

S:

$$P(a, x, g(x)) = P(u, v, w) \equiv P(a, x, y)$$

S	R	
\emptyset	$P(a, x, g(x)) = P(u, v, w) =$ $= P(a, x, y)$	Initial.
	$a = u, x = v, g(x) = w,$ $u = a \quad \quad \quad v = y,$ $w = y$	Desc.
$a = u$	$x = v, g(x) = w,$ $u = u, v = y, w = y.$	Rez.
$a = u$	$x = v, g(x) = w$ $v = y, w = y$	scote.
$x = v$ $a = u$	$g(v) = w, v = x,$ $w = y$	Rez.
$v = y$ $x = v$ $a = u$	$g(y) = w$ $w = y$	Rez.
$w = y$ $v = y$ $x = v$ $a = u$	$g(y) = y$	Exec

Examen iunie 2018

$$f(a, x, g(x)), f(u, u, w) \quad f(a, y, y)$$

$$a = ct$$

	A	B
init	$f(a, x, g(x)) = f(u, u, w)$ $f(u, u, w) = f(a, y, y)$	
Decompune	$a = u$ $x = u$ $g(x) = w$	$u = a$ $u = y$ $w = y$
Reduci ^o	$x = u$ $g(x) = w$	$u = y$ $w = y$
Reduci ^o	$x = u$ $g(x) = y$	$u = a$ $g(x) = w$
Reduci ^o	$x = u$ $u = g(x)$	$u = a$ $g(x) = w$ $g(x) = y$
Reduci^o ESEC	$x = g(x)$ ESEC	$u = a$ $u = g(x)$ $w = A(x)$ $y = g(x)$

5.14

5.11

- (1) $m(e, c)$
- (2) $m(d, e)$
- (3) $f(a, e)$
- (4) $f(a, c)$
- (5) $p(a)$
- (6) $p(d)$
- (7) $p(x) : \neg f(y, x), p(y)$

? - $p(x), m(y, x), p(y)$

- $G_0 = \neg p(x) \vee \neg m(y, x) \vee p(y)$
- $G_1 = \neg p(x) \vee \neg m(d, x)$ (SLD, 6, $\theta = \{x \leftarrow d\}$)
- $G_2 = \neg f(y, x_1) \vee \neg p(y) \vee \neg m(d, x)$ (SLD, 7, $\theta = \{x \leftarrow x_1, y \leftarrow y_1\}$)
- $G_3 = \neg f(a, x_1) \vee \neg m(d, x)$ (SLD 5 $\theta = \{x_1 \leftarrow a\}$)
- $G_4 = \neg m(d, x)$ (SLD, 3 $\theta = \{x \leftarrow d\}$)
- $G_5 = \square$ (SLD² $\theta = \{x \leftarrow d\}$)

5.11

$$\neg \xi, p \vee \xi, \Delta \rightarrow \neg p, \Delta \vdash \neg \eta.$$

1. $\neg \xi$ premisă
2. $p \vee \xi$ premisă
3. $\Delta \rightarrow \neg p$ premisă
4. Δ premisă

$$G_7 = \square$$

P₃

$\neg q$

$p \vee q$

$s \rightarrow \neg p$

$s \vdash \neg \wedge (\Rightarrow) \vdash s \rightarrow \neg \wedge$

① $\neg q$ premissa

② $p \vee q$ premissa

③ $s \rightarrow \neg p$ premissa

④ $p \vee \neg q$ ($\vee i$ 2, 1)

⑤ $\neg p$ hipótese

⑥ $\neg p$ ($\rightarrow e$ 3, 5)

⑦ $\neg p \wedge \neg q$ ($\wedge i$ 5, 6)

⑧ \perp ($\neg e$ 2, 7)

⑨ $\neg s$

⑩ $\vdash s \rightarrow \neg \wedge$

S_{III}. $\neg q, p \vee q, s \rightarrow \neg p, s \vdash \neg r.$

Premiza : 1. $\neg q$ premiza

2. $p \vee q$ premiza

3. $s \rightarrow \neg p$ premiza

4. s premiza

5. $\neg p$ ($\rightarrow e, 4$)

~~6. $\neg q$~~

S_{IV}. $\exists x \left(\underbrace{(\Delta(x) \vee \exists y P(y))}_{\mathcal{L}_1} \rightarrow \underbrace{(\forall y \Delta(y) \wedge P(c))}_{\mathcal{L}_2} \right)$

$$\exists x (\neg (\Delta(x) \vee \exists y P(y)) \vee (\forall y \Delta(y) \wedge P(c)))$$

$$\exists x ((\neg \Delta(x) \wedge \forall y \neg P(y)) \vee (\forall y \Delta(y) \wedge P(c)))$$

$$\exists x ((\neg \Delta(x) \wedge \forall y \neg P(y)) \vee (\forall w \Delta(w) \wedge P(c)))$$

$$\exists x \forall w \forall y ((\neg \Delta(x) \wedge \neg P(y)) \vee \underbrace{(\Delta(w) \wedge P(c))}_h)$$

$$\exists x \forall w \forall y ((\neg \Delta(x) \vee h) \wedge (\neg P(y) \vee h))$$

$$\exists x \forall w \forall y ((\neg \Delta(x) \vee (\Delta(w) \wedge P(c))) \wedge (\neg P(y) \vee (\Delta(w) \wedge P(c))))$$

$$\exists x \forall w \forall y ((\neg \Delta(w) \vee \Delta(w)) \wedge (\neg \Delta(x) \vee P(c)) \wedge ((\neg P(y) \vee \Delta(w)) \wedge$$

$$\exists x \forall w \forall y ((\neg \Delta(x) \vee P(c)) \wedge (\neg \Delta(x) \vee P(c)) \wedge (\neg P(y) \vee P(c)))$$

$$\exists x \forall w \forall y ((\neg \Delta(x) \vee P(c)) \wedge (\neg P(y) \vee \Delta(w)) \wedge (\neg P(y) \vee P(c)))$$

$$\forall w \forall y ((\neg \Delta(a) \vee P(c)) \wedge (\neg P(y) \vee \Delta(w)) \wedge (\neg P(y) \vee P(c)))$$

$$C = \{ \{ \neg D(a), P(c) \}, \{ \neg P(y), D(w) \}, \{ \neg P(y), P(c) \} \}$$

$$S_{\Sigma}. \quad \varphi := \forall x \forall y \forall z (P(x, f(a, y)) \wedge Q(f(x, y)) \wedge \neg P(b, f(z, b)))$$

$$\text{ari}(P) = 2$$

$$\text{ar}(Q) = 1$$

$$\text{ar}(f) = 2$$

a, b - const.

$$f(f(a, b), f(a, b)) \quad f(f(a, b), a)$$

$$f(a, f(a, b)) \quad f(b, f(a, b))$$

$$T(\varphi) = \{ a, b, f(a, b), f(f(a, b)), f(f(f(a, b))), \dots \}$$

$$\begin{aligned} \underline{\underline{Th(\varphi)}} = & \{ Q(a), Q(b), Q(f(a, b)), Q(f(f(a, b))), \dots \\ & P(a, b), P(f(a, b), f(a, b)), \\ & P(f(a, b), f(f(a, b))), \dots \\ & P(f(f(a, b), f(a, b))), \dots \\ & P(a, f(a, b)), P(a, f(f(a, b))) \} \end{aligned}$$

$$\begin{aligned} & Q(a), Q(b), Q(f(a, b)), Q(f(f(a, b))) \\ & P(a, b) \end{aligned}$$