

## Recursion

Every Recursive function has three things.

One or more base cases

One or more ways to break the problem down into a smaller problem

E.g. Given a number as input, we need to break it down into a smaller number

Solve the smaller problem recursively; from that, form a solution to the original problem

Write `num_digits`, which takes in a number `n` and returns the number of digits it has.

`def num_digits(n): """Takes in a positive integer and returns the number of digits.`

`""" num_digits(0)1 >>> num_digits(1)1 >>> num_digits(7)1 >>> num_digits(1093)4"""`

`[1in] if n < 10: return 1 else: return 1 + num_digits(n//10)`

Write a function `is_sorted` that takes in an integer `n` and returns true if the digits of that number are sorted.

`def is_sorted(n): """Return true if the digits are in increasing order from rightmost digit to leftmost digit. (C`

`""" is_sorted(2)True >>> is_sorted(22222)True >>> is_sorted(9876543210)True >>> is_sorted(9087654321)False`

`[1in] right_digit = n % 10; rest = n // 10; if rest == 0: return True; elif right_digit > rest % 10: return False; else: return is_sorted(rest)`

Environment Diagrams Draw an environment diagram for the following code:

`x = 20 def foo(y): x = 5 def bar(): return lambda y: x - y return bar`

`y = foo(7) z = y() print(z(2))`

`[2in] Output: 3`

`[scale=0.5]img/foobar.png`

What would change here?

`x = 20`

`def bar(): return lambda y: x-y`

`def foo(y): x = 5 return bar`

`y = foo(7) z = y() print(z(2))`

`[0.3in] Output: 18`

`[scale=0.5]img/foobar2.png`

## Higher Order Functions

Write a higher order function that passes the following doctests. *Challenge:* Write the function body

`""" """ from operator import add, mul """ a = mystery(add, 3) """ a(4) equivalent to add(3,4) 7 """`

`[2in] def mystery(f, x): def helper(y): return f(x,y) return helper`

One-line solution: `return lambda y: f(x,y)`

What do these print out? `""" foo = mystery(lambda a,b: a(b), lambda c: 5 + square(c)) """ foo(-2)`