

## Making Analysis of Algorithms and Data Structures Make Sense

Catherine Leung  
School of ICT  
Seneca College

## Contents

- Review of Big-O notation
- Growth Rates
- Counting operations
- Examples
- Resources

## Algorithm and Data Structures

- Ways to store, retrieve, and manipulate data

## Analysis

- Measure for resource usage
- Resources:
  - Anything consumed by your program is a resource
  - Top two are time and memory
  - But not only those two

## Big-O

- A way to measure resource needs
- Based on amount of data
- Does NOT measure amount of resources needed to process  $n$  pieces of data
- Does measure amount of resource increase to process  $n+1$  pieces of data
- All about growth rates!

## Formally

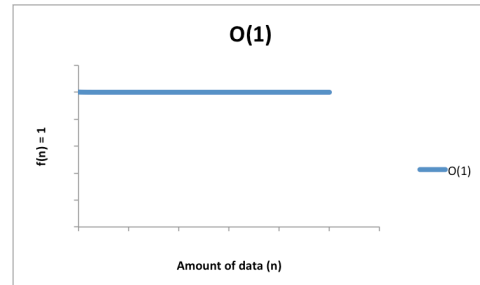
- Let the function  $T(n)$  represent the amount of resources needed to process  $n$  pieces of data by a particular algorithm
- $T(n)$  is  $O(f(n))$  iff there exists two constants  $c$  and  $n_0$  such that  $T(n) \leq c f(n)$  for all  $n > n_0$
- Yikes! How to explain that?

### The $f(n)$ inside the $O()$

- The function  $f(n)$  describes a curve

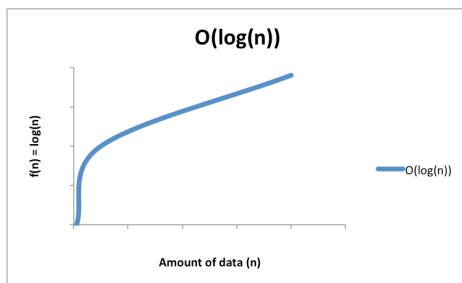
$$f(n) = 1$$

constant



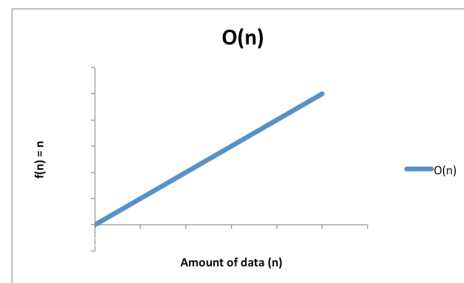
$$f(n) = \log(n)$$

logarithmic

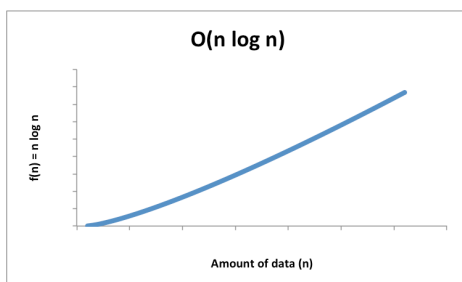


$$f(n) = n$$

linear

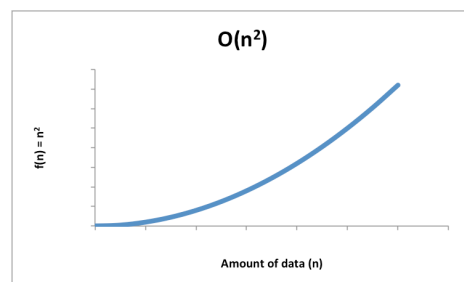


$$f(n) = n \log n$$

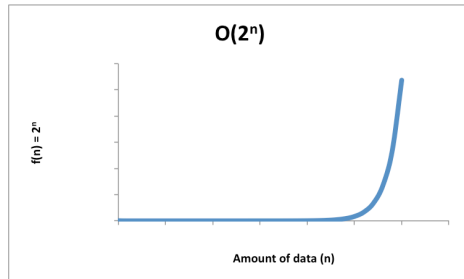


$$f(n) = n^2$$

Quadratic



$$f(n) = 2^n$$



## Big-O as a rating system

- $O(1)$
- $O(\log n)$
- $O(n)$
- $O(n \log n)$
- $O(n^2)$
- $O(n^3)$
- $O(2^n)$

smaller growth in  
resource need

larger growth in  
resource need

## The $c$ and $n_0$

- $T(n)$  is  $O(f(n))$  iff there exists two constants  $c$  and  $n_0$  such that  $T(n) \leq c f(n)$  for all  $n > n_0$
- If we can describe our resource need with a function  $T(n)$  we can give it a “rating”, a best fit curve
- The  $c$  allows us to stretch the curve
- The  $n_0$  allows the statement to not have to be true for all  $n$ ,  $n > n_0$

## Linear Search

```
int linearSearch(int key, int arr[],
                 int size){
    int rc=-1;
    for(int i=0; i<size && rc==-1; i++){
        if(arr[i]==key){
            rc=i;
        }
    }
    return rc;
}
```

## More...

- Lots of DS and algs to choose from... please pick:
  - Stacks/Queues (implementation array vs. linked list)
  - Heaps and Heapsort
  - Binary search trees
  - Hash Tables

## Resources

- Code/slides from this talk:
  - <https://github.com/cathyatseneca/CEMC2015>
- My data structures and algorithms notes:
  - <https://www.gitbook.com/book/cathyatseneca/data-structures-and-algorithms/details>
- My animations:
  - <http://cathyatseneca.github.io/DSAnim/index.html>