# R Notebook: Panel Data Models with R - October 2021

This is an R Markdown Notebook. When you execute code within the notebook, the results appear beneath the code.

Try executing this chunk by clicking the Run button within the chunk or by placing your cursor inside it and pressing Cmd+Shift+Enter (in Windows press CTRL+Enter).

Add a new chunk by clicking the *Insert Chunk* button on the toolbar or by pressing Cmd+Option+I (or CTRL+Alt+I in Windows).

When you save the notebook, an HTML file containing the code and output will be saved alongside it (click the Preview button or press Cmd+Shift+K to preview the HTML file).

The preview shows you a rendered HTML copy of the contents of the editor. Consequently, unlike *Knit*, *Preview* does not run any R code chunks. Instead, the output of the chunk when it was last run in the editor is displayed.

# Package Management Tool

Here I am uploading my packages (code omitted).

# Prepare the data

Here I am reading a Stata data file (code omitted).

# **Statistics**

## 3

72

1

```
names(nlswork)
                                "birth_yr" "age"
    [1] "idcode"
                    "year"
                                                       "race"
                                                                   "msp"
   [7] "nev_mar"
                                "collgrad" "not_smsa"
                                                                   "south"
                    "grade"
                                                      "c_city"
## [13] "ind_code"
                    "occ_code" "union"
                                           "wks_ue"
                                                       "ttl_exp"
                                                                   "tenure"
## [19] "hours"
                    "wks_work" "ln_wage"
 head(nlswork)
## # A tibble: 6 x 21
##
     idcode year birth_yr
                              age race
                                           msp nev_mar grade collgrad not_smsa c_city
##
      <dbl> <dbl>
                      <dbl> <dbl> <dbl> <dbl> <
                                                  <dbl> <dbl>
                                                                  <dbl>
                                                                           <dbl>
                                                                                   <dbl>
## 1
                                                                               0
          1
               70
                         51
                               18
                                       2
                                             0
                                                      1
                                                           12
                                                                      0
                                                                                       1
## 2
          1
               71
                         51
                               19
                                       2
                                             1
                                                      0
                                                           12
                                                                      0
                                                                               0
                                                                                       1
```

1

20

51

2

12

0

0

1

```
## 4
       1
             73
                      51
                            21 2 1
                                                  12
                                                                             1
## 5
              75
                      51
                            23
                                  2
                                        1
                                               0
                                                    12
                                                             0
                                                                             1
         1
                            25
                                  2
## 6
              77
                      51
                                        0
                                               0
                                                    12
                                                             0
                                                                             1
## # ... with 10 more variables: south <dbl>, ind_code <dbl>, occ_code <dbl>,
    union <dbl>, wks_ue <dbl>, ttl_exp <dbl>, tenure <dbl>, hours <dbl>,
      wks_work <dbl>, ln_wage <dbl>
# str(nlswork)
 # dplyr::glimpse(nlswork)
dplyr::glimpse(nlswork$ln_wage)
## num [1:28534] 1.45 1.03 1.59 1.78 1.78 ...
## - attr(*, "label")= chr "ln(wage/GNP deflator)"
```

# ExpData(nlswork, type=1)

## - attr(\*, "format.stata")= chr "%9.0g"

##		Descriptions	Value
##	1	Sample size (nrow)	28534
##	2	No. of variables (ncol)	21
##	3	No. of numeric/interger variables	21
##	4	No. of factor variables	0
##	5	No. of text variables	0
##	6	No. of logical variables	0
##	7	No. of identifier variables	0
##	8	No. of date variables	0
##	9	No. of zero variance variables (uniform)	0
##	10	%. of variables having complete cases	33.33% (7)
##	11	%. of variables having >0% and <50% missing cases	66.67% (14)
##	12	%. of variables having >=50% and <90% missing cases	0% (0)
##	13	%. of variables having >=90% missing cases	0% (0)

#### ExpData(nlswork,type=2)

##		Index	Variable_Name	Variable_Type	Sample_n	Missing_Count	Per_of_Missing
##	1	1	idcode	numeric	28534	0	0.000
##	2	2	year	numeric	28534	0	0.000
##	3	3	birth_yr	numeric	28534	0	0.000
##	4	4	age	numeric	28510	24	0.001
##	5	5	race	numeric	28534	0	0.000
##	6	6	msp	numeric	28518	16	0.001
##	7	7	nev_mar	numeric	28518	16	0.001
##	8	8	grade	numeric	28532	2	0.000
##	9	9	collgrad	numeric	28534	0	0.000
##	10	10	${\tt not\_smsa}$	numeric	28526	8	0.000
##	11	11	c_city	numeric	28526	8	0.000
##	12	12	south	numeric	28526	8	0.000
##	13	13	ind_code	numeric	28193	341	0.012
##	14	14	occ_code	numeric	28413	121	0.004
##	15	15	union	numeric	19238	9296	0.326
##	16	16	wks_ue	numeric	22830	5704	0.200

##	17	17	ttl_exp	numeric	28534	0	0.000
##	18	18	tenure	numeric	28101	433	0.015
	19	19	hours	numeric	28467	67	0.002
	20	20	wks_work	numeric	27831	703	0.025
##	21	21	ln_wage	numeric	28534	0	0.000
##			distinct_values				
##	1		4711				
##			15				
##	3		14				
##	4		33				
##	5		3				
##	6		2				
##	7		2				
##	8		19				
##	9		2				
##	10		2				
##	11		2				
##	12		2				
##	13		12				
##	14		13				
##	15		2				
##	16		61				
##	17		4744				
##	18		270				
##	19		85				
##	20		105				
##	21		8173				

# Exploratory data analysis

Start discussing the statistics and graphs.

```
## grade

## Min. : 0.00

## 1st Qu.:12.00

## Median :12.00

## Mean :12.53

## 3rd Qu.:14.00

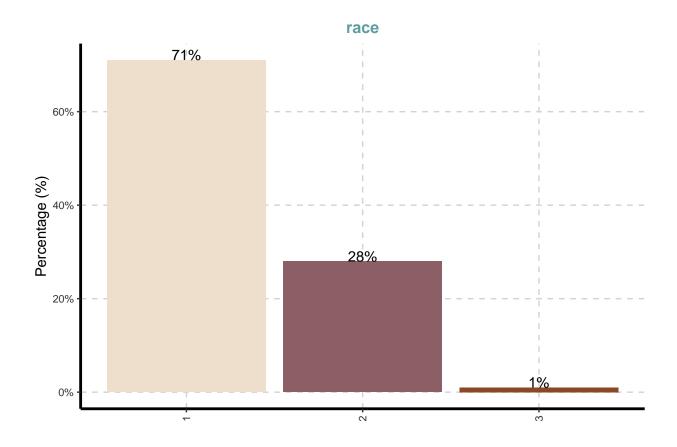
## Max. :18.00

## NA's :2
```

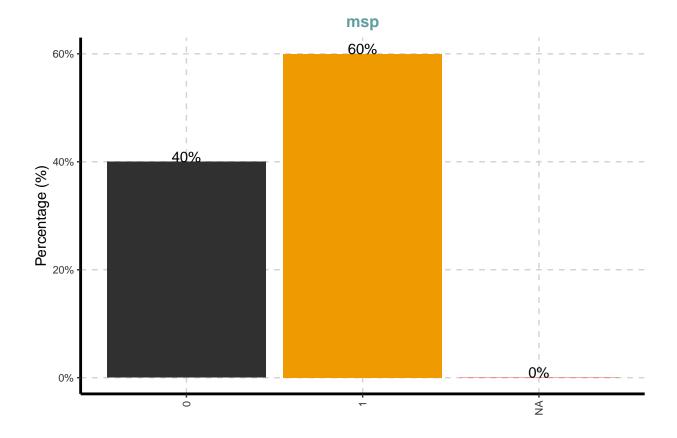
##		Vname	Group	TN	nNeg	nZero	nPos	NegInf	PosInf	NA_Value	Per_of_Missing
##	4	age	All	28534	0	0	28510	0	0	24	0.08
##	3	birth_yr	All	28534	0	0	28534	0	0	0	0.00
##	5	grade	All	28534	0	21	28511	0	0	2	0.01
##	11	hours	All	28534	0	0	28467	0	0	67	0.23
##	1	idcode	All	28534	0	0	28534	0	0	0	0.00
##	6	${\tt ind\_code}$	All	28534	0	0	28193	0	0	341	1.20
##	13	ln_wage	All	28534	0	2	28532	0	0	0	0.00
##	7	occ_code	All	28534	0	0	28413	0	0	121	0.42
##	10	tenure	All	28534	0	1248	26853	0	0	433	1.52
##	9	ttl_exp	All	28534	0	21	28513	0	0	0	0.00
##	8	wks_ue	All	28534	0	17394	5436	0	0	5704	19.99

##	12	wks_work	All	28534	0 478	27353	0 0	703		2.46
##	2	year	All	28534	0 0	28534	0 0	0		0.00
##		\$	sum min	max	mean	median	SD CV	IQR	Skewness	
##	4	828076	.00 14	46.00	29.05	28.00	6.70 0.23	11.00	0.26	
##	3	1372060	.00 41	54.00	48.09	48.00	3.01 0.06	5.00	-0.12	
##	5	357580	.00 0	18.00	12.53	12.00	2.32 0.19	2.00	0.10	
##	11	1040741	.00 1	168.00	36.56	40.00	9.87 0.27	5.00	-0.90	
##	1	74225046	.00 1	5159.00	2601.28	2606.00	1487.36 0.57	2554.00	-0.02	
##	6	216888	.00 1	12.00	7.69	7.00	2.99 0.39	6.00	0.00	
##	13	47791	.80 0	5.26	1.67	1.64	0.48 0.29	0.60	0.33	
##	7	135748	.00 1	13.00	4.78	3.00	3.07 0.64	3.00	1.08	
##	10	87782	.92 0	25.92	3.12	1.67	3.75 1.20	3.67	1.94	
##	9	177347	.83 0	28.88	6.22	5.06	4.65 0.75	6.67	0.86	
##	8	58173	.00 0	76.00	2.55	0.00	7.29 2.86	0.00	4.02	
##	12	1502577	.00 0	104.00	53.99	52.00	29.03 0.54	36.00	0.19	
##	2	2224472	.00 68	88.00	77.96	78.00	6.38 0.08	11.00	0.09	
##		${\tt Kurtosis}$	10%	20%	50%	LB.25%	UB.75% nOu	tliers		
##	4	-0.91	21.00	23.00	28.00	6.50	50.50	0		
##	3	-0.99	44.00	45.00	48.00	38.50	58.50	0		
##	5	1.37	10.00	12.00	12.00	9.00	17.00	2125		
##	11	4.26	20.00	32.00	40.00	27.50	47.50	6100		
##	1	-1.19	518.00	1051.00	2606.00	-2504.00	7712.00	0		
##	6	-1.46	4.00			-4.00	20.00	0		
##	13	1.67	1.17	1.30	1.64	0.46	2.87	660		
##	7	0.68	1.00	3.00			10.50	1846		
##	10	3.90	0.17	0.42	1.67	-5.00	9.67	2138		
##	9	0.06	1.04	2.00	5.06			191		
##	8	18.25	0.00	0.00	0.00	0.00	0.00	5436		
##	12	-0.68	14.00	28.00	52.00	-18.00	126.00	0		
##	2	-1.30	70.00	71.00	78.00	55.50	99.50	0		

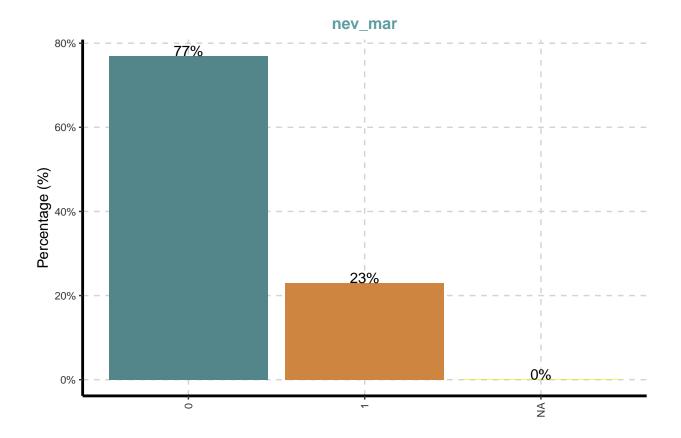
## [[1]]



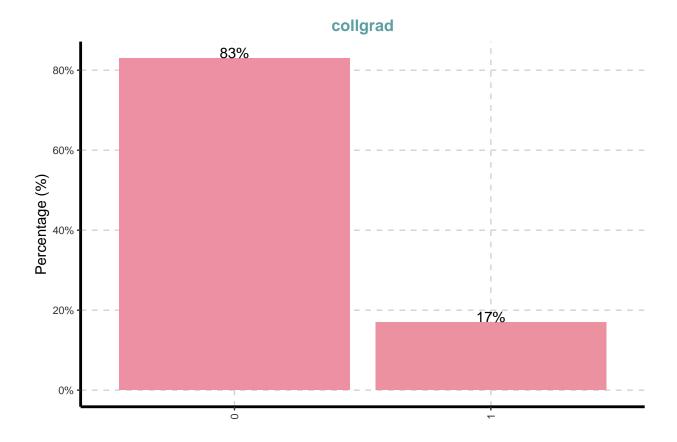
## ## [[2]]



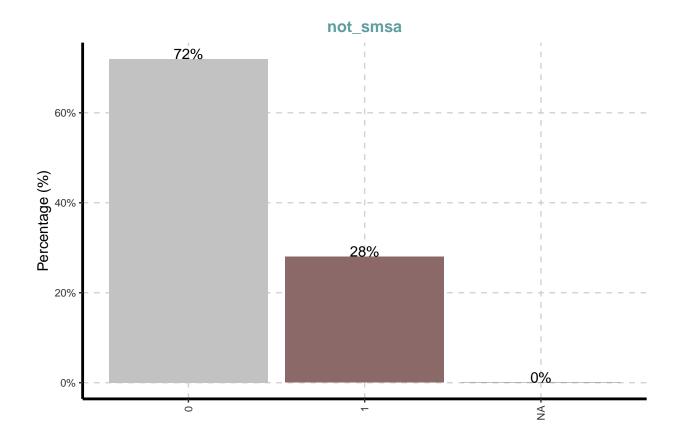
## ## [[3]]



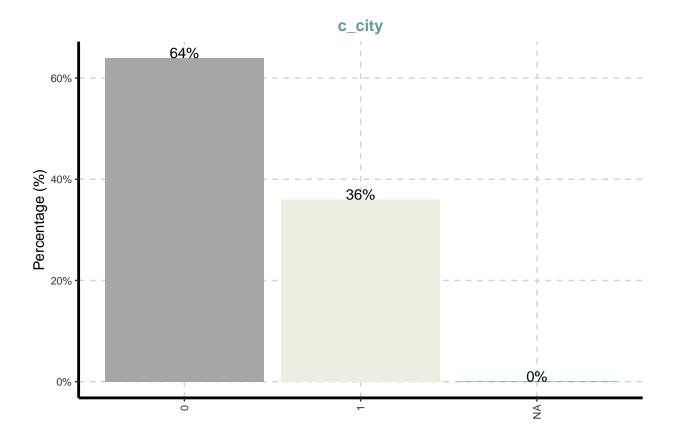
## ## [[4]]



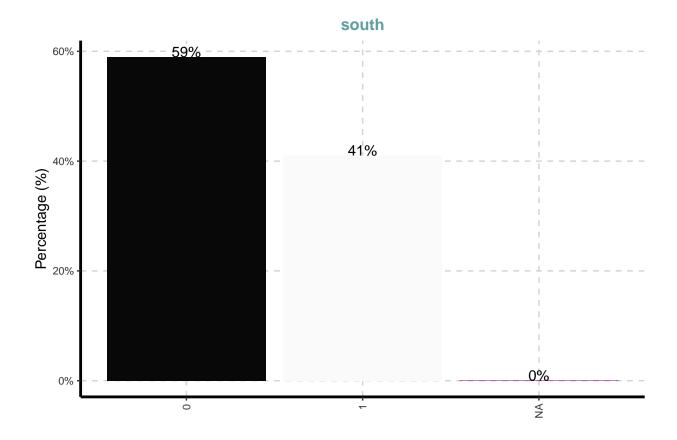
## ## [[5]]



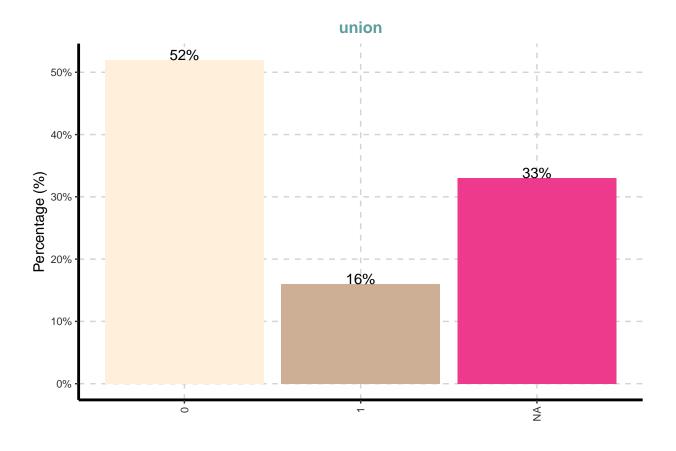
## ## [[6]]



## ## [[7]]

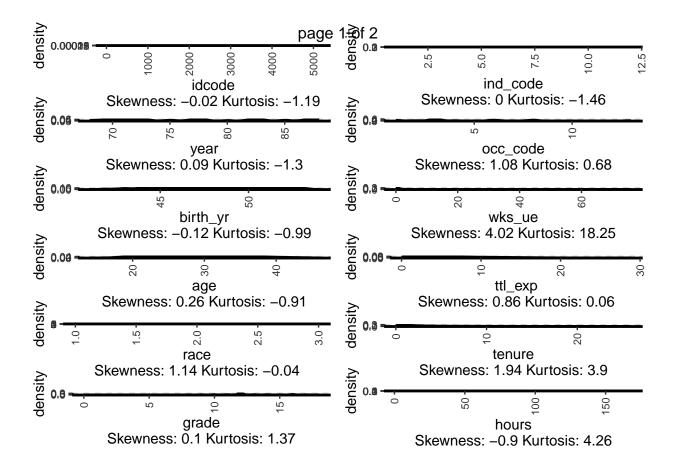


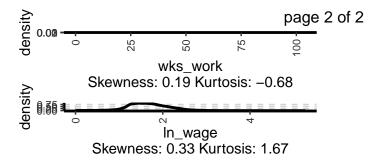
## ## [[8]]



## Warning in matrix(data = seq(1, pn), nrow = nr, ncol = nc): data length [14] is
## not a sub-multiple or multiple of the number of rows [6]

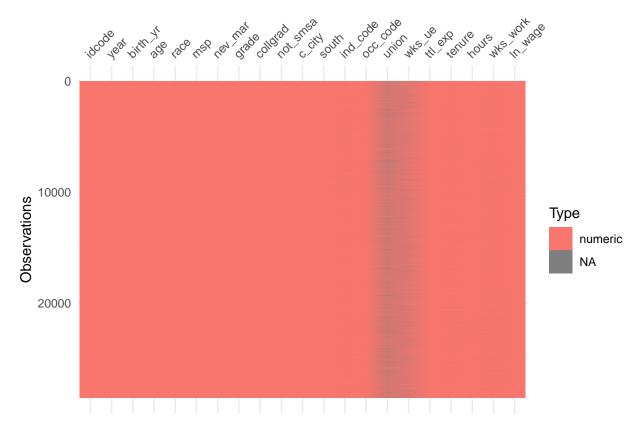
## \$'0'





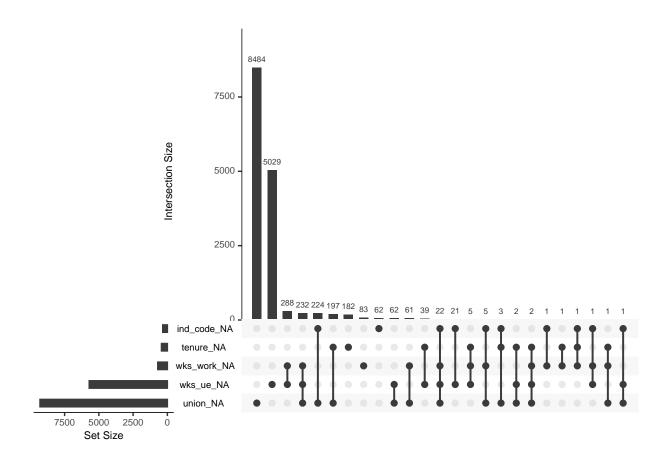
# MISSING VALUES

vis\_dat(nlswork)



# vis\_miss(nlswork) # ALTERNATIVE

gg\_miss\_upset(nlswork)



## Add a dataframe

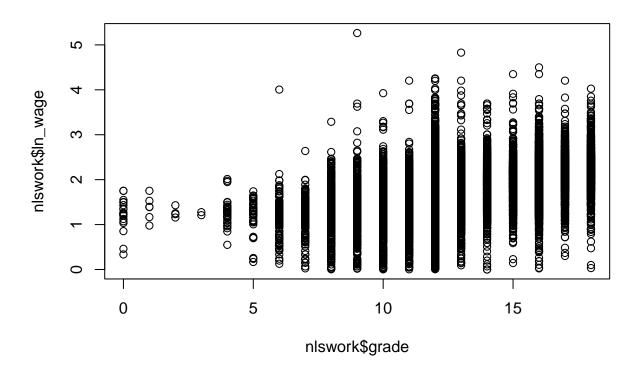
# Export output

```
##
## Summary statistics
## Statistic
                      Mean
                              St. Dev.
                                          Min
                                                Pct1(25) Pct1(75)
                                                 1,327
                                                          3,881
## idcode
             28,534 2,601.284 1,487.359
                                           1
                                                                   5,159
## year
             28,534 77.959
                                6.384
                                           68
                                                   72
                                                            83
                                                                    88
## birth_yr 28,534
                     48.085
                                3.013
                                           41
                                                   46
                                                            51
                                                                    54
             28,510 29.045
                                6.701
                                         14.000 23.000
                                                          34.000
                                                                  46.000
## age
## race
             28,534
                      1.303
                                0.482
                                           1
                                                   1
                                                            2
                                                                     3
## msp
             28,518
                      0.603
                                0.489
                                         0.000
                                                 0.000
                                                          1.000
                                                                   1.000
                      0.230
                                                          0.000
## nev_mar
             28,518
                                0.421
                                         0.000
                                                 0.000
                                                                   1.000
## grade
             28,532 12.533
                                2.324
                                         0.000
                                                 12.000
                                                          14.000 18.000
```

```
## collgrad
             28,534
                       0.168
                                 0.374
                                            0
                                                    0
                                                              0
                                                                       1
                                                                     1.000
## not_smsa
             28,526
                      0.282
                                 0.450
                                          0.000
                                                  0.000
                                                            1.000
             28,526
                      0.357
                                                            1.000
                                                                     1.000
## c_city
                                 0.479
                                          0.000
                                                  0.000
## south
             28,526
                      0.410
                                          0.000
                                                  0.000
                                                            1.000
                                                                     1.000
                                 0.492
## ind_code
             28,193
                      7.693
                                 2.994
                                          1.000
                                                  5.000
                                                            11.000
                                                                    12.000
## occ_code
             28,413
                       4.778
                                 3.065
                                          1.000
                                                  3.000
                                                            6.000
                                                                    13.000
## union
             19,238
                       0.234
                                 0.424
                                          0.000
                                                  0.000
                                                            0.000
                                                                     1.000
             22,830
                                                                    76.000
## wks_ue
                       2.548
                                 7.294
                                          0.000
                                                  0.000
                                                            0.000
## ttl_exp
             28,534
                       6.215
                                 4.652
                                          0.000
                                                  2.462
                                                            9.128
                                                                    28.885
## tenure
             28,101
                                 3.751
                                          0.000
                                                  0.500
                                                            4.167
                                                                    25.917
                       3.124
## hours
             28,467
                      36.560
                                 9.870
                                          1.000
                                                  35.000
                                                            40.000
                                                                    168.000
             27,831
                                29.032
                                          0.000
                                                            72.000
                                                                    104.000
## wks_work
                      53.989
                                                  36.000
             28,534
                                 0.478
                                          0.000
                                                            1.964
                                                                     5.264
  ln_wage
                       1.675
                                                  1.361
```

# Produce a graph

plot(nlswork\$grade,nlswork\$ln\_wage)



# Save the graph

## Tabulations and further statistics

## nlswork\$race n percent ## 20180 0.70722647 ## 2 8051 0.28215462 ## 3 303 0.01061891

## Frequencies

## nlswork\$year

## Label: interview year

## Type: Numeric

4	+	#	
1	t	#	

##						
##		Freq	% Valid	% Valid Cum.	% Total	% Total Cum.
##						
##	88	2272	7.96	7.96	7.96	7.96
##	77	2171	7.61	15.57	7.61	15.57
##	87	2164	7.58	23.15	7.58	23.15
##	75	2141	7.50	30.66	7.50	30.66
##	82	2085	7.31	37.97	7.31	37.97
##	85	2085	7.31	45.27	7.31	45.27
##	83	1987	6.96	52.24	6.96	52.24
##	73	1981	6.94	59.18	6.94	59.18
##	78	1964	6.88	66.06	6.88	66.06
##	71	1851	6.49	72.55	6.49	72.55
##	80	1847	6.47	79.02	6.47	79.02
##	72	1693	5.93	84.95	5.93	84.95
##	70	1686	5.91	90.86	5.91	90.86
##	68	1375	4.82	95.68	4.82	95.68
##	69	1232	4.32	100.00	4.32	100.00
##	<na></na>	0			0.00	100.00
##	Total	28534	100.00	100.00	100.00	100.00

## Frequencies

## nlswork\$race

## Label: 1=white, 2=black, 3=other

## Type: Numeric

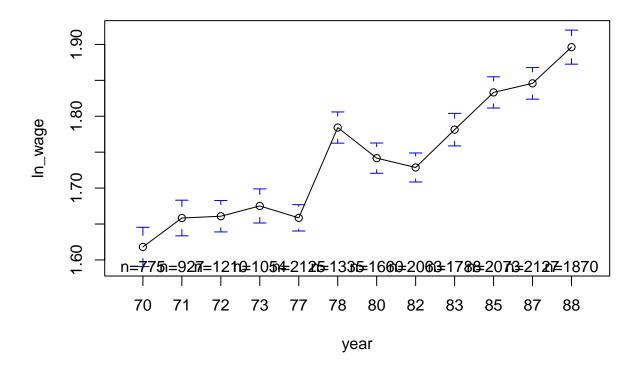
##

##		Freq	% Valid	% Valid Cum.	% Total	% Total Cum.
##						
##	1	20180	70.72	70.72	70.72	70.72
##	2	8051	28.22	98.94	28.22	98.94
##	3	303	1.06	100.00	1.06	100.00
##	<na></na>	0			0.00	100.00
##	Total	28534	100.00	100.00	100.00	100.00

A new dataset: exclude onservations with missing information in a subset of variables

Add variable

Plot variables means



# Regression analysis

- Estimating a Mincerian Wage Equation
- $\bullet \ \ POLS \ estimator \ with \ cluster-robust \ standard \ errors$

# Q1

Pooled OLS model

Export regression output

```
##
                         OLS
                                        panel
##
                                       linear
##
                         OLS
                                       Pooled
##
## Union
                       0.113***
                                      0.113***
##
                       (0.007)
                                       (0.007)
## Collage Graduate
                       0.351***
                                      0.351***
##
                       (0.007)
                                      (0.007)
## Age
                       0.022***
                                      0.022***
##
                      (0.004)
                                       (0.004)
## Age sqrd.
                      -0.0003***
                                     -0.0003***
##
                       (0.0001)
                                      (0.0001)
## Tenure
                       0.055***
                                      0.055***
##
                       (0.002)
                                       (0.002)
                     -0.002***
                                      -0.002***
## Tenure sqrd.
##
                      (0.0001)
                                      (0.0001)
## Not SMSA
                     -0.205***
                                      -0.205***
##
                      (0.007)
                                       (0.007)
## South
                     -0.141***
                                      -0.141***
##
                       (0.006)
                                       (0.006)
## City
                      -0.032***
                                      -0.032***
##
                       (0.007)
                                       (0.007)
## N
                        19,007
                                       19,007
                        0.319
                                        0.319
## Notes:
                   Standard errors in parentheses.
```

• SMSA: Standard Metropolitan Statistical Area

```
# ftable(c_city) # 1 if central city
```

## CLUSTERED Standard-errors

```
pols_robust <- coeftest(pols, function(x) vcovHC(x, type = 'sss'))</pre>
stargazer(pols,pols_robust,title = "Regression analysis",
          model.numbers = FALSE,
          column.labels = c("Pooled", "Pooled (cluster)"),
          label = "regressions",
          table.placement = "!ht",
          notes.append = FALSE,
          notes.align="l",
          notes="Standard errors in parentheses.",
          header = FALSE,
          no.space = TRUE,
          covariate.labels = c("Union", "Collage graduate", "Age", "Age sqrd.",
                                "Tenure", "Tenure sqrd.", "Not SMSA", "South", "City"),
          omit = c("Constant"),
          omit.stat = c("adj.rsq", "f", "ser"),
          digits = 6,
          digits.extra = 7,
```

```
omit.yes.no = c("Constant",""),
dep.var.caption="",
dep.var.labels.include = FALSE,
style = "qje",
type="text")
```

```
##
## Regression analysis
##
                       panel
                                    coefficient
##
                       linear
                                        test
##
                       Pooled
                                  Pooled (cluster)
                     0.112774***
                                    0.112774***
## Union
##
                    (0.006774)
                                    (0.011731)
## Collage graduate 0.350946***
                                    0.350946***
                                     (0.014112)
##
                    (0.007149)
## Age
                    0.022481***
                                    0.022481***
##
                    (0.004249)
                                     (0.005373)
## Age sqrd.
                   -0.000306***
                                    -0.000306***
##
                     (0.000068)
                                     (0.000088)
## Tenure
                     0.054787***
                                    0.054787***
##
                    (0.001944)
                                    (0.002743)
## Tenure sqrd.
                   -0.001540***
                                    -0.001540***
##
                     (0.000125)
                                     (0.000180)
## Not SMSA
                    -0.205457***
                                    -0.205457***
##
                    (0.007120)
                                     (0.013137)
## South
                    -0.140589***
                                    -0.140589***
##
                     (0.005850)
                                     (0.010964)
## City
                    -0.031543***
                                    -0.031543***
##
                     (0.006683)
                                     (0.011691)
## N
                       19,007
## R2
                      0.319459
## Notes:
                   Standard errors in parentheses.
```

## Q2

Random effects estimator (RE)

• SEE THE DISCUSSION HERE for the comparison between R and Stata

https://stats.stackexchange.com/questions/421374/different-results-from-random-effects-plm-r-and-xtreg-stata

• R and Stata treat differently unbalanced panels

for a balanced panel we have

```
nlswork_balanced <- read_dta("data/nlswork_balanced.dta")</pre>
 re_balanced <- plm(data = nlswork_balanced, ln_wage ~ union +
                    collgrad +age +agesq +tenure +tensq +
                    not_smsa +south +c_city, model="random",
                   index=c("idcode", "year"))
     summary(re_balanced)
## Oneway (individual) effect Random Effect Model
##
     (Swamy-Arora's transformation)
##
## Call:
## plm(formula = ln_wage ~ union + collgrad + age + agesq + tenure +
      tensq + not smsa + south + c city, data = nlswork balanced,
##
      model = "random", index = c("idcode", "year"))
##
## Balanced Panel: n = 53, T = 12, N = 636
## Effects:
                   var std.dev share
## idiosyncratic 0.03698 0.19230 0.319
## individual
               0.07902 0.28110 0.681
## theta: 0.8063
##
## Residuals:
       Min.
             1st Qu.
                       Median
                               3rd Qu.
                                           Max.
## -0.904519 -0.104813 0.015673 0.114854 0.658580
##
## Coefficients:
                Estimate Std. Error z-value Pr(>|z|)
##
## (Intercept) 1.05650211 0.20514289 5.1501 2.604e-07 ***
             0.06087668 0.02949229 2.0642 0.0390030 *
## union
## collgrad
             0.20128253  0.17651938  1.1403  0.2541673
             ## age
             ## agesq
## tenure
             0.00332254 0.00616575 0.5389 0.5899766
## tensq
             0.00011290 0.00028483 0.3964 0.6918193
## not_smsa
             ## south
             0.00068168 0.03609511 0.0189 0.9849322
## c_city
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Total Sum of Squares:
## Residual Sum of Squares: 23.689
## R-Squared:
                 0.27447
## Adj. R-Squared: 0.26404
## Chisq: 236.819 on 9 DF, p-value: < 2.22e-16
 re <- plm(data = nlswork_clean, ln_wage ~ union +
            collgrad +age +agesq +tenure +tensq +
            not smsa +south +c city, model="random",
          index=c("idcode", "year"))
```

#### summary(re)

```
## Oneway (individual) effect Random Effect Model
##
      (Swamy-Arora's transformation)
##
## Call:
## plm(formula = ln_wage ~ union + collgrad + age + agesq + tenure +
##
       tensq + not_smsa + south + c_city, data = nlswork_clean,
       model = "random", index = c("idcode", "year"))
##
## Unbalanced Panel: n = 4134, T = 1-12, N = 19007
## Effects:
##
                    var std.dev share
## idiosyncratic 0.06476 0.25448 0.444
## individual
                0.08108 0.28475 0.556
## theta:
     Min. 1st Qu. Median
                             Mean 3rd Qu.
##
  0.3336 0.5920 0.6572 0.6406 0.6987 0.7502
##
## Residuals:
      Min. 1st Qu.
                      Median
                                 Mean 3rd Qu.
## -1.77886 -0.13081 0.00854 0.00428 0.14314 3.03289
## Coefficients:
                 Estimate Std. Error z-value Pr(>|z|)
## (Intercept) 1.1369e+00 5.0729e-02 22.4103 < 2.2e-16 ***
## union
              1.0368e-01 6.4468e-03 16.0819 < 2.2e-16 ***
## collgrad
               3.6931e-01 1.2344e-02 29.9171 < 2.2e-16 ***
## age
               2.3031e-02 3.3174e-03
                                        6.9424 3.856e-12 ***
## agesq
              -2.4910e-04 5.3181e-05 -4.6839 2.814e-06 ***
## tenure
               4.0771e-02 1.5826e-03 25.7618 < 2.2e-16 ***
              -1.2466e-03 1.0022e-04 -12.4393 < 2.2e-16 ***
## tensq
              -1.5114e-01 9.3804e-03 -16.1119 < 2.2e-16 ***
## not smsa
## south
              -1.1157e-01 8.4671e-03 -13.1766 < 2.2e-16 ***
               3.9713e-04 7.4923e-03
                                       0.0530
                                                  0.9577
## c_city
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Total Sum of Squares:
                            1942.3
## Residual Sum of Squares: 1268
## R-Squared:
                  0.34903
## Adj. R-Squared: 0.34872
## Chisq: 4820.91 on 9 DF, p-value: < 2.22e-16
 re_robust <- coeftest(re, function(x) vcovHC(x, type = 'sss'))</pre>
  stargazer(pols,pols_robust,re,re_robust,title = "Regression analysis",
           model.numbers = FALSE,
            column.labels = c("Pooled", "Pooled (cluster)", "RE", "RE (cluster"),
            label = "regressions",
            table.placement = "!ht",
```

```
notes.append = FALSE,
notes.align="1",
notes="Standard errors in parentheses.",
header = FALSE,
no.space = TRUE,
covariate.labels = c("Union", "College Graduate", "Age", "Age sqrd.",
                      "Tenure", "Tenure sqrd.", "Not SMSA", "South", "City"),
omit = c("Constant"),
omit.stat = c("adj.rsq", "f", "ser"),
digits = 3,
digits.extra = 5,
omit.yes.no = c("Constant",""),
dep.var.caption="",
dep.var.labels.include = FALSE,
style = "qje",
type="text")
```

#### ## Regression analysis ## panel panel coefficient coefficient ## linear test linear test ## RE (cluster Pooled Pooled (cluster) RE ## Union 0.113\*\*\* 0.113\*\*\* 0.104\*\*\* 0.104\*\*\* (0.007)(0.012)(0.006)(0.009)## College Graduate 0.351\*\*\* 0.351\*\*\* 0.369\*\*\* 0.369\*\*\* ## (0.007)(0.014)(0.012)(0.013)0.022\*\*\* 0.023\*\*\* ## Age 0.022\*\*\* 0.023\*\*\* ## (0.004)(0.005)(0.003)(0.005)-0.0002\*\*\* -0.0002\*\*\* ## Age sqrd. -0.0003\*\*\* -0.0003\*\*\* ## (0.0001)(0.0001)(0.0001)(0.0001)## Tenure 0.055\*\*\* 0.055\*\*\* 0.041\*\*\* 0.041\*\*\* ## (0.002)(0.003)(0.002)(0.002)-0.001\*\*\* -0.001\*\*\* ## Tenure sqrd. -0.002\*\*\* -0.002\*\*\* ## (0.0001)(0.0002)(0.0001)(0.0001)## Not SMSA -0.205\*\*\* -0.205\*\*\* -0.151\*\*\* -0.151\*\*\* ## (0.007)(0.013)(0.009)(0.012)## South -0.141\*\*\* -0.141\*\*\* -0.112\*\*\* -0.112\*\*\* ## (0.011)(0.006)(0.011)(0.008)-0.032\*\*\* -0.032\*\*\* 0.0004 0.0004 ## City (0.010)## (0.007)(0.012)(0.007)## N 19,007 19,007 ## R2 0.349 0.319 ## Notes: Standard errors in parentheses.

##

## Regression analysis

##

##					
##		panel	coefficient	panel	coefficient
##		linear	test	linear	test
##		Pooled	Pooled (cluster)	RE	RE (cluster
##					
##	Union	0.113***	0.113***	0.104***	0.104***
##		(0.007)	(0.012)	(0.006)	(0.009)
##	College Graduate	0.351***	0.351***	0.369***	0.369***
##		(0.007)	(0.014)	(0.012)	(0.013)
##	Age	0.022***	0.022***	0.023***	0.023***
##		(0.004)	(0.005)	(0.003)	(0.005)
##	Age sqrd.	-0.0003***	-0.0003***	-0.0002***	-0.0002***
##		(0.0001)	(0.0001)	(0.0001)	(0.0001)
##	Tenure	0.055***	0.055***	0.041***	0.041***
##		(0.002)	(0.003)	(0.002)	(0.002)
##	Tenure sqrd.	-0.002***	-0.002***	-0.001***	-0.001***
##		(0.0001)	(0.0002)	(0.0001)	(0.0001)
##	Not SMSA	-0.205***	-0.205***	-0.151***	-0.151***
##		(0.007)	(0.013)	(0.009)	(0.012)
##	South	-0.141***	-0.141***	-0.112***	-0.112***
##		(0.006)	(0.011)	(0.008)	(0.011)
##	City	-0.032***	-0.032***	0.0004	0.0004
##		(0.007)	(0.012)	(0.007)	(0.010)
##	N	19,007		19,007	
##	R2	0.319		0.349	
##					
##	Notes:	Standard en	rrors in parenthe	ses.	

# LM test for the presence of unobserved effects

```
plmtest(pols, type=c("bp"))
```

##

Table 1: LM test for the presence of unobserved effects

statistic	p.value	parameter	method	alternative
14041.19	0	1	Lagrange Multiplier Test - (Breusch-Pagan) for unbalanced panels	significant effects

## Fixed effects estimator (FE)

```
## Oneway (individual) effect Within Model
##
## Call:
## plm(formula = ln_wage ~ union + collgrad + age + agesq + tenure +
##
      tensq + not smsa + south + c city, data = nlswork clean,
      model = "within", index = c("idcode", "year"))
##
## Unbalanced Panel: n = 4134, T = 1-12, N = 19007
##
## Residuals:
      Min. 1st Qu.
                    Median 3rd Qu.
                                         Max.
## -1.88027 -0.10216 0.00000 0.10774 2.80710
##
## Coefficients:
              Estimate Std. Error t-value Pr(>|t|)
##
## union
           9.3877e-02 6.9662e-03 13.4761 < 2.2e-16 ***
           2.4259e-02 3.4467e-03
                                   7.0383 2.031e-12 ***
## age
## agesq -2.2618e-04 5.5316e-05 -4.0890 4.356e-05 ***
          3.2966e-02 1.6465e-03 20.0218 < 2.2e-16 ***
## tenure
           -1.1002e-03 1.0291e-04 -10.6916 < 2.2e-16 ***
## tensq
## not_smsa -9.3105e-02 1.2970e-02 -7.1787 7.372e-13 ***
## south -6.3222e-02 1.3279e-02 -4.7611 1.944e-06 ***
## c city 1.1409e-02 8.8964e-03 1.2824
                                            0.1997
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Total Sum of Squares:
                            1119.5
## Residual Sum of Squares: 962.69
## R-Squared:
                   0.14005
## Adj. R-Squared: -0.099505
## F-statistic: 302.62 on 8 and 14865 DF, p-value: < 2.22e-16
  stargazer(pols,re,fe,title = "Regression analysis",
            model.numbers = FALSE,
            column.labels = c("Pooled", "RE", "FE"),
            label = "regressions",
            table.placement = "!ht",
            notes.append = FALSE,
            notes.align="l",
            notes="Standard errors in parentheses.",
            header = FALSE,
            no.space = TRUE,
            covariate.labels = c("Union", "College", "Age", "Age sqrd.", "Tenure",
                                  "Tenure sqrd.", "Not SMSA", "South", "City"),
            omit = c("Constant"),
            omit.stat = c("adj.rsq", "f", "ser"),
            digits = 6,
            digits.extra = 7,
            omit.yes.no = c("Constant",""),
            dep.var.caption="",
            dep.var.labels.include = FALSE,
            style = "qje",
            type="text")
##
```

```
##
                   Pooled
                                  RE
                                                FΕ
## Union
                0.112774*** 0.103677*** 0.093877***
##
                                            (0.006966)
                 (0.006774)
                              (0.006447)
## College
                0.350946*** 0.369309***
##
                 (0.007149)
                              (0.012344)
## Age
                0.022481*** 0.023031*** 0.024259***
##
                 (0.004249)
                              (0.003317)
                                           (0.003447)
                -0.000306*** -0.000249*** -0.000226***
## Age sqrd.
##
                 (0.000068)
                              (0.000053)
                                            (0.000055)
## Tenure
                0.054787***
                             0.040771*** 0.032966***
##
                 (0.001944)
                              (0.001583)
                                            (0.001646)
## Tenure sqrd. -0.001540*** -0.001247*** -0.001100***
##
                 (0.000125)
                              (0.000100)
                                            (0.000103)
## Not SMSA
                -0.205457*** -0.151136*** -0.093105***
                 (0.007120)
                              (0.009380)
                                            (0.012970)
##
                -0.140589*** -0.111567*** -0.063222***
## South
##
                 (0.005850)
                               (0.008467)
                                            (0.013279)
```

0.000397

(0.007492)

19,007

-0.031543\*\*\*

(0.006683)

19,007

## Regression analysis

## City

## N

0.011409 (0.008896)

19,007

```
0.319459
                             0.349029
                                         0.140054
Standard errors in parentheses.
# Testing for fixed effects, null: OLS better than fixed
# 'F test for individual effects' <<==>> 'F test that all u_i=0'
 ols_0 <- lm(data = nlswork_clean, ln_wage ~ union +</pre>
               age +agesq +tenure +tensq +
               not_smsa +south +c_city)
     summary(ols 0)
##
## Call:
## lm(formula = ln_wage ~ union + age + agesq + tenure + tensq +
      not_smsa + south + c_city, data = nlswork_clean)
##
## Residuals:
##
      Min
               1Q Median
                              30
                                     Max
## -1.7497 -0.2508 -0.0182 0.2379 3.4100
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.008e+00 6.821e-02 14.776 < 2e-16 ***
             1.294e-01 7.181e-03 18.026 < 2e-16 ***
## union
## age
              3.929e-02 4.495e-03 8.740 < 2e-16 ***
              -5.387e-04 7.175e-05 -7.509 6.24e-14 ***
## agesq
              5.806e-02 2.062e-03 28.158 < 2e-16 ***
## tenure
             -1.699e-03 1.331e-04 -12.765 < 2e-16 ***
## tensq
## not_smsa
             -2.311e-01 7.538e-03 -30.657 < 2e-16 ***
             -1.475e-01 6.208e-03 -23.762 < 2e-16 ***
## south
              -3.451e-02 7.094e-03 -4.864 1.16e-06 ***
## c_city
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4091 on 18998 degrees of freedom
## Multiple R-squared: 0.2331, Adjusted R-squared: 0.2328
## F-statistic: 721.9 on 8 and 18998 DF, p-value: < 2.2e-16
pFtest(fe, ols 0)
##
## F test for individual effects
##
## data: ln_wage ~ union + collgrad + age + agesq + tenure + tensq + not_smsa + ...
## F = 8.2833, df1 = 4133, df2 = 14865, p-value < 2.2e-16
## alternative hypothesis: significant effects
# generate fixed-effects
# nlswork_clean$specific_effects <- fixef(fe)</pre>
```

```
# *Q3.1*
 fe robust <- coeftest(fe, function(x) vcovHC(x, type = 'sss'))</pre>
 stargazer(ols_0,fe,fe_robust,title = "Regression analysis",
            model.numbers = FALSE,
            column.labels = c("OLS", "FE", "FE (cluster)"),
            label = "regressions",
            table.placement = "!ht",
            notes.append = FALSE,
            notes.align="l",
            notes="Standard errors in parentheses.",
            header = FALSE,
            no.space = TRUE,
            covariate.labels = c("Union", "Age", "Age sqrd.", "Tenure",
                                  "Tenure sqrd.", "Not SMSA", "South", "City"),
            omit = c("Constant"),
            omit.stat = c("adj.rsq", "f", "ser"),
            digits = 6,
            digits.extra = 7,
            omit.yes.no = c("Constant",""),
            dep.var.caption="",
            dep.var.labels.include = FALSE,
            style = "qje",
            type="text")
```

```
##
## Regression analysis
##
                 OLS
                            panel
                                     coefficient
##
                            linear
                                         test
##
                 OLS
                                     FE (cluster)
             0.129446*** 0.093877*** 0.093877***
## Union
##
              (0.007181)
                          (0.006966)
                                     (0.009565)
## Age
              0.039289*** 0.024259*** 0.024259***
##
              (0.004495)
                          (0.003447)
                                      (0.005008)
              -0.000539*** -0.000226*** -0.000226***
## Age sqrd.
##
              (0.000072)
                          (0.000055)
                                     (0.000081)
## Tenure
              0.058063*** 0.032966*** 0.032966***
##
               (0.002062)
                          (0.001646)
                                      (0.002085)
## Tenure sqrd. -0.001699*** -0.001100*** -0.001100***
##
               (0.000133)
                          (0.000103)
                                      (0.000126)
## Not SMSA
              -0.231095*** -0.093105*** -0.093105***
##
              (0.007538)
                          (0.012970)
                                      (0.019790)
## South
              -0.147518*** -0.063222*** -0.063222***
##
              (0.006208)
                          (0.013279)
                                     (0.021653)
## City
             -0.034506***
                          0.011409
                                       0.011409
##
               (0.007094)
                          (0.008896)
                                      (0.012605)
## N
                19,007
                            19,007
                0.233124
                           0.140054
## Notes:
              Standard errors in parentheses.
```

```
# *Q3.2*
 linearHypothesis(ols,c("age=0","agesq=0"))
## Linear hypothesis test
## Hypothesis:
## age = 0
## agesq = 0
##
## Model 1: restricted model
## Model 2: ln_wage ~ union + collgrad + age + agesq + tenure + tensq + not_smsa +
       south + c_city
##
##
##
    Res.Df
              RSS Df Sum of Sq
                                         Pr(>F)
## 1 18999 2832.2
## 2 18997 2821.8 2
                      10.418 35.066 6.294e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
linearHypothesis(ols,c("age=0", "agesq=0"), white.adjust = "hc1")
## Linear hypothesis test
## Hypothesis:
## age = 0
## agesq = 0
## Model 1: restricted model
## Model 2: ln_wage ~ union + collgrad + age + agesq + tenure + tensq + not_smsa +
##
       south + c_city
## Note: Coefficient covariance matrix supplied.
##
    Res.Df Df
                   F
                        Pr(>F)
## 1 18999
## 2 18997 2 40.554 < 2.2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
  Wald_test(fe, vcov = "CR1", cluster = nlswork_clean$idcode,
             constraints = constrain_zero(c("age", "agesq")), test = "Naive-F")
       test Fstat df_num df_denom p_val sig
## Naive-F 80.4
                            4133 <0.001 ***
                      2
```

## LSDV estimator

```
# *LSDV Estimator=FE estimator* <<==>> takes too long
# *using a smaller sample*
nlswork balanced <- read dta("data/nlswork balanced small.dta")
  LSDV <- lm(data = nlswork_balanced, ln_wage ~ union +
              age +agesq +tenure +tensq +
              not_smsa +south +c_city + factor(idcode))
  summary(LSDV)
##
## Call:
## lm(formula = ln_wage ~ union + age + agesq + tenure + tensq +
##
       not_smsa + south + c_city + factor(idcode), data = nlswork_balanced)
##
## Residuals:
                   10
                         Median
                                       30
## -0.254362 -0.069457 0.004535 0.078344 0.239917
## Coefficients: (2 not defined because of singularities)
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     0.5332323 0.4915522 1.085
                                                   0.2833
## union
                     0.0895838 0.0548743
                                           1.633
                                                   0.1090
## age
                     0.0758967 0.0334355
                                           2.270
                                                   0.0276 *
## agesq
                    -0.0011959 0.0005405 -2.212
                                                   0.0316 *
## tenure
                     0.0125105
                                0.0162130 0.772
                                                    0.4440
                    0.0006329
                                0.0007176
                                                   0.3821
## tensq
                                           0.882
## not smsa
                                       NA
                                               NA
                                                        NA
                            NA
## south
                                       NA
                                               NA
                                                        NA
                            NA
## c_city
                     0.1164782 0.0875330
                                           1.331
                                                   0.1895
                                                   0.0140 *
## factor(idcode)20 0.3287869 0.1289784
                                           2.549
## factor(idcode)126 -0.0167263 0.0546551 -0.306
                                                   0.7609
## factor(idcode)128  0.0375653  0.0882907
                                           0.425
                                                    0.6724
## factor(idcode)379 -0.1504303 0.1188913 -1.265
                                                    0.2118
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.1149 on 49 degrees of freedom
## Multiple R-squared: 0.8021, Adjusted R-squared: 0.7617
## F-statistic: 19.86 on 10 and 49 DF, p-value: 5.49e-14
 fe_LSDV <- plm(data = nlswork_balanced, ln_wage ~ union +</pre>
              age +agesq +tenure +tensq +
              not_smsa +south +c_city, model="within", index=c("idcode", "year"))
  summary(fe_LSDV)
## Oneway (individual) effect Within Model
##
## Call:
## plm(formula = ln_wage ~ union + age + agesq + tenure + tensq +
      not_smsa + south + c_city, data = nlswork_balanced, model = "within",
      index = c("idcode", "year"))
##
```

```
##
## Balanced Panel: n = 5, T = 12, N = 60
## Residuals:
        Min.
              1st Qu.
                          Median
                                    3rd Qu.
## -0.2543619 -0.0694565 0.0045351 0.0783435 0.2399171
## Coefficients:
          Estimate Std. Error t-value Pr(>|t|)
## union 0.08958377 0.05487432 1.6325 0.10898
      0.07589667 0.03343547 2.2699 0.02765 *
## agesq -0.00119586 0.00054052 -2.2124 0.03163 *
## tenure 0.01251051 0.01621304 0.7716 0.44404
## tensq 0.00063295 0.00071759 0.8821 0.38206
## c_city 0.11647818 0.08753305 1.3307 0.18945
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Total Sum of Squares:
                          2.3839
## Residual Sum of Squares: 0.64685
## R-Squared:
              0.72866
## Adj. R-Squared: 0.67329
## F-statistic: 21.9312 on 6 and 49 DF, p-value: 2.4403e-12
 stargazer(LSDV,fe_LSDV,title = "Regression analysis",
           model.numbers = FALSE,
           column.labels = c("LSDV", "FE"),
           label = "regressions",
           table.placement = "!ht",
           notes.append = FALSE,
           notes.align="l",
           notes="Standard errors in parentheses.",
           header = FALSE,
           no.space = TRUE,
           covariate.labels = c("Union", "Age", "Age sqrd.", "Tenure",
                              "Tenure sqrd.", "Not SMSA", "South", "City"),
           omit = c("Constant"),
           omit.stat = c("adj.rsq", "f", "ser"),
           digits = 6,
           digits.extra = 7,
           omit.yes.no = c("Constant",""),
           dep.var.caption="",
           dep.var.labels.include = FALSE,
           style = "qje",
           type="text")
##
## Regression analysis
panel
##
                         OLS
##
                                       linear
##
                         LSDV
                                       FE
## Union
                      0.089584
                                     0.089584
```

```
##
                       (0.054874)
                                      (0.054874)
## Age
                       0.075897**
                                      0.075897**
##
                       (0.033435)
                                      (0.033435)
                      -0.001196**
                                      -0.001196**
## Age sqrd.
##
                       (0.000541)
                                      (0.000541)
                                      0.012511
## Tenure
                       0.012511
                       (0.016213)
                                      (0.016213)
##
## Tenure sqrd.
                       0.000633
                                      0.000633
##
                       (0.000718)
                                      (0.000718)
## Not SMSA
##
## South
##
## City
                                       0.116478
                       0.116478
                       (0.087533)
                                      (0.087533)
##
## factor(idcode)20
                       0.328787**
##
                       (0.128978)
## factor(idcode)126
                       -0.016726
                       (0.054655)
##
## factor(idcode)128
                       0.037565
##
                       (0.088291)
## factor(idcode)379
                       -0.150430
##
                       (0.118891)
## N
                                          60
                          60
                                       0.728663
## R2
                       0.802119
## Notes:
                    Standard errors in parentheses.
```

#### Hausman test

```
##
## Hausman Test
##
## data: ln_wage ~ union + age + agesq + tenure + tensq + not_smsa + south + ...
## chisq = 607.1, df = 8, p-value < 2.2e-16
## alternative hypothesis: one model is inconsistent</pre>
```

#### **BE** estimator

```
//Final slide 46
# *Q5*
 be <- plm(data = nlswork_clean, ln_wage ~ union +
            collgrad +age +agesq +tenure +tensq +
            not_smsa +south +c_city, model="between",
          index=c("idcode", "year"))
     summary(be)
## Oneway (individual) effect Between Model
##
## Call:
## plm(formula = ln_wage ~ union + collgrad + age + agesq + tenure +
      tensq + not smsa + south + c city, data = nlswork clean,
      model = "between", index = c("idcode", "year"))
##
## Unbalanced Panel: n = 4134, T = 1-12, N = 19007
## Observations used in estimation: 4134
##
## Residuals:
       Min.
               1st Qu.
                         Median
                                  3rd Qu.
                                               Max.
## -1.5946586 -0.2004452 -0.0067495 0.1909616 1.8487578
## Coefficients:
                Estimate Std. Error t-value Pr(>|t|)
## (Intercept) 1.19446539 0.15356828
                                   7.7781 9.240e-15 ***
## union
             0.11135322 0.01636297
                                   6.8052 1.154e-11 ***
             0.34850931 0.01308193 26.6405 < 2.2e-16 ***
## collgrad
## age
             0.02113165 0.01022918
                                   2.0658
                                            0.03891 *
             -0.00034316  0.00016368  -2.0965
                                            0.03610 *
## agesq
             0.09570307 0.00539210 17.7488 < 2.2e-16 ***
## tenure
            ## tensq
            ## not smsa
## south
            ## c_city
             -0.02215011 0.01385878 -1.5983 0.11006
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Total Sum of Squares:
                         773.5
## Residual Sum of Squares: 464.95
## R-Squared:
                0.3989
## Adj. R-Squared: 0.39759
```

## F-statistic: 304.083 on 9 and 4124 DF, p-value: < 2.22e-16

#### FD estimator

```
# //Final slide 53
# *Q6*
 fd <- plm(data = nlswork_clean, ln_wage ~ 0 + union +
             collgrad +age +agesq +tenure +tensq +
             not_smsa +south +c_city, model="fd",
           index=c("idcode", "year"))
   summary(fd)
## Oneway (individual) effect First-Difference Model
##
## Call:
## plm(formula = ln_wage ~ 0 + union + collgrad + age + agesq +
      tenure + tensq + not_smsa + south + c_city, data = nlswork_clean,
      model = "fd", index = c("idcode", "year"))
##
##
## Unbalanced Panel: n = 4134, T = 1-12, N = 19007
## Observations used in estimation: 14873
##
## Residuals:
     Min. 1st Qu. Median
                             Mean 3rd Qu.
## -2.9266 -0.0925 0.0073 0.0156 0.1279 3.3217
## Coefficients:
              Estimate Std. Error t-value Pr(>|t|)
           6.9160e-02 6.6336e-03 10.4257 < 2.2e-16 ***
## union
           2.2744e-02 5.5436e-03 4.1027 4.104e-05 ***
## age
           -2.5853e-04 9.0084e-05 -2.8698 0.004113 **
## agesq
## tenure
          3.2078e-02 2.1241e-03 15.1024 < 2.2e-16 ***
           -1.2023e-03 1.7526e-04 -6.8600 7.160e-12 ***
## tensq
## not_smsa -7.7277e-02 1.4369e-02 -5.3780 7.645e-08 ***
## south
         -4.6889e-02 1.5675e-02 -2.9913 0.002782 **
           2.2987e-02 9.9149e-03 2.3185 0.020437 *
## c_city
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Total Sum of Squares:
                           1441.5
## Residual Sum of Squares: 1404.4
```

# Output Table

## R-Squared:

## Adj. R-Squared: 0.028332

0.02879

## F-statistic: 85.5285 on 8 and 14865 DF, p-value: < 2.22e-16

```
notes.align="1",
notes="Standard errors in parentheses.",
header = FALSE,
no.space = TRUE,
omit = c("Constant"),
omit.stat = c("adj.rsq","f","ser"),
digits = 6,
digits.extra = 7,
omit.yes.no = c("Constant",""),
dep.var.caption="",
dep.var.labels.include = FALSE,
style = "qje",
type="text")
```

```
##
## Regression analysis
##
               OLS
                             RE
                                         FΕ
                                                      BE
## union
           0.112774*** 0.103677*** 0.093877*** 0.111353***
##
            (0.006774)
                         (0.006447)
                                      (0.006966)
                                                  (0.016363)
## collgrad 0.350946*** 0.369309***
                                                 0.348509***
##
            (0.007149)
                        (0.012344)
                                                  (0.013082)
## age
           0.022481***
                        0.023031*** 0.024259***
                                                  0.021132**
##
            (0.004249)
                       (0.003317)
                                     (0.003447)
                                                  (0.010229)
## agesq
           -0.000306*** -0.000249*** -0.000226*** -0.000343**
##
            (0.000068)
                         (0.000053)
                                     (0.000055)
                                                  (0.000164)
## tenure
           0.054787*** 0.040771*** 0.032966*** 0.095703***
##
            (0.001944)
                         (0.001583)
                                     (0.001646)
                                                  (0.005392)
## tensq
           -0.001540*** -0.001247*** -0.001100*** -0.003440***
##
            (0.000125)
                         (0.000100)
                                      (0.000103)
                                                  (0.000364)
## not_smsa -0.205457*** -0.151136*** -0.093105*** -0.205362***
##
            (0.007120)
                         (0.009380)
                                     (0.012970)
                                                  (0.014408)
## south
           -0.140589*** -0.111567*** -0.063222*** -0.130589***
            (0.005850)
                         (0.008467)
                                     (0.013279)
                                                  (0.011458)
## c_city
           -0.031543***
                         0.000397
                                      0.011409
                                                  -0.022150
##
            (0.006683)
                         (0.007492)
                                      (0.008896)
                                                  (0.013859)
## N
              19,007
                           19,007
                                       19,007
                                                    4,134
## R2
             0.319459
                          0.349029
                                      0.140054
                                                   0.398899
## Notes:
           Standard errors in parentheses.
```

## FURTHER SPECIFICATION TESTS FOR PANEL DATA

Test for heteroskedasticity within panel data

```
# HO) The null hypothesis for the Breusch-Pagan test is homoskedasticity
# takes too long to compute
# bptest(data = nlswork_clean, ln_wage ~ union +
```

```
##
## Breusch-Pagan test
##
## data: ln_wage ~ union + collgrad + age + agesq + tenure + tensq + not_smsa + south + c_city + f
## BP = 5.2368, df = 10, p-value = 0.8748
```

## Test of serial correlation within panel data

• Unobserved effects test «» Wooldridge's test for unobserved individual effects «»

# Locally robust tests for serial correlation or random effects

• Baltagi and Li AR-RE joint test - balanced panel

```
##
## Baltagi and Li AR-RE joint test - balanced panel
##
## data: formula
## chisq = 50.736, df = 2, p-value = 9.612e-12
## alternative hypothesis: AR(1) errors or random effects
```

#### General serial correlation tests

• Breusch-Godfrey/Wooldridge test for serial correlation in panel models «»

```
##
## Breusch-Godfrey/Wooldridge test for serial correlation in panel models
##
## data: ln_wage ~ union + collgrad + age + agesq + tenure + tensq + not_smsa + south + c_city
## chisq = 181.23, df = 2, p-value < 2.2e-16
## alternative hypothesis: serial correlation in idiosyncratic errors</pre>
```

# Wooldridge's test for serial correlation in FE panels

```
pwartest(data = nlswork_balanced, ln_wage ~ union +
            collgrad +age +agesq +tenure +tensq +
            not_smsa +south +c_city)
##
   Wooldridge's test for serial correlation in FE panels
##
## data: plm.model
## F = 12.205, df1 = 1, df2 = 53, p-value = 0.0009707
## alternative hypothesis: serial correlation
Wooldridge first-difference-based test
  pwfdtest(data = nlswork_balanced, ln_wage ~ union +
            collgrad +age +agesq +tenure +tensq +
            not_smsa +south +c_city)
##
##
   Wooldridge's first-difference test for serial correlation in panels
## data: plm.model
## F = 8.5778, df1 = 1, df2 = 48, p-value = 0.005192
## alternative hypothesis: serial correlation in differenced errors
  pwfdtest(data = nlswork_balanced, ln_wage ~ union +
            collgrad +age +agesq +tenure +tensq +
            not_smsa +south +c_city, h0="fe")
##
## Wooldridge's first-difference test for serial correlation in panels
##
## data: plm.model
## F = 2.9964, df1 = 1, df2 = 48, p-value = 0.08988
## alternative hypothesis: serial correlation in original errors
Tests for cross-sectional dependence
  pcdtest(data = nlswork_balanced, ln_wage ~ union +
            collgrad +age +agesq +tenure +tensq +
           not_smsa +south +c_city)
## Pesaran CD test for cross-sectional dependence in panels
## data: ln_wage ~ union + collgrad + age + agesq + tenure + tensq + not_smsa +
                                                                                     south + c_city
```

## z = 1.8975, p-value = 0.05776

## alternative hypothesis: cross-sectional dependence

# HIGH DIMENSIONAL FIXED-EFFECTS

```
## CHECK: 'lfe' and 'fixest'
### https://github.com/sgaure/lfe
### https://github.com/lrberge/fixest
# *including 1 fixed effect*
 HDFE1a <- feols(data = nlswork_clean, ln_wage ~ union +
                age +agesq +tenure +tensq +
                not_smsa +south +c_city | idcode)
     summary(HDFE1a)
## OLS estimation, Dep. Var.: ln_wage
## Observations: 19,007
## Fixed-effects: idcode: 4,134
## Standard-errors: Clustered (idcode)
         Estimate Std. Error t value Pr(>|t|)
## union
         ## age
         ## agesq -0.000226 0.000081 -2.778400 0.005488 **
          ## tenure
         ## tensq
## south -0.063222 0.021654 -2.919600 0.003524 **
## c_city 0.011409 0.012606 0.905058 0.365487
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## RMSE: 0.225053
                  Adj. R2: 0.703151
                Within R2: 0.140054
 HDFE1b <- felm(data = nlswork_clean, ln_wage ~ union +</pre>
               age +agesq +tenure +tensq +
                not_smsa +south +c_city | idcode, clustervar=c("idcode"))
## Warning: Argument(s) clustervar are deprecated and will be removed, use
## multipart formula instead
     summary(HDFE1b)
##
## Call:
##
     felm(formula = ln_wage ~ union + age + agesq + tenure + tensq + not_smsa + south + c_city |
##
## Residuals:
##
     Min
             1Q Median
                          3Q
                                Max
## -1.8803 -0.1022 0.0000 0.1077 2.8071
##
## Coefficients:
##
           Estimate Cluster s.e. t value Pr(>|t|)
```

```
## union
          9.388e-02
                      9.565e-03 9.814 < 2e-16 ***
## age
          2.426e-02 5.008e-03 4.844 1.32e-06 ***
## agesq
          -2.262e-04 8.141e-05 -2.778 0.00549 **
          3.297e-02
                      2.086e-03 15.807 < 2e-16 ***
## tenure
## tensq
          -1.100e-03 1.262e-04 -8.719 < 2e-16 ***
## south -6.322e-02 2.165e-02 -2.920 0.00352 **
         1.141e-02 1.261e-02 0.905 0.36549
## c_city
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.2545 on 14865 degrees of freedom
## Multiple R-squared(full model): 0.7678
                                     Adjusted R-squared: 0.7032
## Multiple R-squared(proj model): 0.1401
                                      Adjusted R-squared: -0.0995
## F-statistic(full model, *iid*):11.87 on 4141 and 14865 DF, p-value: < 2.2e-16
## F-statistic(proj model): 168 on 8 and 4133 DF, p-value: < 2.2e-16
# *including a 2nd fixed effect*
 HDFE2a <- feols(data = nlswork_clean, ln_wage ~ union +
                 age +agesq +tenure +tensq +
                 not_smsa +south +c_city | idcode + year)
     summary(HDFE2a)
## OLS estimation, Dep. Var.: ln_wage
## Observations: 19,007
## Fixed-effects: idcode: 4,134, year: 12
## Standard-errors: Clustered (idcode)
          Estimate Std. Error t value Pr(>|t|)
          ## union
          0.073440 0.013588 5.404700 6.86e-08 ***
## age
## agesq -0.000720 0.000116 -6.218800 5.51e-10 ***
## tenure 0.032423 0.002104 15.408000 < 2.2e-16 ***
          -0.001090 0.000129 -8.443500 < 2.2e-16 ***
## tensq
## south -0.064281 0.021622 -2.972900 0.002967 **
## c_city
          ## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## RMSE: 0.223942
                   Adj. R2: 0.705857
##
                 Within R2: 0.066421
 HDFE2b <- felm(data = nlswork_clean, ln_wage ~ union +</pre>
                age +agesq +tenure +tensq +
                not_smsa +south +c_city | idcode + year, clustervar=c("idcode"))
## Warning: Argument(s) clustervar are deprecated and will be removed, use
## multipart formula instead
     summary(HDFE2b)
```

```
##
## Call:
##
     felm(formula = ln_wage ~ union + age + agesq + tenure + tensq +
                                                                         not_smsa + south + c_city |
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -1.90155 -0.09933 0.00000 0.10738
##
## Coefficients:
##
             Estimate Cluster s.e. t value Pr(>|t|)
## union
            0.0956999
                         0.0095207 10.052 < 2e-16 ***
                         0.0135842
                                    5.406 6.80e-08 ***
## age
            0.0734400
           -0.0007205
                         0.0001158 -6.221 5.44e-10 ***
## agesq
## tenure
            0.0324225
                         0.0021036 15.413 < 2e-16 ***
                         0.0001291 -8.446 < 2e-16 ***
## tensq
           -0.0010902
## not_smsa -0.0905368
                         0.0196138
                                   -4.616 4.03e-06 ***
                         0.0216158 -2.974 0.00296 **
           -0.0642811
## south
## c_city
            0.0104319
                         0.0126641
                                   0.824 0.41014
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2533 on 14854 degrees of freedom
## Multiple R-squared(full model): 0.7701
                                           Adjusted R-squared: 0.7059
## Multiple R-squared(proj model): 0.06642 Adjusted R-squared: -0.1945
## F-statistic(full model, *iid*):11.98 on 4152 and 14854 DF, p-value: < 2.2e-16
## F-statistic(proj model): 62.59 on 8 and 4133 DF, p-value: < 2.2e-16
```

# Exercise with simulated data

See the Stata file 'stata\_do\_example.do' that produces the data in folder tmp\_files.

```
simulated <- read_dta("data/data_simulation.dta")

# names(nlswork)
# head(nlswork)
# str(nlswork)</pre>
```

# **EDA: Exploratory Data Analysis**

```
# eda_report(simulated,output_dir = "EDA/",output_file = "eda_simulated.pdf")
ExpData(simulated,type=1)
```

```
##
                                               Descriptions
                                                                   Value
## 1
                                         Sample size (nrow)
                                                                    4950
## 2
                                   No. of variables (ncol)
                                                                      22
## 3
                         No. of numeric/interger variables
                                                                      22
## 4
                                   No. of factor variables
                                                                       0
## 5
                                     No. of text variables
                                                                       0
                                  No. of logical variables
                                                                       0
## 6
```

```
## 7
                              No. of identifier variables
## 8
                                    No. of date variables
                                                                     0
## 9
                 No. of zero variance variables (uniform)
                                                                     0
## 10
                    \%. of variables having complete cases 95.45% (21)
        \%. of variables having >0% and <50% missing cases
                                                             4.55% (1)
## 12 %. of variables having >=50% and <90% missing cases
                                                                0% (0)
               \%. of variables having >=90% missing cases
                                                                0% (0)
```

# ExpData(simulated, type=2)

##		Index	Variable_Name	Variable_Type	Sample_n	Missing_Count	Per_of_Missing
##	1	1	workerid	numeric	4950	0	0.0
##	2	2	year	numeric	4950	0	0.0
##	3	3	ui	numeric	4950	0	0.0
##	4	4	quarter	numeric	4950	0	0.0
##		5	q1	numeric	4950	0	0.0
##		6	wage	numeric	4950	0	0.0
	7	7	educ	numeric	4950	0	0.0
##		8	exper	numeric	4950	0	0.0
##		9	union	numeric	4950	0	0.0
##		10	exper2	numeric	4950	0	0.0
	11	11	lnwage	numeric	4950	0	0.0
	12	12	yy1	numeric	4950	0	0.0
	13	13	yy2	numeric	4950	0	0.0
	14	14	ууЗ	numeric	4950	0	0.0
##		15	yy4	numeric	4950	0	0.0
	16	16	уу5	numeric	4950	0	0.0
	17	17	уу6	numeric	4950	0	0.0
	18	18	уу7	numeric	4950	0	0.0
	19	19	уу8	numeric	4950	0	0.0
##		20	уу9	numeric	4950	0	0.0
	21	21	уу10	numeric	4950	0	0.0
## ##	22	22 No. of	lag_lnwage	numeric	4455	495	0.1
##	1	NO_OI_	distinct_value_ 49				
	2			0			
	3		49				
	4			4			
	5			2			
	6		495				
	7		246				
##				9			
##				2			
##				9			
##			495				
	12			2			
##				2			
	14			2			
##				2			
##	16			2			
##	17			2			
##	18			2			
##	19			2			
##	20			2			

```
## 21 2
## 22 4454
```

#### summary(simulated)

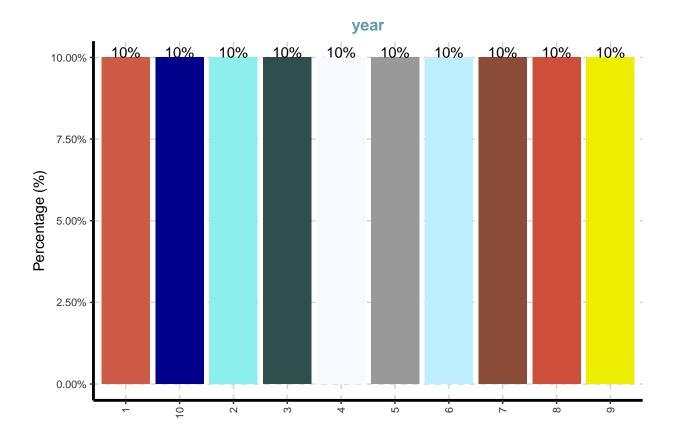
```
##
       workerid
                       year
                                       ui
                                                         quarter
##
   Min. : 1
                  Min. : 1.0
                                         :0.0004503
                                                      Min. :1.000
                                 Min.
##
   1st Qu.:124
                  1st Qu.: 3.0
                                 1st Qu.:0.2438383
                                                      1st Qu.:2.000
##
   Median:248
                  Median: 5.5
                                 Median: 0.4766747
                                                      Median :2.000
##
   Mean
           :248
                  Mean
                        : 5.5
                                 Mean
                                         :0.4879205
                                                      Mean
                                                            :2.517
##
   3rd Qu.:372
                  3rd Qu.: 8.0
                                 3rd Qu.:0.7447072
                                                      3rd Qu.:4.000
##
   Max.
           :495
                  Max.
                        :10.0
                                 Max.
                                         :0.9957856
                                                      Max.
                                                            :4.000
##
##
          q1
                          wage
                                            educ
                                                            exper
##
   Min.
           :0.0000
                     Min. : 662.1
                                      Min.
                                             : 0.000
                                                        Min. : 0.00
##
    1st Qu.:0.0000
                     1st Qu.:1226.8
                                      1st Qu.: 2.322
                                                        1st Qu.: 9.00
##
   Median :0.0000
                     Median :1718.1
                                                        Median :15.00
                                      Median : 4.646
   Mean :0.2404
                     Mean :1998.8
                                      Mean : 5.226
                                                        Mean :14.34
##
   3rd Qu.:0.0000
                     3rd Qu.:2482.9
                                       3rd Qu.: 7.635
                                                        3rd Qu.:19.00
##
   Max.
         :1.0000
                     Max.
                           :7170.2
                                      Max.
                                             :19.446
                                                        Max.
                                                               :28.00
##
##
        union
                         exper2
                                          lnwage
                                                                         yy2
                                                           yy1
##
   Min.
          :0.0000
                     Min. : 0.0
                                     Min.
                                             :6.495
                                                      Min.
                                                           :0.0
                                                                    Min.
                                                                            :0.0
##
   1st Qu.:0.0000
                     1st Qu.: 81.0
                                     1st Qu.:7.112
                                                      1st Qu.:0.0
                                                                    1st Qu.:0.0
                     Median :225.0
   Median :0.0000
                                     Median :7.449
                                                      Median:0.0
                                                                    Median:0.0
   Mean
          :0.4863
                     Mean
                           :247.3
                                     Mean
                                            :7.483
                                                      Mean
                                                             :0.1
                                                                    Mean
                                                                           :0.1
##
   3rd Qu.:1.0000
                     3rd Qu.:361.0
                                     3rd Qu.:7.817
                                                      3rd Qu.:0.0
                                                                    3rd Qu.:0.0
##
           :1.0000
                            :784.0
                                             :8.878
   Max.
                     Max.
                                     Max.
                                                      Max.
                                                             :1.0
                                                                    Max.
                                                                           :1.0
##
##
                       yy4
                                                    уу6
         ууЗ
                                     уу5
                                                                  уу7
                         :0.0
   Min.
           :0.0
                  Min.
                                Min.
                                       :0.0
                                               Min.
                                                      :0.0
                                                             Min.
                                                                    :0.0
##
   1st Qu.:0.0
                  1st Qu.:0.0
                                1st Qu.:0.0
                                               1st Qu.:0.0
                                                             1st Qu.:0.0
   Median:0.0
                  Median:0.0
                                Median:0.0
                                               Median:0.0
                                                             Median:0.0
##
   Mean :0.1
                  Mean
                        :0.1
                                Mean
                                       :0.1
                                               Mean
                                                      :0.1
                                                             Mean
                                                                    :0.1
                                3rd Qu.:0.0
##
    3rd Qu.:0.0
                  3rd Qu.:0.0
                                               3rd Qu.:0.0
                                                             3rd Qu.:0.0
##
                         :1.0
   Max. :1.0
                  Max.
                                Max.
                                       :1.0
                                               Max.
                                                      :1.0
                                                             Max.
                                                                    :1.0
##
##
         уу8
                       уу9
                                     yy10
                                                 lag_lnwage
##
   Min. :0.0
                  Min. :0.0
                                Min. :0.0
                                               Min.
                                                      :6.495
   1st Qu.:0.0
                  1st Qu.:0.0
                                1st Qu.:0.0
                                               1st Qu.:7.085
   Median:0.0
                  Median:0.0
                                Median:0.0
                                               Median :7.425
##
   Mean
         :0.1
                  Mean
                        :0.1
                                Mean
                                        :0.1
                                               Mean
                                                      :7.455
##
   3rd Qu.:0.0
                  3rd Qu.:0.0
                                3rd Qu.:0.0
                                               3rd Qu.:7.784
##
   Max.
           :1.0
                  Max.
                         :1.0
                                Max.
                                        :1.0
                                               Max.
                                                      :8.724
##
                                               NA's
                                                      :495
```

### ftable(simulated\$year)

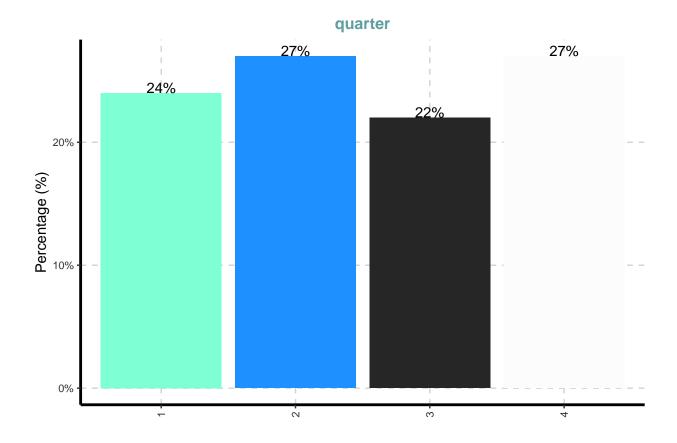
##		Variable	Valid	Frequency	Percent	CumPercent
##	1	year	1	495	10.00	10.00
##	2	year	10	495	10.00	20.00
##	3	year	2	495	10.00	30.00
##	4	year	3	495	10.00	40.00
##	5	year	4	495	10.00	50.00
##	6	year	5	495	10.00	60.00
##	7	year	6	495	10.00	70.00
##	8	year	7	495	10.00	80.00
##	9	year	8	495	10.00	90.00
##	10	year	9	495	10.00	100.00
##	11	year	TOTAL	4950	NA	NA
##	12	quarter	1	1190	24.04	24.04
##	13	quarter	2	1350	27.27	51.31
##	14	quarter	3	1070	21.62	72.93
##	15	quarter	4	1340	27.07	100.00
##	16	quarter	TOTAL	4950	NA	NA
##	17	q1	0	3760	75.96	75.96
##	18	q1	1	1190	24.04	100.00
##	19	_	TOTAL	4950	NA	NA
##	20	union	0	2543	51.37	51.37
##	21	union	1	2407	48.63	100.00
##	22	union		4950	NA	NA
##	23	уу1	0	4455	90.00	90.00
##	24	yy1	1	495	10.00	100.00
	25		TOTAL	4950	NA	NA
##	26	yy2	0	4455	90.00	90.00
##	27	yy2	1	495	10.00	100.00
##	28		TOTAL	4950	NA	NA
##	29	ууЗ	0	4455	90.00	90.00
##	30	уу3	1	495	10.00	100.00
##	31		TOTAL	4950	NA	NA
##	32	yy4	0	4455	90.00	90.00
##	33	yy4	1	495	10.00	100.00
##	34		TOTAL	4950	NA	NA
##	35	уу5	0	4455	90.00	90.00
##	36	уу5	1	495	10.00	100.00
	37		TOTAL	4950	NA	NA
	38	уу6	0	4455	90.00	90.00
	39	уу6	1	495	10.00	100.00
	40		TOTAL	4950	NA	NA
##		уу7	0	4455	90.00	90.00
	42	уу7	1	495	10.00	100.00
	43	уу7		4950	NA	NA
	44	уу8	0	4455	90.00	90.00
	45	уу8	1	495	10.00	100.00
	46		TOTAL	4950	NA	NA
	47	уу9	0	4455	90.00	90.00
	48	уу9	1	495	10.00	100.00
	49		TOTAL	4950	NA	NA
##		уу10	0	4455	90.00	90.00
		J J -				

# ExpCatViz(simulated)

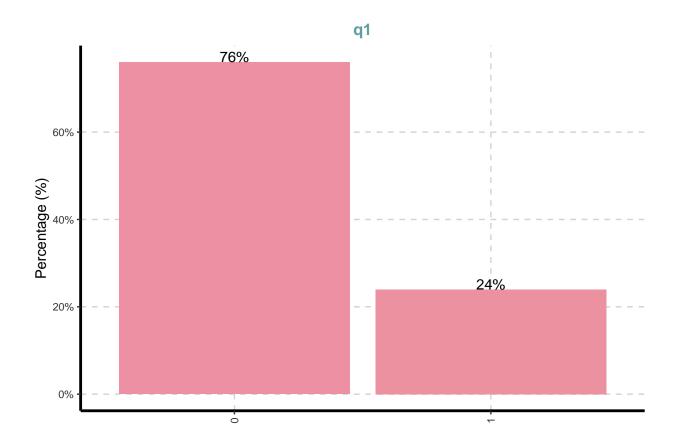
# ## [[1]]



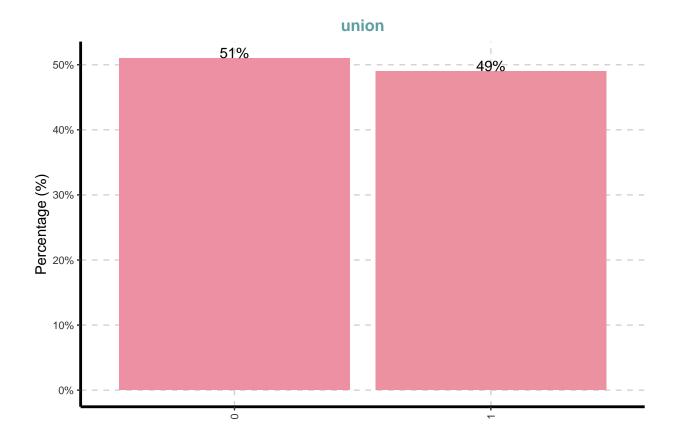
## ## [[2]]



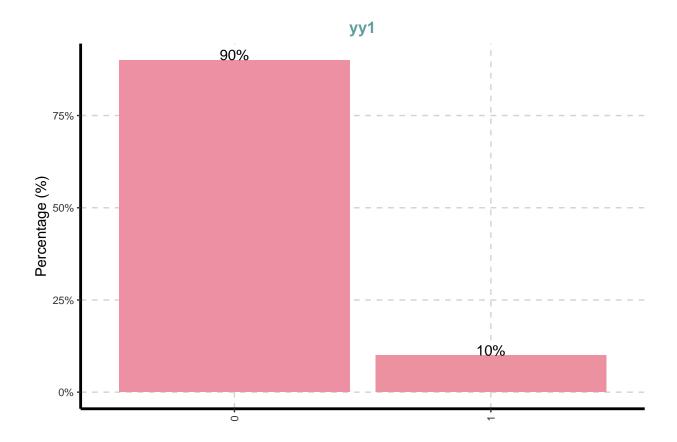
## ## [[3]]



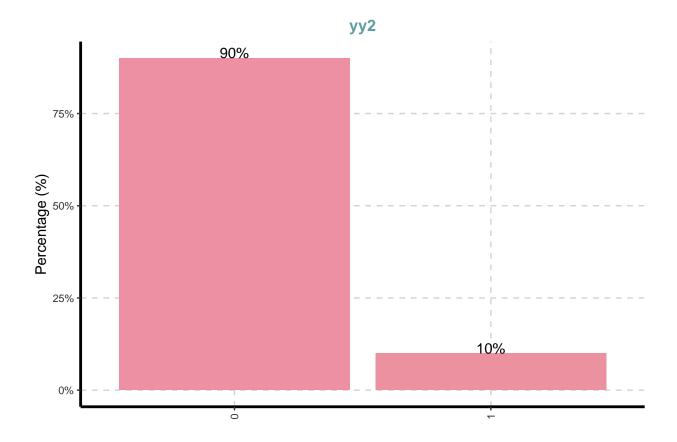
## ## [[4]]



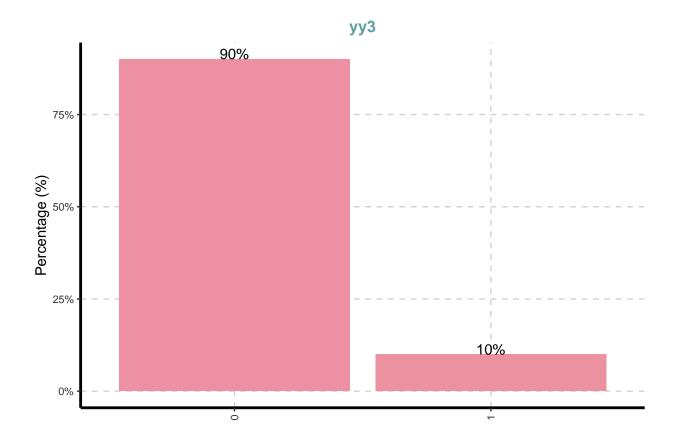
## ## [[5]]



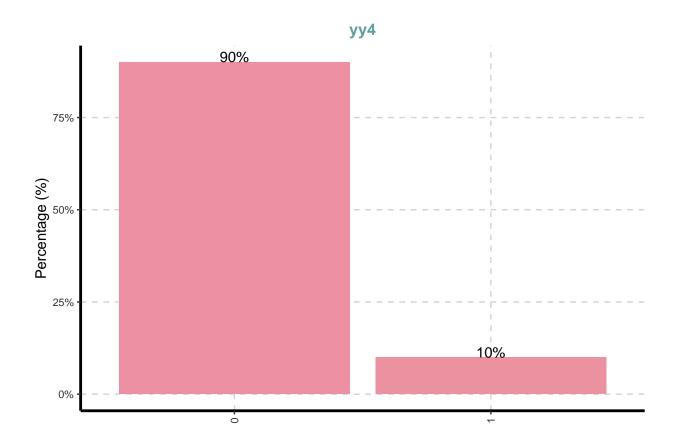
## ## [[6]]



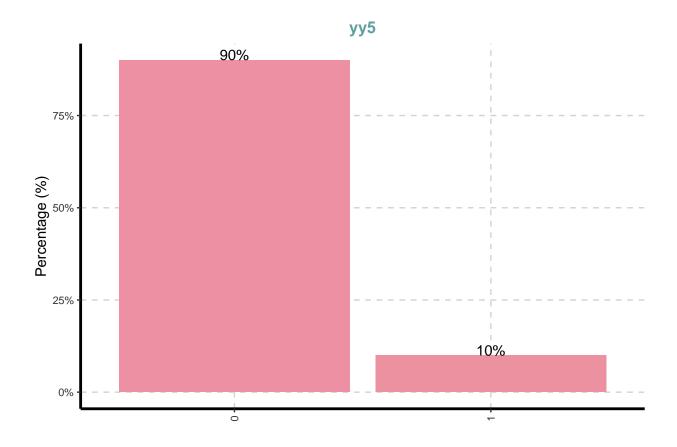
## ## [[7]]



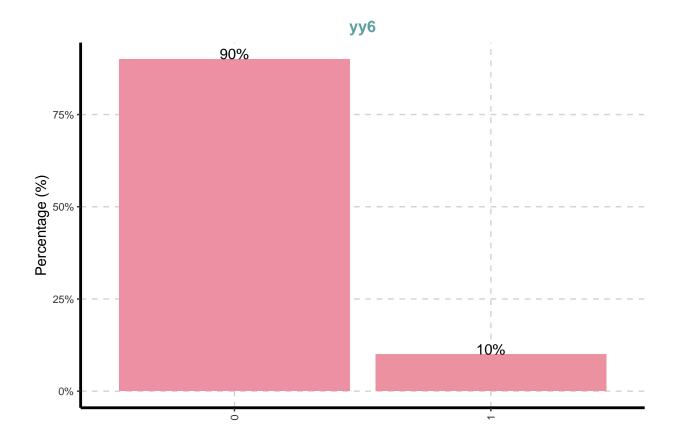
## ## [[8]]



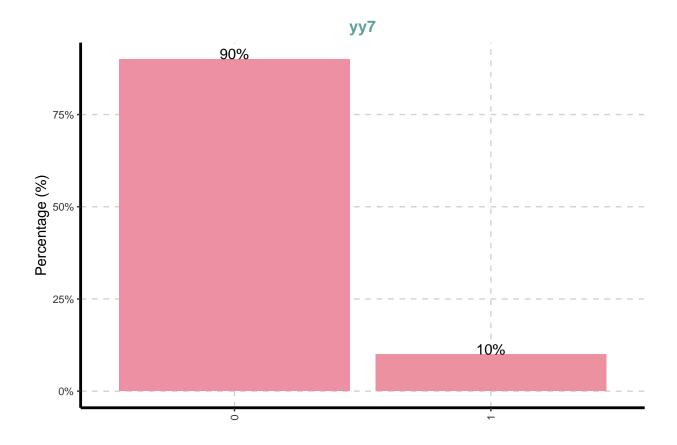
## ## [[9]]



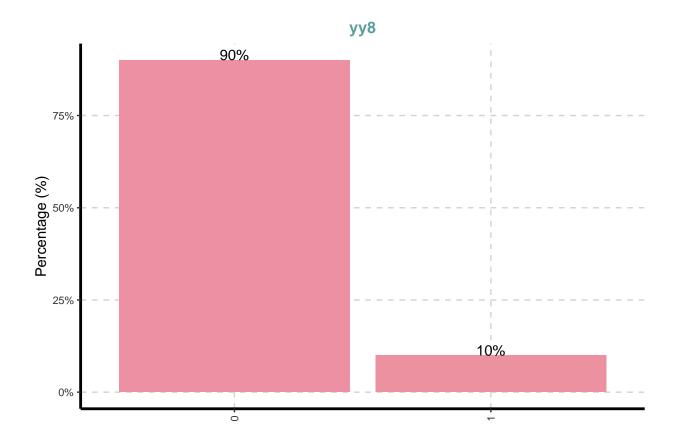
## ## [[10]]



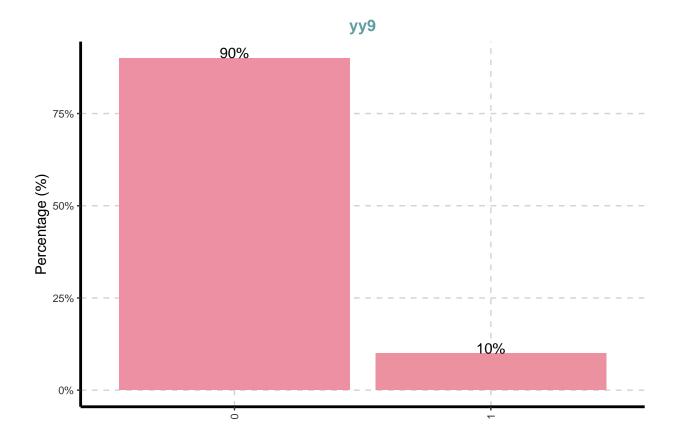
## ## [[11]]



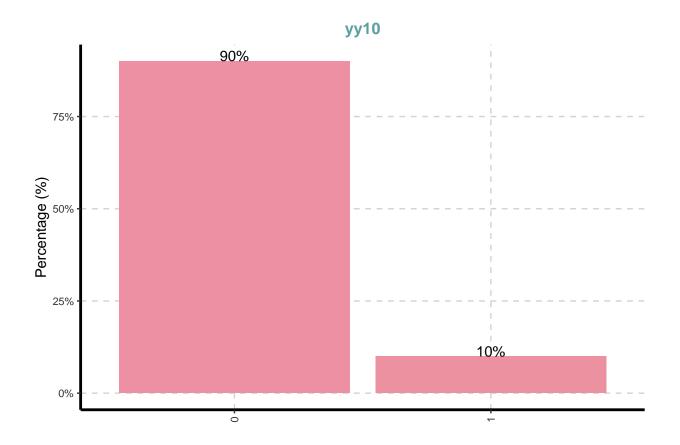
## ## [[12]]



## ## [[13]]



## ## [[14]]



TRY IN A 'JUPYTER NOTEBOOK': ExpNumViz(nlswork)

ExpNumStat(simulated,by="A",Outlier = TRUE,round=2,Qnt=c(0.1,0.25,0.50,0.99))

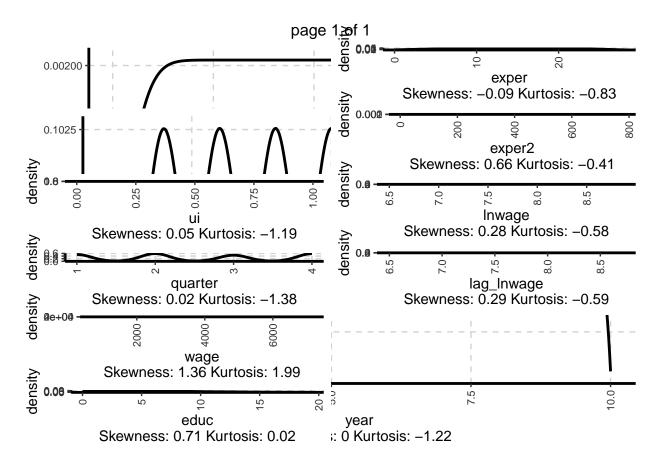
##		Vname	Group	TN	nNeg	nZero	nPos	NegIn	f PosIı	nf NA	_Value	Per_of_Miss	sing
##	5	educ	All	4950	0	333	4617	(	)	0	0		0
##	6	exper	All	4950	0	24	4926	(	)	0	0		0
##	7	exper2	All	4950	0	24	4926	(	)	0	0		0
##	9	lag_lnwage	All	4950	0	0	4455	(	)	0	495		10
##	8	lnwage	All	4950	0	0	4950	(	)	0	0		0
##	3	ui	All	4950	0	0	4950	(	)	0	0		0
##	4	wage	All	4950	0	0	4950	(	)	0	0		0
##	1	workerid	All	4950	0	0	4950	(	)	0	0		0
##	2	year	All	4950	0	0	4950	(	)	0	0		0
##		sum	min	l	max	mear	n med	lian	SD	CV	I	R Skewness	
##	5	25870.22	0.00	19	9.45	5.23	3 4	1.65	3.79	0.73	5.3	0.71	
##	6	70965.00	0.00	28	3.00	14.34	15	5.00	6.46	0.45	10.0	00 -0.09	
##	7	1223895.00	0.00	784	1.00	247.25	225	5.00	187.13	0.76	280.0	0.66	
##	9	33211.94	6.50	) {	3.72	7.45	5 7	7.43	0.47	0.06	0.7	70 0.29	
##	8	37041.95	6.50	) {	3.88	7.48	3 7	7.45	0.48	0.06	0.7	71 0.28	
##	3	2415.21	0.00	) :	1.00	0.49	9 (	.48	0.29	0.59	0.5	0.05	
##	4	9893953.84	662.08	7170	0.24	1998.78	3 1718	3.12 10	032.19	0.52	1256.1	1.36	
##	1	1227600.00	1.00	495	5.00	248.00	248	3.00	142.91	0.58	248.0	0.00	

```
0.00
## 2
       27225.00
                   1.00
                           10.00
                                     5.50
                                              5.50
                                                      2.87 0.52
                                                                     5.00
##
     Kurtosis
                  10%
                           25%
                                    50%
                                            99% LB.25%
                                                          UB.75% nOutliers
                 0.52
## 5
         0.02
                          2.32
                                   4.65
                                          15.46
                                                   -5.65
                                                            15.61
        -0.83
                 5.00
                          9.00
                                                   -6.00
                                                                           0
## 6
                                  15.00
                                          27.00
                                                            34.00
##
        -0.41
                25.00
                         81.00
                                225.00
                                         729.00
                                                 -339.00
                                                           781.00
                                                                          19
        -0.59
                 6.86
                          7.08
                                  7.43
                                           8.55
                                                    6.04
                                                             8.83
## 9
                                                                           0
        -0.58
                 6.88
                          7.11
                                   7.45
                                           8.61
                                                    6.05
## 8
                                                             8.87
                                                                           1
        -1.19
                 0.08
                          0.24
                                   0.48
                                           0.99
                                                   -0.51
## 3
                                                             1.50
                                                                           0
##
         1.99 969.90 1226.81 1718.12 5468.17 -657.39 4367.13
                                                                         186
                        124.00
                                248.00
## 1
        -1.20
                50.00
                                         490.51 -248.00
                                                           744.00
                                                                           0
## 2
        -1.22
                 1.90
                          3.00
                                   5.50
                                          10.00
                                                   -4.50
                                                            15.50
                                                                           0
```

#### ExpNumViz(simulated, Page=c(6,2))

## Warning in matrix(data = seq(1, pn), nrow = nr, ncol = nc): data length [10] is
## not a sub-multiple or multiple of the number of rows [6]

#### ## \$'0'



# ExpOutliers(simulated, varlist=c("lnwage"))

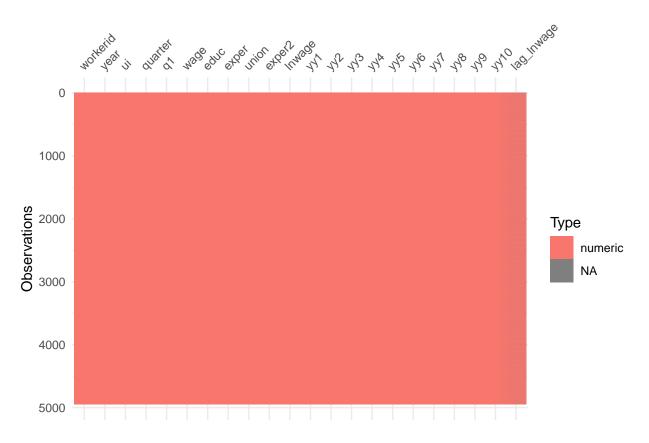
```
## $outlier_summary
## Category lnwage
## 1 Lower cap : 0.05 6.75808242272123
```

```
## 2
        Upper cap: 0.95 8.32169651894011
## 3
             Lower bound
                                      6.05
## 4
             Upper bound
                                      8.87
## 5
         Num of outliers
                                         1
## 6
     Lower outlier case
      Upper outlier case
                                       210
## 7
## 8
             Mean before
                                      7.48
## 9
              Mean after
                                      7.48
## 10
           Median before 7.44898780138622
## 11
            Median after 7.44896911785069
##
## $outlier_data
                         ui quarter q1
##
         workerid year
                                                            educ exper union exper2
                                                  wage
##
               1
                                        2 0 1913.481 6.3080420
                                                                            1
                                                                                  289
                      1 0.5734584
                                                                     17
##
      2:
                1
                      2 0.5734584
                                        2 0 2065.687 6.3080420
                                                                     18
                                                                            1
                                                                                  324
                                        2 0 2015.642 7.3080420
##
      3:
                1
                      3 0.5734584
                                                                     19
                                                                            1
                                                                                  361
##
      4:
                      4 0.5734584
                                        2 0 2274.630 8.3080425
                                                                     20
                                                                            1
                                                                                  400
                1
##
      5:
                1
                      5 0.5734584
                                        2 0 2576.639 9.3080425
                                                                                  441
##
## 4946:
              495
                      6 0.3515452
                                        1 1 1257.155 0.0000000
                                                                                  289
                                                                     17
                                                                            1
## 4947:
              495
                      7 0.3515452
                                        1 1 1170.614 0.3515451
                                                                     18
                                                                            1
                                                                                  324
## 4948:
              495
                      8 0.3515452
                                        1 1 1211.788 0.3515451
                                                                     19
                                                                                  361
## 4949:
              495
                      9 0.3515452
                                        1 1 1346.442 0.3515451
                                                                     20
                                                                            1
                                                                                  400
## 4950:
              495
                    10 0.3515452
                                         1
                                           1 1279.959 0.3515451
                                                                                  441
##
           lnwage yy1 yy2 yy3 yy4 yy5 yy6 yy7 yy8 yy9 yy10 lag_lnwage
      1: 7.556680
                    1
                         0
                             0
                                 0
                                     0
                                         0
                                              0
                                                  0
                                                      0
                                                           0
                                                                      NA
##
      2: 7.633218
                    0
                         1
                             0
                                 0
                                     0
                                         0
                                              0
                                                  0
                                                      0
                                                           0
                                                                7.556680
##
      3: 7.608693
                    0
                         0
                             1
                                 0
                                     0
                                         0
                                              0
                                                  0
                                                      0
                                                           0
                                                                7.633218
##
                    0
                         0
                             0
                                     0
                                         0
                                              0
                                                  0
                                                      0
                                                                7.608693
      4: 7.729573
                                 1
                                                           0
##
      5: 7.854241
                                 0
                                         0
                                                  0
                                                                7.729573
                                     1
                                              0
                                                      0
                                                           0
     ___
##
## 4946: 7.136607
                    0
                         0
                             0
                                 0
                                     0
                                              0
                                                  0
                                                      0
                                                           0
                                                                6.973784
                                         1
## 4947: 7.065284
                             0
                                 0
                                     0
                                         0
                                                  0
                    0
                         0
                                              1
                                                      0
                                                           0
                                                                7.136607
## 4948: 7.099852
                    0
                         0
                             0
                                 0
                                     0
                                         0
                                            0
                                                  1
                                                      0
                                                           0
                                                                7.065284
## 4949: 7.205221
                                         0
                    0
                         0
                             0
                                 0
                                     0
                                              0
                                                  0
                                                      1
                                                           0
                                                                7.099852
## 4950: 7.154584
                    0
                                 0
                                     0
                                         0
                                                 0
                                                      0
                                                           1
                                                                7.205221
##
         out cap lnwage
##
      1:
               7.556680
##
      2:
               7.633218
##
      3:
               7.608693
##
               7.729573
##
      5:
               7.854241
## 4946:
               7.136607
## 4947:
               7.065284
## 4948:
               7.099852
## 4949:
               7.205221
## 4950:
               7.154584
##
## $outlier_index
## $outlier_index$upper_out_index
## $outlier_index$upper_out_index[[1]]
## [1] 210
##
```

```
##
## $outlier_index$lower_out_index
## $outlier_index$lower_out_index[[1]]
## numeric(0)
```

vis\_dat(simulated)

##



## ##	Summary statistics										
	Statistic	N	Mean	St. Dev.	Min	Pct1(25)	Pct1(75)	Max			
	workerid	4,950	248.000	142.908	1	124	372	495			
##	year	4,950	5.500	2.873	1	3	8	10			
##	ui	4,950	0.488	0.289	0.0005	0.244	0.745	0.996			
##	quarter	4,950	2.517	1.128	1	2	4	4			
##	q1	4,950	0.240	0.427	0	0	0	1			

```
4,950 1,998.779 1,032.194 662.083 1,226.806 2,482.937 7,170.242
## wage
## educ
           4,950
                  5.226
                           3.795
                                   0.000
                                          2.322
                                                7.635
                                                           19.446
           4,950 14.336
                           6.460
                                   0
                                           9
                                                   19
## exper
                                                             28
## union
           4,950
                 0.486
                                    0
                                            0
                                                             1
                           0.500
                                                    1
## exper2
           4,950 247.252 187.126
                                    0
                                           81
                                                    361
                                                             784
                                                   7.817
## lnwage
           4,950
                 7.483 0.476
                                 6.495 7.112
                                                            8.878
           4,950
                 0.100 0.300
                                   0
                                           0
                                                     0
## yy1
                                                             1
           4,950
                  0.100
                                                     0
## yy2
                         0.300
                                    0
                                            0
                                                              1
## yy3
           4,950
                  0.100 0.300
                                    0
                                            0
                                                     0
                                                              1
           4,950
                  0.100 0.300
                                    0
                                            0
                                                     0
## yy4
                                                              1
## yy5
           4,950
                  0.100
                           0.300
                                    0
                                           0
                                                     0
                                                             1
                                           0
                                                     0
           4,950
                  0.100
                           0.300
                                    0
## yy6
                                                             1
## yy7
                                            0
                                                     0
           4,950
                  0.100 0.300
                                    0
                                                             1
                                                     0
## yy8
           4,950 0.100 0.300
                                    0
                                            0
                                                             1
## yy9
           4,950
                  0.100
                           0.300
                                    0
                                            0
                                                     0
                                                              1
## yy10
           4,950
                  0.100
                           0.300
                                    0
                                            0
                                                     0
                                                              1
                  7.455
                                          7.085
                                                            8.724
## lag_lnwage 4,455
                           0.470
                                   6.495
                                                   7.784
```

```
## DASHBOARD

###### ExPanD()
```

# Regressions

OBSERVE THE MISTAKE FOLLOWING THE INTRODUCTION OF TIME DUMMIES AND EXPERIENCE IN THE FIXED-EFFECTS MODEL

```
pols <- plm(data = simulated, lnwage ~ educ + exper +</pre>
              exper2 + factor(year),
            model="pooling", index=c("workerid", "year"))
 re <- plm(data = simulated, lnwage ~ educ + exper +
            exper2 + factor(year),
          model="random", index=c("workerid", "year"))
  plmtest(pols, type=c("bp"))
##
## Lagrange Multiplier Test - (Breusch-Pagan) for balanced panels
##
## data: lnwage ~ educ + exper + exper2 + factor(year)
## chisq = 19885, df = 1, p-value < 2.2e-16
## alternative hypothesis: significant effects
 fe <- plm(data = simulated, lnwage ~ educ + exper +</pre>
              exper2 + factor(year),
            model="within", index=c("workerid", "year"))
 pFtest(fe, pols)
```

```
## F test for individual effects
##
## data: lnwage ~ educ + exper + exper2 + factor(year)
## F = 270.97, df1 = 493, df2 = 4444, p-value < 2.2e-16
## alternative hypothesis: significant effects
 phtest(fe, re)
##
  Hausman Test
##
##
## data: lnwage ~ educ + exper + exper2 + factor(year)
## chisq = 309.92, df = 11, p-value < 2.2e-16
## alternative hypothesis: one model is inconsistent
 pols_robust <- coeftest(pols, function(x) vcovHC(x, type = 'sss'))</pre>
  re_robust <- coeftest(re, function(x) vcovHC(x, type = 'sss'))</pre>
  fe_robust <- coeftest(fe, function(x) vcovHC(x, type = 'sss'))</pre>
  stargazer(pols_robust,re_robust, fe_robust,title = "Regression analysis",
            model.numbers = FALSE,
            column.labels = c("Pooled (cluster)", "RE (cluster)", "FE (cluster"),
            label = "regressions",
            table.placement = "!ht",
            notes.append = FALSE,
            notes.align="l",
            notes="Standard errors in parentheses.",
            header = FALSE,
            no.space = TRUE,
            omit = c("Constant"),
            omit.stat = c("adj.rsq", "f", "ser"),
            digits = 3,
            digits.extra = 5,
            omit.yes.no = c("Constant",""),
            dep.var.caption="",
            dep.var.labels.include = FALSE,
            style = "qje",
            type="text")
##
```

#### ## Regression analysis ## Pooled (cluster) RE (cluster) FE (cluster ## educ 0.107\*\*\* 0.067\*\*\* 0.062\*\*\* (0.002)## (0.001)(0.001)0.013\*\*\* 0.005\*\* 0.025\*\*\* ## exper (0.001)(0.005)(0.002)## -0.0003\* 0.000004 0.000004 ## exper2 ## (0.0002)(0.00002)(0.00002)-0.001 0.019\*\*\* 0.0002 ## factor(year)2 ## (0.004)(0.004)(0.003)## factor(year)3 -0.002 0.038\*\*\* 0.001 ## (0.005)(0.005)(0.003)

```
## factor(year)4
                                      0.052***
                                                    -0.004*
                        -0.008
##
                       (0.007)
                                      (0.007)
                                                    (0.003)
## factor(year)5
                                                    -0.0002
                        -0.004
                                      0.075***
##
                                      (0.009)
                                                    (0.002)
                       (0.009)
## factor(year)6
                        -0.005
                                      0.095***
                                                     0.001
##
                       (0.010)
                                      (0.011)
                                                    (0.003)
## factor(year)7
                        -0.009
                                      0.112***
                                                    -0.001
                                                    (0.003)
##
                       (0.012)
                                      (0.013)
## factor(year)8
                        -0.011
                                      0.131***
                                                    0.00004
##
                       (0.014)
                                      (0.015)
                                                    (0.003)
## factor(year)9
                        -0.013
                                      0.148***
                                                    -0.002
                                                    (0.003)
##
                       (0.016)
                                      (0.017)
## factor(year)10
                        -0.011
                                      0.169***
##
                       (0.018)
                                       (0.019)
## ===
## Notes:
                  Standard errors in parentheses.
```

# Close the log file

```
end_time <- Sys.time()
end_time - start_time</pre>
```

## Time difference of 58.05126 secs

```
# sprintf(end_time - start_time,fmt = '%#.1f')
```

#