

```

In[ ]:= (* C3.AI COVID CHALLENGE *)

In[1127]:= Clear["Global`*"]

In[1128]:= type = "Cases_per_Million";
           policy = "C6_Policy";

In[1130]:= pD0 = 0.9640;
           pD1 = 0.0046;
           pD2 = 0.0268;
           pD3 = 0.0046;
           pD0 + pD1 + pD2 + pD3

Out[ ]:= 1.

In[ ]:= (* C0nditional Prob *)

In[1136]:= pD0C6l1 = 0.850239;
           pD1C6l1 = 0.9;
           pD2C6l1 = 0.9828;
           pD3C6l1 = 0.9;

In[1140]:= pD0C6l0 = 1 - pD0C6l1;
           pD1C6l0 = 1 - pD1C6l1;
           pD2C6l0 = 1 - pD2C6l1;
           pD3C6l0 = 1 - pD3C6l1;

In[ ]:= (* C6 - 1 *)

In[1145]:= prC6l0 = pD0 pD0C6l0 + pD1 pD1C6l0 + pD2 pD2C6l0 + pD3 pD3C6l0

Out[ ]:= 0.145751

In[1146]:= prC6l1 = pD0 pD0C6l1 + pD1 pD1C6l1 + pD2 pD2C6l1 + pD3 pD3C6l1

Out[ ]:= 0.854249

In[ ]:= (* Quantum Prob *)

In[1148]:= interfC6l0 = Sqrt[pD0 pD0C6l0 pD1 pD1C6l0] Cos[θ00 - θ10] +
           Sqrt[pD0 pD0C6l0 pD2 pD2C6l0] Cos[θ00 - θ20] +
           Sqrt[pD0 pD0C6l0 pD3 pD3C6l0] Cos[θ00 - θ30] +
           Sqrt[pD1 pD1C6l0 pD2 pD2C6l0] Cos[θ10 - θ20] +
           Sqrt[pD1 pD1C6l0 pD3 pD3C6l0] Cos[θ10 - θ30] +
           Sqrt[pD2 pD2C6l0 pD3 pD3C6l0] Cos[θ20 - θ30];

In[1149]:= interfC6l1 = Sqrt[pD0 pD0C6l1 pD1 pD1C6l1] Cos[θ01 - θ11] +
           Sqrt[pD0 pD0C6l1 pD2 pD2C6l1] Cos[θ01 - θ21] +
           Sqrt[pD0 pD0C6l1 pD3 pD3C6l1] Cos[θ01 - θ31] +
           Sqrt[pD1 pD1C6l1 pD2 pD2C6l1] Cos[θ11 - θ21] +
           Sqrt[pD1 pD1C6l1 pD3 pD3C6l1] Cos[θ11 - θ31] +
           Sqrt[pD2 pD2C6l1 pD3 pD3C6l1] Cos[θ21 - θ31];

In[1150]:= qprC6l0 = prC6l0 + 2 interfC6l0;

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In[1151]:= qprC6l1 = prC6l1 + 2 interfC6l1;

In[1152]:=

In[1153]:= qprC6l0Norm = FullSimplify[ $\frac{\text{qprC6l0}}{\text{qprC6l0} + \text{qprC6l1}}$ ];

In[1154]:= qprC6l1Norm = 1 - qprC6l0Norm;
(*FullSimplify[ $\frac{\text{qprC6l1}}{\text{qprC6l0} + \text{qprC6l1}}$ ]; *)

In[1155]:= res = Minimize[{qprC6l0Norm, qprC6l0Norm + qprC6l1Norm == 1},
{ $\theta00, \theta01, \theta10, \theta20, \theta30, \theta11, \theta21, \theta31$ }]

Out[1155]:= {0.0650655, { $\theta00 \rightarrow -1.26329, \theta01 \rightarrow 1.37013, \theta10 \rightarrow 1.8783, \theta20 \rightarrow 1.8783,$ 
 $\theta30 \rightarrow -4.40488, \theta11 \rightarrow 1.37013, \theta21 \rightarrow 1.37013, \theta31 \rightarrow 1.37013$ }}

In[1156]:= (* Params *)

In[1157]:=  $\theta10 = \text{res}[[2]][[3]][[2]]$ ;
 $\theta20 = \text{res}[[2]][[4]][[2]]$ ;
 $\theta30 = \text{res}[[2]][[5]][[2]]$ ;
 $\theta11 = \text{res}[[2]][[6]][[2]]$ ;
 $\theta21 = \text{res}[[2]][[7]][[2]]$ ;
 $\theta31 = \text{res}[[2]][[8]][[2]]$ ;

In[1158]:=

In[1159]:= qprC6l0Norm = FullSimplify[ $\frac{\text{qprC6l0}}{\text{qprC6l0} + \text{qprC6l1}}$ ];

In[1160]:= qprC6l1Norm = 1 - qprC6l0Norm;

In[1161]:= (* Updated probabilities *)

In[1162]:= {qprC6l0Norm, qprC6l1Norm}

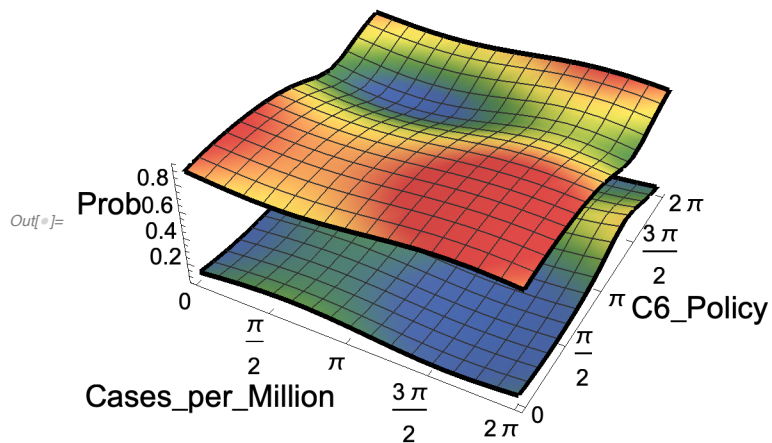
Out[1162]:= { $\left(4.55365 - 0.453944 \cos[\theta00] + 1.42939 \sin[\theta00]\right) / \left(32.281 + 1. \cos[1.8783 - \theta00] +\right.$ 
 $0.499739 \cos[4.40488 + \theta00] + 16.1546 \cos[1.37013 - \theta01]\right),$ 
 $1 - \left(4.55365 - 0.453944 \cos[\theta00] + 1.42939 \sin[\theta00]\right) / \left(32.281 +\right.$ 
 $1. \cos[1.8783 - \theta00] + 0.499739 \cos[4.40488 + \theta00] + 16.1546 \cos[1.37013 - \theta01]\right)}$ 

In[1163]:= p0 = Plot3D[qprC6l0Norm, { $\theta00, 0, 2\pi$ },
{ $\theta01, 0, 2\pi$ }, ColorFunction -> (ColorData["DarkRainbow"][#3] &),
AxesLabel -> {Style[type, 16], Style[policy, 16], Style["Prob", 16]},
BoundaryStyle -> Thick, Boxed -> False,
Ticks -> {{0, Pi/2, Pi, 3 Pi/2, 2 Pi}, {0, Pi/2, Pi, 3 Pi/2, 2 Pi}, Automatic},
TicksStyle -> Directive[Black, 12]];

In[1164]:= p1 = Plot3D[qprC6l1Norm, { $\theta00, 0, 2\pi$ },
{ $\theta01, 0, 2\pi$ }, ColorFunction -> (ColorData["DarkRainbow"][#3] &),
AxesLabel -> {Style[type, 16], Style[policy, 16], Style["Prob", 16]},
BoundaryStyle -> Thick, Boxed -> False,
Ticks -> {{0, Pi/2, Pi, 3 Pi/2, 2 Pi}, {0, Pi/2, Pi, 3 Pi/2, 2 Pi}, Automatic},
TicksStyle -> Directive[Black, 12]];

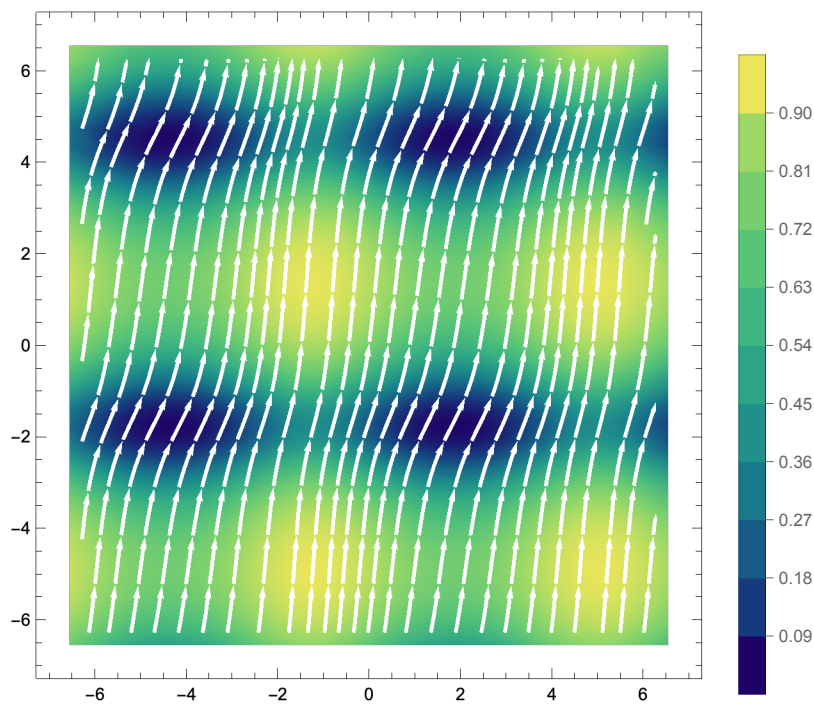
```

In[1170]:= Show[p0, p1]



In[]:=

In[1172]:= `fig = StreamDensityPlot[{qprC6l0Norm, qprC6l1Norm},
 {000, -2 π, 2 π}, {001, -2 π, 2 π}, ColorFunction → "BlueGreenYellow",
 PlotLegends → BarLegend[{"BlueGreenYellow", {0, 1}}, 10],
 AxesLabel → Automatic, StreamStyle → {White, Thick}]`



In[]:= Clear[010, 020, 030, 011, 021, 031]

In[]:= `res = Maximize[{qprC6l0Norm, qprC6l0Norm + qprC6l1Norm == 1},
 {000, 001, 010, 020, 030, 011, 021, 031}]`

Out[]:= {0.343433, {000 → 1.8783, 001 → -1.77146, 010 → 0.96554, 020 → -1.49878,
 030 → 1.61366, 011 → 0.495041, 021 → 0.328515, 031 → 0.159847}}

```

In[ ]:=  $\theta_{10} = \text{res}[[2]][[3]][[2]];$ 
 $\theta_{20} = \text{res}[[2]][[4]][[2]];$ 
 $\theta_{30} = \text{res}[[2]][[5]][[2]];$ 
 $\theta_{11} = \text{res}[[2]][[6]][[2]];$ 
 $\theta_{21} = \text{res}[[2]][[7]][[2]];$ 
 $\theta_{31} = \text{res}[[2]][[8]][[2]];$ 

In[ ]:=  $\text{qprC6l0Norm} = \text{FullSimplify}\left[\frac{\text{qprC6l0}}{\text{qprC6l0} + \text{qprC6l1}}\right];$ 

In[ ]:=  $\text{qprC6l1Norm} = 1 - \text{qprC6l0Norm};$ 

In[ ]:= (* Updated probabilities *)

In[ ]:= {qprC6l0Norm, qprC6l1Norm}

Out[ ]:= 
$$\left\{ \frac{8.88708 + 0.598153 \cos[\theta_{00}] + 0.82299 \sin[\theta_{00}]}{64.3066 + 0.598153 \cos[\theta_{00}] + 30.4127 \cos[\theta_{01}] + 0.82299 \sin[\theta_{00}] + 10.3507 \sin[\theta_{01}]}, \right.$$

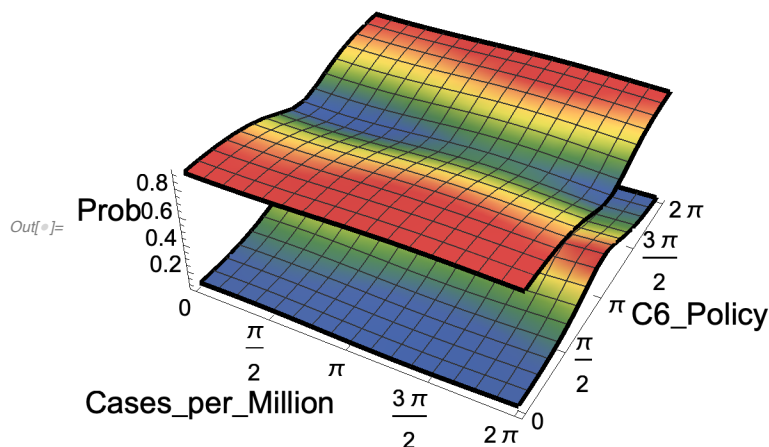

$$\left. 1 - \left( \frac{8.88708 + 0.598153 \cos[\theta_{00}] + 0.82299 \sin[\theta_{00}]}{64.3066 + 0.598153 \cos[\theta_{00}] + 30.4127 \cos[\theta_{01}] + 0.82299 \sin[\theta_{00}] + 10.3507 \sin[\theta_{01}]} \right) \right\}$$


In[ ]:=  $p_0 = \text{Plot3D}[\text{qprC6l0Norm}, \{\theta_{00}, 0, 2\pi\},$ 
 $\{\theta_{01}, 0, 2\pi\}, \text{ColorFunction} \rightarrow (\text{ColorData}["\text{DarkRainbow}"])[\#3] \&),$ 
 $\text{AxesLabel} \rightarrow \{\text{Style}[\text{type}, 16], \text{Style}[\text{policy}, 16], \text{Style}["\text{Prob}"], 16\},$ 
 $\text{BoundaryStyle} \rightarrow \text{Thick}, \text{Boxed} \rightarrow \text{False},$ 
 $\text{Ticks} \rightarrow \{\{0, \pi/2, \pi, 3\pi/2, 2\pi\}, \{0, \pi/2, \pi, 3\pi/2, 2\pi\}, \text{Automatic}\},$ 
 $\text{TicksStyle} \rightarrow \text{Directive}[\text{Black}, 12]];$ 

In[ ]:=  $p_1 = \text{Plot3D}[\text{qprC6l1Norm}, \{\theta_{00}, 0, 2\pi\},$ 
 $\{\theta_{01}, 0, 2\pi\}, \text{ColorFunction} \rightarrow (\text{ColorData}["\text{DarkRainbow}"])[\#3] \&),$ 
 $\text{AxesLabel} \rightarrow \{\text{Style}[\text{type}, 16], \text{Style}[\text{policy}, 16], \text{Style}["\text{Prob}"], 16\},$ 
 $\text{BoundaryStyle} \rightarrow \text{Thick}, \text{Boxed} \rightarrow \text{False},$ 
 $\text{Ticks} \rightarrow \{\{0, \pi/2, \pi, 3\pi/2, 2\pi\}, \{0, \pi/2, \pi, 3\pi/2, 2\pi\}, \text{Automatic}\},$ 
 $\text{TicksStyle} \rightarrow \text{Directive}[\text{Black}, 12]];$ 

In[ ]:= Show[p0, p1]

```



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In[ ]:= fig = StreamDensityPlot[{qprC6l0Norm, qprC6l1Norm},
  {000, -2  $\pi$ , 2  $\pi$ }, {001, -2  $\pi$ , 2  $\pi$ }, ColorFunction -> "BlueGreenYellow",
  PlotLegends -> BarLegend[{"BlueGreenYellow", {0, 1}}, 10],
  AxesLabel -> Automatic, StreamStyle -> {White, Thick}]

```

