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I. A

the prior:

the probability I am in Pittsburgh is $P(\text{in Pittsburgh}) = 0.9$, I am at my parents' home is $P(\text{at parents' home}) = 0.08$,
I am on vacation is $P(\text{on vacation}) = 0.02$

II. B

$P(\text{ocean}) = P(\text{ocean}|\text{in Pittsburgh})P(\text{in Pittsburgh}) + P(\text{ocean}|\text{at parents' home})P(\text{at parents' home}) +$
 $P(\text{ocean}|\text{on vacation})P(\text{on vacation}) = 0.02 \times 0.1 = 0.002$

the likelihood:

$P(\text{ocean}|\text{in Pittsburgh}) = 0$, $P(\text{ocean}|\text{at parents' home}) = 0$, $P(\text{ocean}|\text{on vacation}) = 0.1$

the posterior:

$$P(\text{in Pittsburgh}|\text{ocean}) = \frac{P(\text{ocean}|\text{in Pittsburgh})P(\text{in Pittsburgh})}{P(\text{ocean})} = 0$$

$$P(\text{at parents' home}|\text{ocean}) = \frac{P(\text{ocean}|\text{at parents' home})P(\text{at parents' home})}{P(\text{ocean})} = 0$$

$$P(\text{on vacation home}|\text{ocean}) = \frac{P(\text{ocean}|\text{on vacation})P(\text{on vacation})}{P(\text{ocean})} = 1$$