

$\emptyset \neq T \supseteq A, B, C, D :=$ nonempty subsets.

$$T := A \cup B \cup C \cup D \cup \{0\}$$

$$P(\forall x \subseteq T)$$

$$\bar{X} := T \setminus X$$

$$(1) A \cap B \subseteq C \Delta D / nC; \quad C \Delta D = (C \setminus D) \cup (D \setminus C)$$

$$(2) B \cap C \subseteq (A \cap D) \cup (\bar{A} \cap \bar{D}) / nA$$

$$(3) \bar{A} \cap \bar{B} \subseteq \bar{C} \cap \bar{D} \subseteq C$$

$$(i) \bar{A} \cap \bar{B} \subseteq \bar{C}$$

$$(ii) A \cup B \cup C \subseteq \emptyset$$

$$(1) A \cap B \cap C \subseteq (C \Delta D) \cap C$$

$$\cancel{A \cap B \cap C} \subseteq [(C \setminus D) \cup (D \setminus C)] \cap C$$

$$= ((C \setminus D) \cap C) \cup ((D \setminus C) \cap C)$$

$$= C \setminus D$$

$$(1) \Rightarrow \boxed{A \cap B \cap C \subseteq C \setminus D}$$

$$(2) A \cap B \cap C = ((A \cap D) \cup (\bar{A} \cap \bar{D})) \cap A$$

$$\cancel{A \cap B \cap C}$$

$$\Rightarrow \text{dist. n false} \cup \quad \bar{A} \cap A \cap D = \emptyset$$

$$(A \cap D \cap A) \cup (\bar{A} \cap \bar{D} \cap A) = A \cap D$$

$$A \cap A \cap D = A \cap D \quad \emptyset$$

$$\boxed{A \cap B \cap C \subseteq A \cap D}$$

$$A \cap B \cap C \subseteq (C \setminus D) \cap (A \cap D) = (C \setminus D) \cap (D \cap A) \Rightarrow$$

$$\Rightarrow A \cap B \cap C = \emptyset$$