

# MUTABLE DATA STRUCTURES AND DATA ABSTRACTIONS

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COMPUTER SCIENCE MENTORS 61A

February 15 to February 19, 2016

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## 1 Lists

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1. Draw box-and-pointer diagrams for the following:

```
>>> a = [1, 2, 3]
>>> a
```

**Solution:**

```
[1, 2, 3]
```

```
>>> a[2]
```

**Solution: 3**

```
>>> b = a
>>> a = a + [4, 5]
>>> a
```

**Solution:**

```
[1, 2, 3, 4, 5]
```

```
>>> b
```

**Solution:**

```
[1, 2, 3]
```

```
>>> c = a
```

```
>>> a = [4, 5]
```

```
>>> a
```

**Solution:**

```
[4, 5]
```

```
>>> c
```

**Solution:**

```
[1, 2, 3, 4, 5]
```

**Solution:** [Box and pointer diagram in Python Tutor - tinyurl.com/week5-bap](https://tinyurl.com/week5-bap)

2. Write a function that takes in a list `nums` and returns a new list with only the primes from `nums`. Assume that `is_prime(n)` is defined. You may use a `while` loop, a `for` loop, or a list comprehension.

```
def all_primes(nums):
```

**Solution:**

```
    result = []
    for i in nums:
        if is_prime(i):
            result = result + [i]
    return result
```

List comprehension:

```
return [x for x in nums if is_prime(x)]
```

## 2 Data Abstraction

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3. The following is an **Abstract Data Type (ADT)** for elephants. Each elephant keeps track of its name, age, and whether or not it can fly. Given our provided constructor, fill out the selectors:

```
def elephant(name, age, can_fly):  
    """  
    Takes in a string name, an int age, and a boolean can_fly.  
    Constructs an elephant with these attributes.  
    >>> dumbo = elephant("Dumbo", 10, True)  
    >>> elephant_name(dumbo)  
    "Dumbo"  
    >>> elephant_age(dumbo)  
    10  
    >>> elephant_can_fly(dumbo)  
    True  
    """  
    return [name, age, can_fly]  
def elephant_name(e):
```

**Solution:**

```
    return e[0]
```

```
def elephant_age(e):
```

**Solution:**

```
    return e[1]
```

```
def elephant_can_fly(e):
```

**Solution:**

```
    return e[2]
```

4. This function returns the correct result, but there's something wrong about its implementation. How do we fix it?

```
def elephant_roster(elephants):  
    """  
    Takes in a list of elephants and returns a list of their  
    names.  
    """  
    result = []  
    for elephant in elephants:  
        result = result + [elephant[0]]  
    return result
```

**Solution:**

elephant[0] is a Data Abstraction Violation (DAV).  
We should use a selector instead.

5. Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):
```

**Solution:**

```
    return [[name, age], can_fly]
```

```
def elephant_name(e):  
    return e[0][0]  
def elephant_age(e):  
    return e[0][1]  
def elephant_can_fly(e):  
    return e[1]
```

6. How can we write the fixed `elephant_roster` function for the constructors and selectors in the previous question?

**Solution:** No change is necessary to fix `elephant_roster` since using the `elephant` selectors “protects” the roster from constructor definition changes.

7. (Optional) Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):  
    """  
    >>> chris = elephant("Chris Martin", 38, False)  
    >>> elephant_name(chris)  
        "Chris Martin"  
    >>> elephant_age(chris)  
        38  
    >>> elephant_can_fly(chris)  
        False  
    """  
    def select(command)
```

**Solution:**

```
        if command == "name":  
            return name  
        elif command == "age":  
            return age  
        elif command == "can_fly":  
            return can_fly  
        return "Breaking abstraction barrier!"  
    return select  
def elephant_name(e):  
    return e("name")  
def elephant_age(e):  
    return e("age")  
def elephant_can_fly(e):  
    return e("can_fly")
```

### 3 Trees

#### Things to remember

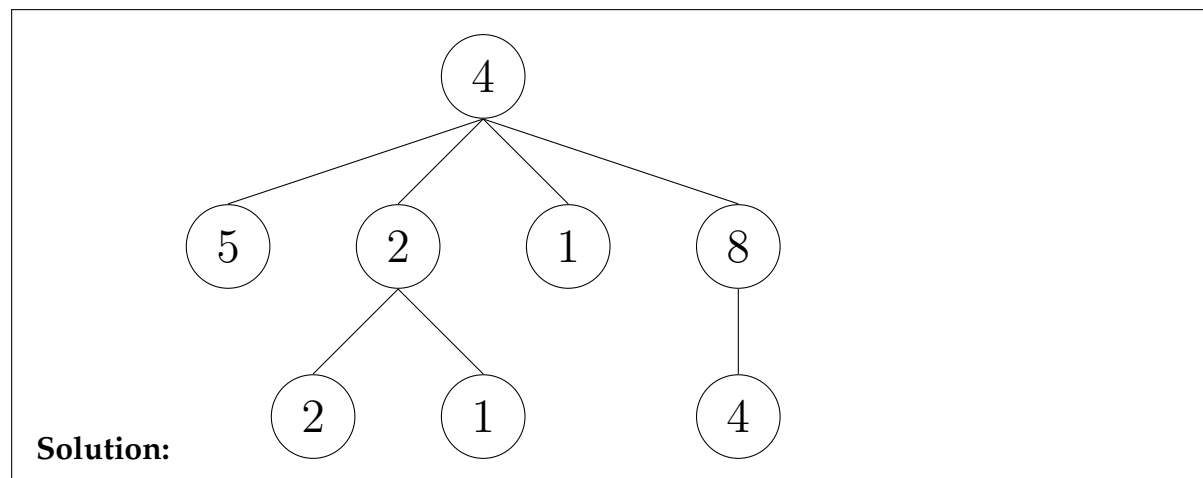
```
def tree(root, branches=[]): # ALWAYS OUTPUTS A TREE
    for branch in branches:
        assert is_tree(branch), 'branches must be trees'
    return [root] + list(branches)
```

```
def root(t): # ALWAYS OUTPUTS A NUMBER
    return t[0]
```

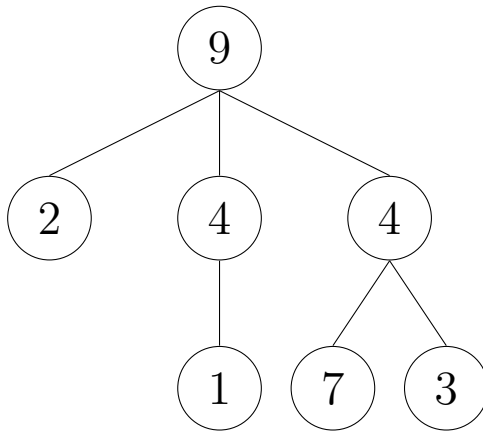
```
def branches(t): # ALWAYS OUTPUTS A LIST
    return t[1:]
```

8. Draw the tree that is created by the following statement:

```
tree(4,
    [tree(5, []),
     tree(2,
        [tree(2, []),
         tree(1, [])]),
     tree(1, []),
     tree(8,
        [tree(4, [])])])
```



9. Construct the following tree and save it to the variable `t`.



**Solution:**

```
t = tree(9, [tree(2, []),
              tree(4, [tree(1, [])]),
              tree(4, [tree(7, []),
                      tree(3, [])])])
```

10. What would this output?

```
>>> root(t)
```

**Solution:** 9

```
>>> branches(t)[2]
```

**Solution:**

```
tree(4, [tree(7, []), tree(3, [])])
```

```
>>> branches(branches(t)[2])[0]
```

**Solution:**

```
tree(7, [])
```

11. Write the Python expression to get the integer 2 from `t`.

**Solution:**

```
root(branches(t)[0])
```

12. Write the function `sum_of_nodes` which takes in a tree and outputs the sum of all the elements in the tree.

```
def sum_of_nodes(t):  
    """  
    >>> t = Tree(...) # Tree from question 2.  
    >>> sum_of_nodes(t) # 9 + 2 + 4 + 4 + 1 + 7 + 3 = 30  
    30  
    """
```

**Solution:**

```
total = root(t)  
for branch in branches(t):  
    total += sum_of_nodes(branch)  
return total  
  
Alternative solution:  
return root(t) +\  
    sum([sum_of_nodes(b) for b in branches(t)])
```