

Cal State Fullerton

College of Engineering and Computer Science

Project 1:

Implementing Algorithm for Sorting Disks

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Class: CPSC 335-11

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Introduction

In this first assignment for CS335 Algorithm class, we will implement two ways of sorting an alternating disks vector.

The definition of the problem is:

Input: a list of alternating light and dark disks size of $2n$, with n is a positive integer.

Output: sorted vector with dark disks on the left and light disks on the right.

Screenshots

A screenshot of a code editor window titled 'README.md' with the file path '~/Desktop/cs335/project-1-implementing-algorithms-holly'. The editor contains the following text:

```
1  [Review Assignment Due Date](https://classroom.github.com/assets/deadline-readme-button-24ddc0f5d75046c5622901739e7c5dd533143b0c8e959d652212380cedb1ea36.svg)  (https://classroom.github.com/a/nL7H4IG3)
2 # 335-project-1-starter
3 Alternating disks
4
5 Group members:
6
7 Name:
8
9 Holly Do
10
11 CSU Email:
12
13 hollydo@csu.fullerton.edu
14
15
```

```

holly@holly-VirtualBox:~/Desktop/cs335/project-1-implementing-algorithms-holly$ git push
Enumerating objects: 7, done.
Counting objects: 100% (7/7), done.
Delta compression using up to 17 threads
Compressing objects: 100% (4/4), done.
Writing objects: 100% (4/4), 393 bytes | 393.00 KiB/s, done.
Total 4 (delta 3), reused 0 (delta 0), pack-reused 0
remote: Resolving deltas: 100% (3/3), completed with 3 local objects.
To github.com:CSUF-Spring2024/project-1-implementing-algorithms-holly.git
 9456ec4..628da58  main -> main
holly@holly-VirtualBox:~/Desktop/cs335/project-1-implementing-algorithms-holly$ g++ -std=c++11 disks_test.cpp -o d
isks_test
holly@holly-VirtualBox:~/Desktop/cs335/project-1-implementing-algorithms-holly$ ./disks_test
disk_state still works: passed, score 1/1
sorted_disks still works: passed, score 1/1
disk_state::is_initialized: passed, score 1/1
disk_state::is_sorted: passed, score 1/1
alternate, n=3: passed, score 1/1
alternate, n=4: passed, score 1/1
alternate, other values: passed, score 1/1
lawnmower, n=3: passed, score 1/1
lawnmower, n=4: passed, score 1/1
lawnmower, other values: passed, score 1/1
TOTAL SCORE = 10 / 10
holly@holly-VirtualBox:~/Desktop/cs335/project-1-implementing-algorithms-holly$

```

Pseudo-Code

1/

sort_lawnmower (disk_state& before)

disk_state after = before; // 1

count = 0; //1

for j=0 to (count()/2) -1 do // (count()/2) -1 +1

for i=j to (count()-1)-j-1 jump 2 steps forward do // ((count()-1)-j-1 -j) / 2 +1

if (after[i]== DISK_LIGHT && after[i+1] == DISK_DARK) // 1+1+1 = 3

{

swap; //1

count++; //1

}

else do nothing //0

endif

for i = count()-1-j to 1+j-1 jump 2 steps backward do // (1+j-1 - (count()-1-j)) / 2 +1

if (after[i]== DISK_LIGHT && after[i+1] == DISK_DARK) //3

{

```
swap; //1
count++; //1
}
else do nothing
endif
endfor
endfor
```

```
return after;
```

```
2/
```

```
sort_alternate (disk_state& before)
```

```
disk_state after = before; //1
count = 0; //1
for j=0 to (count() -2) do // (count() -2) +1
for i=j to count()-2) jump 2 steps forward do // ((count() -2) - j ) / 2 +1
if (after[i]== DISK_LIGHT && after[i+1] == DISK_DARK) //3
{
swap; //1
count++; //1
}
else do nothing
endif
endfor
endfor
return after
```

Big O Analysis

The input disks arrangement starts with a white disk and then a black disk and so on until the end of the vector. The length of this array/vector is always even because we started with an integer n number of white disks then add n number of black disks. For the algorithms to complete the entire length of the vector, we need to make sure to set the iteration numbers correctly. For example, the `sort_alternate()` function needs to be repeated $n/2$ times, which means the last pair will be at indexes $(n/2)-1$ and $n/2$. Similarly, the `sort_lawnmower()` swapping decision needs to be iterated until the last pair of indexes $(n/2)-1$ and $n/2$. Below is the Big O analysis of the runtime for both functions.

`sort_lawnmower()`

$$1/ \text{ if } s.c = 3 + \max(2, 0) = 5$$

$$\text{inner loop } \neq 1: s.c = 5 \left(\frac{c-1-j-1-j}{2} + 1 \right) = \left(\frac{c}{2} - j \right) \cdot 5$$

$$\text{second inner for loop: } s.c = 5 \left(\frac{(1+j-1) - (c-1) - j}{-2} + 1 \right) = \left(\frac{c}{2} - j + 1 \right) 5.$$

$$\text{Total } s.c = 1 + 1 + \sum_{j=0}^{\frac{c}{2}-1} 5 \left(\frac{c}{2} - j \right) + \sum_{j=0}^{\frac{c}{2}-1} 5 \left(\frac{c}{2} - j + 1 \right)$$

$$= 2 + \sum_{j=0}^{\frac{c}{2}-1} 5 \left(\frac{c}{2} - j + \frac{c}{2} - j + 1 \right) = 2 + \sum_{j=0}^{\frac{c}{2}-1} 5(c - 2j + 1)$$

$$= 2 + 5 \left(\frac{c}{2} + 1 + 1 \right) - 10 \left(\frac{\left(\frac{c}{2} - 1 \right) \left(\frac{c}{2} \right)}{2} \right) + 5c \left(\frac{c}{2} - 1 + 1 \right)$$

$$= 2 + 5 \frac{c}{2} - 5 \left(\frac{c^2}{4} - \frac{c}{2} \right) + 5c \left(\frac{c}{2} \right)$$

$$= 2 + \frac{5c}{2} - \frac{5}{4}c^2 + \frac{5}{2}c + \frac{5c^2}{2} = 2 + 5c + \frac{5}{4}c^2$$

This belongs to big O of n^2 because largest term is n^2 (or c^2)

sort_alterate()

$$2) \text{ if s.c} = 3 + \max(2, 0) = 5$$

$$\text{inner for loop s.c} = 5 \cdot \left[\left(\frac{c-2-j}{2} \right) + 1 \right] = 5 \left(\frac{c-j}{2} \right)$$

$$\text{Total s.c} = 1 + 1 + \sum_{j=0}^{c-2} \frac{5c}{2} - \sum_{j=0}^{c-2} \frac{5j}{2}$$

$$= 2 + \frac{5}{2} c \cdot (c-2+1) - \frac{5}{2} \frac{(c-2)(c-1)}{2} = \cancel{2 + \frac{5c}{2} \cdot (c-1) - \frac{5}{4} (c-2)(c-1)}$$

$$= 2 + \frac{5}{2} c (c-1) - \frac{5}{4} (c^2 - c - 2c + 2)$$

$$= 2 + \frac{5}{2} c^2 - \frac{5}{2} - \frac{5}{4} (c^2 - 3c + 2)$$

$$= 2 + \frac{5}{2} c^2 - \frac{5}{2} - \frac{5}{4} c^2 + \frac{15}{4} c - \frac{10}{4}$$

$$= \frac{5}{4} c^2 + \frac{15}{4} c - 5 + 2 = \frac{5}{4} c^2 + \frac{15}{4} c - 3$$

This belongs to big O of n^2 (or c^2)