RECURSION AND HIGHER ORDER FUNCTIONS

COMPUTER SCIENCE MENTORS 61A

February 15 to February 19, 2016

Lists

1. Draw box-and-pointer diagrams for the following.

```
>>> a = [1, 2, 3] >>> a
```

Solution:

Solution: 3

```
>>> b = a
>>> a = a + [4, 5]
>>> a
```

Solution:

>>> b

Solution:

Solution:

>>> C

Solution:

Solution: Box and pointer diagram in Python Tutor.

2. Write a function that takes in a list nums and returns a new list with only the primes from nums. Assume that is_prime(n) is defined. You may use a while loop, a for loop, or a list comprehension.

def all_primes(num):

```
Solution:
    result = []
    for i in nums:
        if is_prime(i):
            result = result + [i]
    return result

List comprehension:
    return [x for x in nums if is_prime(x)]
```

2 Data Abstraction

1. The following is an **Abstract Data Type (ADT)** for elephants. Each elephant keeps track of its name, age, and whether or not it can fly. Given our provided constructor, fill out the selectors:

```
def elephant(name, age, can_fly):
    Takes in a string name, an int age, and a boolean can_fly.
    Constructs an elephant with these attributes.
    >>> dumbo = elephant("Dumbo", 10, True)
    >>> elephant_name(dumbo)
        "Dumbo"
    >>> elephant_age(dumbo)
    >>> elephant_can_fly(dumbo)
        True
    11 11 11
    return [name, age, can_fly]
def elephant name(e):
 Solution:
     return e[0]
def elephant_age(e):
 Solution:
     return e[1]
def elephant_can_fly(e):
 Solution:
     return e[2]
```

2. This function returns the correct result, but there's something wrong about its implementation. How do we fix it?

```
def elephant_roster(elephants):
    """

    Takes in a list of elephants and returns a list of their
        names.
    """

    result = []
    for elephant in elephants:
        result = result + [elephant[0]]
    return result
```

Solution:

```
elephant[0] is a Data Abstraction Violation (DAV). We should use a selector instead.
```

3. Fill out the following constructor for the given selectors.

def elephant (name, age, can_fly):

```
Solution:
    return [[name, age], can_fly]

def elephant_name(e):
```

```
def elephant_name(e):
    return e[0][0]
def elephant_age(e):
    return e[0][1]
def elephant_can_fly(e):
    return e[1]
```

4. How can we write the fixed elephant_roster function for the constructors and selectors in the previous question?

Solution: No change is necessary to fix elephant_roster since using the elephant selectors "protects" the roster from constructor definition changes.

5. **(Optional)** Fill out the following constructor for the given selectors.

```
def elephant(name, age, can_fly):
    """"
    >>> chris = elephant("Chris Martin", 38, False)
    >>> elephant_name(chris)
        "Chris Martin"
    >>> elephant_age(chris)
        37
    >>> elephant_can_fly(chris)
        False
    """
    def select(command)
```

```
Solution:
    if command == "name":
        return name
    elif command == "age":
        return age
    elif command == "can_fly":
        return can_fly
    return "Breaking abstraction barrier!"
```

```
return select
def elephant_name(e):
    return e("name")
def elephant_age(e):
    return e("age")
def elephant_can_fly(e):
    return e("can_fly")
```

3 Trees

Things to remember

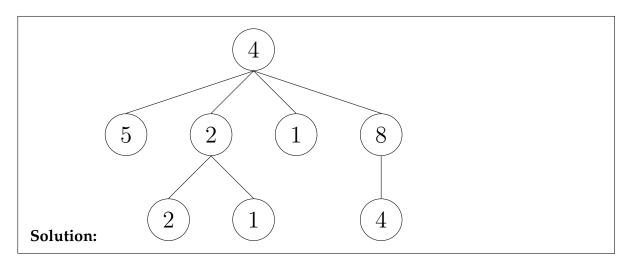
```
def tree(root, branches=[]): # ALWAYS OUTPUTS A TREE
    for branch in branches:
        assert is_tree(branch), 'branches must be trees'
    return [root] + list(branches)

def root(t): # ALWAYS OUTPUTS A NUMBER
    return t[0]
```

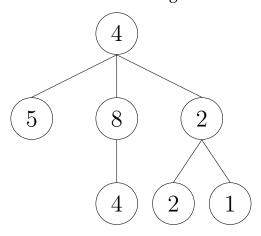
```
def branches(t): # ALWAYS OUTPUTS A LIST
    return t[1:]
```

1. Draw the tree that is created by the following statement:

```
tree(4,
    [tree(5, []),
    tree(2,
        [tree(2, []),
        tree(1, [])]),
    tree(1, []),
    tree(8,
        [tree(4, [])])])
```



2. Construct the following tree and save it to the variable t.



3. What would this output?

>>> root(t)

Solution: 9

>>> branches(t)[2]

```
Solution: tree(4, [tree(7, []), tree(3, [])])
```

>>> branches (branches (t) [2]) [0]

```
Solution:
tree(7, [])
```

4. Write the Python expression to get the integer 2 from t.

```
Solution:
root (branches (t) [0])
```

5. Write the function sum_of_nodes which takes in a tree and outputs the sum of all the elements in the tree.

```
def sum_of_nodes(t):
    """

>>> t = Tree(...) # Tree from question 2.

>>> sum_of_nodes(t) # 9 + 2 + 4 + 4 + 1 + 7 + 3 = 30
30
"""
```

```
Solution:
    sum = 0
    for branch in branches(t):
        sum += sum_of_nodes(branch)
    sum += root(t)
    return sum

Alternative solution:
    return root(t) +\
        sum([sum_of_nodes(b) for b in branches(t)])
```