

## 1343 – Aladdin and the Black Stones

It's said that Aladdin had to solve seven mysteries before getting the Magical Lamp which summons a powerful Genie. Here we are concerned about the third mystery.

In the cave, Aladdin found some black stones arranged in a line. The weights of the stones were not necessarily equal. Though the stones looked gentle, he soon found that he cannot even walk over the stones. Some strange magic were stopping him passing the stones. So, he planned to move the stones. But when he took the first stone, he heard a sound. And it said,

"Remove some stones leaving **even** number of stones, the outer pair should be the heaviest. If the pair is removed, the new outer pair should be the heaviest and if this pair is removed the new outer pair is the heaviest and so on. How many ways you can do? Find it and I will let you through."

Aladdin solved this task and moved forward. Now your task is to do the same, you are given  $n$  stones  $W_1, W_2, \dots, W_n$ , where  $W_i$  denotes the weight of the  $i^{\text{th}}$  stone. You can remove some stones leaving  $2m$  ( $m > 0$ ) stones as  $W_{p1}, W_{p2}, \dots, W_{p2m}$  such that

$$W_{p1} + W_{p2m} > W_{p2} + W_{p2m-1} > W_{p3} + W_{p2m-2} > \dots > W_{pm} + W_{pm+1}$$

Remember that you cannot change the order of the stones. Now your task is to find the number of ways you can do it. Two orderings are different if  $m$  is different or there is at least a position  $i$ , where the stones are different.

### Input

Input starts with an integer  $T$  ( $\leq 30$ ), denoting the number of test cases.

Each case starts with a line containing an integer  $n$  ( $2 \leq n \leq 500$ ) and  $n$  integers denoting the weight of the stones. Weights can be any integer between 1 and  $10^9$ .

### Output

For each case, print the case number and the number of possible orderings modulo  $2^{32}$ .

Sample Input	Output for Sample Input
4	Case 1: 3
3 1 1 1	Case 2: 7
4 1 4 7 20	Case 3: 6
4 10 18 2 9	Case 4: 61
7 2 4 1 4 5 9 13	

### Note

- For the first case, the valid orderings are  $\{1_{(\text{first stone})}, 1_{(\text{second stone})}\}$ ,  $\{1_{(\text{first stone})}, 1_{(\text{third stone})}\}$  and  $\{1_{(\text{second stone})}, 1_{(\text{third stone})}\}$ .
- For the second case, the valid orderings are,  $\{1, 4\}$ ,  $\{1, 7\}$ ,  $\{1, 20\}$ ,  $\{4, 7\}$ ,  $\{4, 20\}$ ,  $\{7, 20\}$ ,  $\{1, 4, 7, 20\}$ .