clustering models, while it exposes easily accessible APIs for users to remove outliers. In addition, our data cleaning library implements User Defined Functions to compute distance between data points and cluster centers, as well as other summary statistics. At this time, our outlier remover can handle outliers with KMeans clustering, Bisecting KMeans, and Gaussian Mixture Model. We use Factory Design Pattern to construct different types of outlier removers with the generic APIs.

#### 4.1.3 Methods.

- KMeans[16]: Users can specify the number of clusters  $k$  to use based their knowledge about the dataset. By default, The system will choose random initial values, and perform 20 iterations of updates. Finally, a summary of the clusterings will be generated, which includes cluster centers, cluster sizes, distances, etc. User can then filter out outliers in each cluster by specifying a minimum distance from the cluster center, and all data points that are beyond that distance will be removed from the dataset.
- Bisecting KMeans: This method is very similar to KMeans clustering. The only difference is that it uses the bisecting Kmeans clustering algorithm. The algorithm does not start with  $k$  clusters. Instead, it gradually divides clusters and generates  $k$  clusters after a number of iterations.

- Gaussian Mixture: Similarly, users can specify the number of clusters (i.e. Gaussian distributions). The algorithm performs 20 iterations of updates by default. A summary that contains mean, covariance matrix and average mahalanobis distance of each cluster can be returned. User can specify a minimum distance to filter out outliers.

## 4.2 Scaling and Normalization

**4.2.1 Design.** Standardization is a common requirement for many machine learning algorithms, since some optimization methods will not work properly without scaling or normalization[2]. Our goal in scaling and normalization is similar to the goal of outlier detection. We will intergrate existing scaling algorithms in PySpark ML module into our library. User can choose existing scaling algorithms to scale their datasets. The future works is to provide framework to register user defined scaling algorithms.

**4.2.2 Architecture.** Since the design is similar with the design of outlier detection, we will follow the architecture of outlier detection. We will use the Factory Design Pattern to allow users construct their desired scaling models. We are considering to implement a single interface between any existing models in PySpark ML module to DataFrame in PySpark SQL module. Hence, we will be able to provide any feature transformation with the existing machine learning models in PySpark ML module.

### 4.2.3 Methods.

- Standard Scale: Performs basic scaling on a particular column or a list of columns in a dataframe so that the values have unit standard deviation and zero mean.
- Min-max Scale: Rescales columns to a user defined range(e.g. [0, 1]) using min max scaling.
- Max-abs Scale: Transforms columns to range between -1 and 1 by dividing through the maximum absolute value in the columns. This operation does not shift/center the data, and thus does not destroy any sparsity.
- Normalization: Given a list of columns, the normalize function can generate a normalized feature vector having unit norm. The default p-norm value for normalization is 2.0, yet users can optionally specify the p-norm value.

## 4.3 Pattern Searching and Replacement

**4.3.1 Design.** To provide a useful text cleaning toolkits, we need to have the flexibility for user to search any pattern and replace the matched ones with any user defined string. At the same time, we have to provide common patterns so that users won't need to reinvent the wheel. For example, url pattern, leading space, trailing space or numbers are common search patterns that we should provide. Moreover, we would like to integrate NLTK[1], a popular natural language toolkit, into our library. With NLTK, we would be able to perform advanced cleaning tasks or feature transformation.

**4.3.2 Architecture.** In order to achieve those design issues, we extract the common logic and column feature transformation into our core functions. We design the architecture such that user defined functions can be applied on a single or multiple columns, and a new DataFrame will be provided. The user defined function could be a regular expression substitution function, a column scaling

**Table 1: Common Regular Expression Pattern**

Common Pattern	Regular Expression
URL	URL regular expression[6]
Leading space	' ^ +'
Trailing space	' +\$'
Consecutive space	' +'
Number	' \d+ '
Not a word	' [^\w\d\s]+ '
Blank	' _+ '

**Table 2: Selected dataset**

	(Row, Col)	Size	Property
311 Service Requests	(9M, 53)	6.01 GB	Text
Permit Issuance	(3M, 60)	1.43 GB	Mixed Type
Job Application Filings	(5M, 89)	2.88 GB	Numerical Value

function or a natural language processing function in NLTK. Our architecture ensures the flexibility to various customized processing methods.

**4.3.3 Methods.** We define several common regular expression patterns in table 1 and provide simple cleaning functions to handle those patterns in text data.

## 5 EXPERIMENT

### 5.1 Dataset

Three datasets are chosen for the experiments. Each of them has different properties and can be used to test different parts of the library. The summary of datasets could be found in table 2.

- 311 Service Requests[10] This dataset contains all 311 Service Requests since 2010. The majority of data has string type, including both categorical data (e.g. City, Status) and variable length data (e.g. Address, Description). This can be useful in testing the string-related features of the library.
- DOB Permit Issuance[11] The dataset consists of a list of permits for buildings in NYC issued by Department of Building. It has diverse data types, including categorical, string, numerical, and geographical data. Hence, it provides a good test case for the versatility of the library.
- DOB Job Application Filings[12] The dataset stores job applications filed through the Borough Offices in NYC. There are many columns containing numerical data, such as fee and number of stories. It can be used to test the data scaling and outlier detection features.

### 5.2 Evaluation

We evaluate our project by comparing it against other existing open-source libraries, including Optimus[15] and Dask[24]. In addition, we examine the scalability of the library.

**5.2.1 Features.** We compare our data cleaning features with previous works, particularly those frequently used functionality in data science such as null value handling, special character removal, duplicate detection, etc.

**Table 3: Evaluation: Features Comparison**

	PySpark DataFrame[20]	PyPandas	Optimus[15]	SparklingPandas[17]	Dask[24]
<b>Data manipulation</b>					
Data integration	✓	✓	✓		✓
Data aggregation	✓	✓	✓	✓	✓
Data filtering	✓	✓	✓		✓
Data profiling	✓	✓	✓	✓	✓
Data sorting	✓	✓	✓		
<b>Basic data cleaning</b>					
Missing value filling	✓	✓	✓		✓
Missing value removing	✓	✓	✓		✓
Duplication removing	✓	✓	✓		✓
<b>Outlier Detection</b>					
Deviation with median			✓		
Clustering algorithms		✓			
<b>Scaling and Normalization</b>					
Standard scaling		✓			✓
Scale in range		✓	✓		✓
Normalization		✓	✓		
<b>Text Cleaning</b>					
Special character removing	✓	✓	✓		
Pattern searching	✓	✓	✓		
Pattern searching and replacement		✓	✓		
Common patterns replacement		✓			

**5.2.2 Performance.** We evaluate the performance of our library by measuring the time consumed and drawing comparison with existing libraries. This performance evaluation shows that this library is efficient and can be useful in production.

**5.2.3 Scalability.** We examine the scalability of our library by running the same task with different numbers of worker nodes. We measure the time consumed under different configuration and analyze the scalability. This evaluation shows how well the library can scale.

### 5.3 Results

After running our experiments on the Dumbo clusters of NYU initially, we migrate all our settings to Amazon Web Service because we could not obtain the privileges needed on Dumbo. While on Amazon Web Service, we can obtain the privileges needed to install other packages and we are able to perform comparison with other related works. In addition, on Amazon Web Service, we are able to customize the clusters we need, such as setting the number of worker nodes. This allows us to perform the scalability experiments.

**5.3.1 Features.** In this section, we compare our features with previous works. The result is shown in table 3. We find that PySpark DataFrame provide easy-to-use data manipulation functions. Since PyPandas and Optimus extend the DataFrame, both of them support the same data manipulation features. In SparklingPandas, the project

only aims to provide grouping methods on Pandas-liked dataframe and miss other important features in data manipulation. Dask also support many features in data manipulation.

PySpark DataFrame, Optimus, Dask, and our library PyPandas all provide the basic data cleaning functions like missing value handling. In the outlier detection, Optimus detects outliers by calculating the deviation with the median of data. On the other hand, PyPandas provides advance detection methods with clustering algorithms. Dask do support several clustering algorithms. Nonetheless, they are not integrated in their Dask DataFrame. Users have to manually train and tune the models to detect the outliers.

In scaling and normalization, Dask and PyPandas provide basic scaling methods like standard scaling or min-max scaling. However, Dask does not provide normalization on their Dask ML preprocessing module.

For the text cleaning, PyPandas provides more powerful pattern searching and replacement feature to let user find out any pattern and replace the matched one with their desired value. Moreover, PyPandas defines several common patterns for users to clean their text quickly without repeating themselves. In summary, PyPandas extends PySpark DataFrame and provides more easy-to-use features for users to clean their data.

**Table 4: Outlier Detection Experiment Result**

Dimension	k = 3	k = 4	k = 5
1	1 m 15.15 s	1 m 6.48 s	1 m 6.27 s
3	1 m 7.13 s	1 m 4.97 s	1 m 5.52 s
5	1 m 5.94 s	1 m 5.30 s	1 m 6.82 s
10	1 m 7.64 s	1 m 12.36 s	1 m 11.18 s
15	1 m 7.57 s	1 m 9.12 s	1 m 7.92 s

**Table 5: Scaling and Normalization Experiment Result**

	311 Service Requests	Permit Issuance	Job Application Filings
Standard Scale	3 m 8.15 s	1 m 25.57 s	1 m 19.96 s
Min-max Scale	3 m 7.15 s	1 m 25.95 s	1 m 20.07 s
Max-abs Scale	3 m 7.15 s	1 m 24.48 s	1 m 19.90 s
Normalization	1 m 18.95 s	38.41 s	39.48 s

**5.3.2 Performance.** We evaluate the performance of different parts of our library. The total of execution times of each task, including the time for Spark initialization, data loading, and data preprocessing, were all recorded and listed below.

- **Outlier Detection Experiment:** This experiment is performed on the DOB Job Application Filings Dataset. 15 columns that contain numerical values are chosen. We use K-Means Outlier Remover with three different k values [1, 2, 3]. For each k value setting, we run the clustering with different number of attributes (dimensions). The results are shown in table 4.
- **Scaling and Normalization Experiment:** This experiment involves all three testing datasets. We choose three columns with numerical values from each dataset as input. For each input, we test all scaling and normalization operations. The experiment results can be found in table 5.

**5.3.3 Scalability.** We evaluate the scalability of different functionalities of PyPandas. In our measurement, we uses the total execution times, which includes the time for Spark initialization, data loading, and data preprocessing.

- **Outlier Detection:** This experiment is performed on the 311 Service Requests Dataset. We perform outlier detection on one particular column that contains numerical values. We use both K-Means and Gaussian Mixture Outlier Remover with k value of 5. For each outlier remover, we use 4 configurations of the clusters. The 4 configurations are exactly the same, except they have different numbers of worker nodes. On each configuration, the same task is performed 3 times, and the average time consumed is record. From the experiment, we find that PyPandas outlier remover has great scalability. Each time we double the number of worker nodes, the performance improves significantly. Note that the improvement is not perfectly linear, because we include the spark initialization and data loading time in our measurement. As the number of workers increases, the overhead of the cluster also increases. The results are shown in table 6.

**Table 6: Outlier Detection - Scalability Experiment Result**

Number of Worker Nodes	KMeans	Gaussian Mixture
2	650.1718 s	1408.2266 s
4	394.6293 s	862.6323 s
6	299.1153 s	622.7715 s
8	270.4852 s	592.1259 s

## 6 CONCLUSIONS

Due to the lack of advance data cleaning features on Spark, we propose PyPandas, a data cleaning toolkit built on PySpark. We provide advance data cleaning features such as outlier detection, data scaling, and text pattern searching and replacement.

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