

# RECURSION AND HIGHER ORDER FUNCTIONS

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COMPUTER SCIENCE MENTORS 61A

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## 1 Recursion

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Every Recursive function has three things.

1. One or more base cases
2. One or more ways to break the problem down into a smaller problem
  - E.g. Given a number as input, we need to break it down into a smaller number
3. Solve the smaller problem recursively; from that, form a solution to the original problem

1. Write `num_digits`, which takes in a number `n` and returns the number of digits it has.

```
def num_digits(n):  
    """Takes in an positive integer and returns the number of  
    digits.  
  
    >>> num_digits(0)  
    1  
    >>> num_digits(1)  
    1  
    >>> num_digits(7)  
    1  
    >>> num_digits(1093)  
    4  
    """
```

2. Write a function `is_sorted` that takes in an integer `n` and returns `true` if the digits of that number are increasing from right to left.

```
def is_sorted(n):  
    """Return true if the digit is in increasing order from  
    rightmost digit to leftmost digit. (Consecutive same digits  
    are allowed).  
    Also return true if it has only one digit. Return false  
    otherwise.  
  
    >>> is_sorted(2)  
    True  
    >>> is_sorted(22222)  
    True  
    >>> is_sorted(9876543210)  
    True  
    >>> is_sorted(9087654321)  
    False  
    """
```

## 2 Environment Diagrams

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3. Draw an environment diagram for the following code:

```
x = 20
def foo(y):
    x = 5
    def bar():
        return lambda y: x - y
    return bar

y = foo(7)
z = y()
print(z(2))
```

4. What would change here?

```
x = 20

def bar():
    return lambda y: x-y

def foo(y):
    x = 5
    return bar

y = foo(7)
z = y()
print(z(2))
```

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### 3 Higher Order Functions

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5. Write a higher order function that passes the following doctests. *Challenge:* Write the function body in one line.

```
"""
>>> from operator import add, mul
>>> a = mystery(add, 3)
>>> a(4) #equivalent to add(3,4)
7
>>> a(12)
15
>>> b = mystery(mul, 5)
>>> b(7) #equivalent to mul(5,7)
35
>>> b(1)
5
>>> c = mystery(lambda x, y: x*x + y, 4)
>>> c(5)
21
>>> c(7)
23
"""
```

6. What do these print out?

```
>>>foo = mystery(lambda a,b: a(b), lambda c: 5 + square(c))
>>>foo(-2)
```