

# Inverse Kinematics

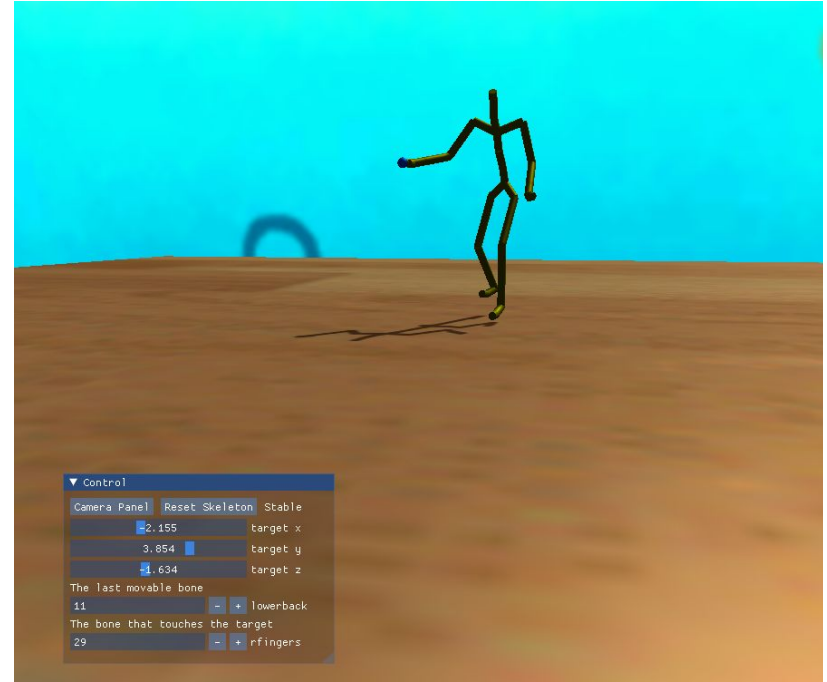
2023 Computer Animation and  
Special Effects

# Outline

- Overview
- Objective
- Report
- Scoring
- Submission

# Overview

- Use different bones to touch the ball
- Start bone
  - The last movable bone
- End bone
  - The bone that touches the ball



Demo link: [https://youtu.be/52-auc1\\_QUk](https://youtu.be/52-auc1_QUk)

# Objective

- Everything you need to implement is in `kinematics.cpp`
- There are three functions you need to implement in this homework
  - `void forwardSolver(...)`
  - `VectorXd pseudoInverseLinearSolver(...)`
  - `bool inverseJacobianIKSolver(...)`
- Bonus
  - Return whether IK is stable so that the skeleton would not swing its hand in the air
  - Take rotation limit of bones into consideration in `bool inverseJacobianIKSolver`

# Objective (cont.)

- `void forwardSolver(...)`
  - Goal
    - Implement forward kinematics, which is similar to HW2

# Objective (cont.)

- `VectorXd pseudoInverseLinearSolver(...)`
  - Goal
    - Find solution of linear least squares system, which will be needed for inverse kinematics
    - i.e. find  $x$  which  $\min(\| \text{jacobian} * x - \text{target} \|)$
  - Hint
    - You might use some pseudo-inverse methods such as **SVD**
    - There are some built-in functions in **Eigen** that you can use
    - **Eigen::Matrixs4Xf** means a matrix with 4 rows and unknown columns
      - `Eigen::Matrix4Xf m(4, 10);` // A matrix with 4 rows and 10 columns
    - **Eigen::VectorXf** means a vector with unknown size
      - `Eigen::VectorXf v(10);` // A vector with 10 elements

# Objective (cont.)

- `bool inverseJacobianIKSolver(...)`
  - Goal
    - Implement inverse kinematics
    - We use inverse-Jacobain method in this homework
  - Hint
    - Review "`kinematics.pptx`" from p.20 - p.50
    - Review "`acclaim_FK_IKnote.pdf`" Inverse Kinematics part
    - Traverse from `end bone` to `start bone`
      - Make `end bone` touch the ball (`target`)
      - `Start bone` is the last movable bone, so you should stop at this bone
    - You can check struct `Bone` in `bone.h`

# Report

- Suggested outline
  - Introduction/Motivation
  - Fundamentals
  - Implementation
  - Result and Discussion
    - How different step and epsilon affect the result
    - Touch the target or not
    - Least square solver
  - Bonus (Optional)
  - Conclusion



# Scoring

- Forward kinematics - 0%
- Least square solver -20%
- Inverse kinematics - 60%
- Report - 20%
- Bonus - 10%

# Submission

- Please upload only two files respectively
  - `kinematics.cpp`
  - `report_< your student ID>.pdf`
  - other necessary files (optional)
  - penalty of 5 points for incorrect submit format
- Late policies
  - Penalty of 10 points on each day after deadline
- Cheating policies
  - 0 points for any cheating on assignments
- Deadline
  - Sunday, 2023/05/14, 23:59