RECURSION, TREE RECURSION AND DATA ABSTRACTION

COMPUTER SCIENCE MENTORS CS 61A

February 18, 2019 to February 20, 2019

1 Recursion

1. Write a function is_sorted that takes in an integer n and returns true if the digits of that number are nondecreasing from right to left.

```
def is_sorted(n):
    """
    >> is_sorted(2)
    True
    >> is_sorted(22222)
    True
    >> is_sorted(9876543210)
    True
    >> is_sorted(9087654321)
    False
    """
```

2. (Spring 2015 MT1 Q3C) Implement the combine function, which takes a non-negative integer n, a two-argument function f, and a number result. It applies f to the first digit of n and the result of combining the rest of the digits of n by repeatedly applying f (see the doctests). If n has no digits (because it is zero), combine returns result.

2 Tree Recursion

1. Mario needs to jump over a series of Piranha plants, represented as a string of 0's and 1's. Mario only moves forward and can either *step* (move forward one space) or *jump* (move forward two spaces) from each position. How many different ways can Mario traverse a level without stepping or jumping into a Piranha plant? Assume that every level begins with a 1 (where Mario starts) and ends with a 1 (where Mario must end up).

Hint: Does it matter whether Mario goes from left to right or right to left? Which one is easier to check?

def	<pre>mario_number(level): """</pre>
	Return the number of ways that Mario can traverse the level, where Mario can either hop by one digit or two digits each turn. A level is defined as being an integer with digits where a 1 is something Mario can step on and 0 is something Mario cannot step on. >>> mario_number(10101)
	<pre>1 >>> mario_number(11101) 2 >>> mario_number(100101)</pre>
	0
	<pre>if:</pre>
	else:

2. James wants to print this week's discussion handouts for all the students in CS 61A. However, both printers are broken! The first printer only prints multiples of n pages, and the second printer only prints multiples of m pages. Help James figure out whether or not it's possible to print exactly total number of handouts!

has_sum(total, n, m):	
>>> has_sum(1, 3, 5)	
False	
>>> has_sum(5, 3, 5) $\#$ 0 \star 3 + 1 \star 5 = 5	
True	
>>> has_sum(11, 3, 5) $\#$ 2 * 3 + 1 * 5 = 11	
True	
п п п	
if	
returnelifelif	_
return	
return	

3. The next day, the printers break down even more! Each time they are used, the first printer prints a random x copies $50 \le x \le 60$, and the second printer prints a random y copies $130 \le y \le 140$. James also relaxes his expectations: he's satisfied as long as there's at least lower copies so there are enough for everyone, but no more than upper copies to prevent waste.

def	<pre>sum_range(lower, upper): """</pre>
	<pre>>>> sum_range(45, 60) # Printer 1 prints within this range True</pre>
	<pre>>>> sum_range(40, 55) # Printer 1 can print a number 56-60 False</pre>
	<pre>>>> sum_range(170, 201) # Printer 1 + 2 will print between 180 and 200 copies total</pre>
	True
	<pre>def copies(pmin, pmax): if:</pre>
	return
	elif:
	return
	return
	return copies(0, 0)

3 Data Abstraction

1. The following is an **Abstract Data Type (ADT)** for elephants. Each elephant keeps track of its name, age, and whether or not it can fly. Given our provided constructor, fill out the selectors:

```
def elephant(name, age, can_fly):
    """
    Takes in a string name, an int age, and a boolean can_fly.
    Constructs an elephant with these attributes.
    >>> dumbo = elephant("Dumbo", 10, True)
    >>> elephant_name(dumbo)
    "Dumbo"
    >>> elephant_age(dumbo)
    10
    >>> elephant_can_fly(dumbo)
    True
    """
    return [name, age, can_fly]

def elephant_name(e):

def elephant_age(e):
```

2. This function returns the correct result, but there's something wrong about its implementation. How do we fix it?

```
def elephant_roster(elephants):
    """

    Takes in a list of elephants and returns a list of their
        names.
    """

    return [elephant[0] for elephant in elephants]
```

3. Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):
```

```
def elephant_name(e):
    return e[0][0]
def elephant_age(e):
    return e[0][1]
def elephant_can_fly(e):
    return e[1]
```

4. How can we write the fixed elephant_roster function for the constructors and selectors in the previous question?

5. **(Optional)** Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):
    """
    >>> chris = elephant("Chris Martin", 38, False)
    >>> elephant_name(chris)
        "Chris Martin"
    >>> elephant_age(chris)
        38
    >>> elephant_can_fly(chris)
        False
    """
    def select(command)
```

```
return select
def elephant_name(e):
    return e("name")
def elephant_age(e):
    return e("age")
def elephant_can_fly(e):
    return e("can_fly")
```