

Principles of Programming Languages

Lecture 6: Functions. Default data structures.

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Outline

Functions

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Default data structures

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- ▶ Input parameters, return value
- ▶ Call-by-value: pass a copy of the original object
- ▶ Call-by-reference: pass a reference to the original object

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int a;  
int b;  
function inc (int x) {  
    x = x + 1;  
    return x;  
};  
function main () {  
    b = inc(a);  
    return;  
}
```

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DEMO

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    <env> Rho:Map => Rho[X <- !L:Int] </env>  
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- ▶ Function declarations:

```
syntax Lambda ::= "lambda" "(" VarDecls "," Block ")"  
rule <k> (function X:Id ( P:VarDecls ) B => .) ...</k>  
      <env> Rho:Map => Rho[X <- !L:Int] </env>  
      <store> Sigma:Map => Sigma[!L <- lambda(P, B) ] </store>
```

- ▶ Demo

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- ▶ ... and a token declaration:

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```

- ▶ Also, declarations are followed by `execute`:

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<k> $PGM:Pgm ↪ execute </k>
```

- ▶ Now, `execute` triggers `main`:

```
rule (.Pgm ↪ execute) => main(.Params);
```

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syntax KResult ::= Int | Bool
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vs.

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syntax Val ::= Int | Bool
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syntax Vals ::= List{Val, ","}
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```
syntax Val ::= Int | Bool
```

```
syntax Vals ::= List{Val, ", "}
```

```
syntax KResult ::= Val | Vals
```

- ▶ Also, enable the use of `Vals` & `Val` in expressions or statements where `Params` & `AExp` (respectively) appear:

```
syntax Params ::= Vals
```

```
syntax AExp ::= Val
```

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- ▶ Function call - steps:
 1. Save the environment
 2. Build the new environment: declare parameters + initialise them with values
 3. Execute the body
 4. Return the computed value
 5. Restore the old environment
- ▶ To accomplish this we use the following 'setup' rule:

```
syntax KItem ::= "mkDecl" "(" VarDecls "," Vals ")"  
syntax KItem ::= "saveEnv"  
rule <k> X:Id (Vs:Vals) => saveEnv  $\hookrightarrow$  mkDecl(P, Vs)  $\hookrightarrow$  B ...</k>  
  <env>... X |-> L:Int ...</env>  
  <store>... L |-> lambda(P, B) ... </store>
```

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Append a new cell:

```
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Rule:

```
rule <k> saveEnv => . ...</k>  
  <env> Rho </env>  
  <fstack> (.List => ListItem(Rho)) ...</fstack>
```

Declare parameters + initialization

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Rules:

```
rule <k> mkDecl((int X:Id, Xs:VarDecls), (V:Int, Vs:Vals)) =>  
    mkDecl(Xs, Vs) ...</k>  
    <env> Rho:Map => Rho[X<-!L:Int] </env>  
    <store> Sigma:Map => Sigma[!L <- V] </store>  
  
rule mkDecl(.VarDecls,.Vals) => .
```

Execute the body

Execute the body

There is nothing to do here.

The body will be executed using the existing rules, as before.

Return + restore environment

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```
<return> .List </return>
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Rules:

```
rule <k> return V:Val ; => V ...</k>  
  <env> _ => Rho </env>  
  <fstack> (ListItem(Rho) => .List) ...</fstack>  
  <return> _ => ListItem(V) </return>
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  <env> _ => Rho </env>  
  <fstack> (ListItem(Rho) => .List) ...</fstack>  
  <return> _ => ListItem(V) </return>
```

```
syntax Val ::= "noValue"  
rule <k> return ; => . ...</k>  
  <env> _ => Rho </env>  
  <fstack> (ListItem(Rho) => .List) ...</fstack>  
  <return> _ => ListItem(noValue) </return>
```

Functions

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- ▶ Exercise: call-by-reference

Data structures

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- ▶ Examples: lists, arrays, trees, records, unions, classes, ...

In K:

- ▶ **Autoincluded builtins**: `Id`, `Int`, `Bool`, `String`, `List`, `Set`, `Map`, ...
- ▶ **Demo**: explore the `include` directory; show various functions

Next time...

... we will discuss a larger language definition with various features.

Lab this week

- ▶ Prepare for your test: solve and evaluate yourself!