# CMPUT 366, Winter 2020 Assignment #3

Due: Tuesday, March 24, 2020, 11:59pm

Total points: 120

For this assignment use the following consultation model:

- 1. you can discuss assignment questions and exchange ideas with other *current* CMPUT 366 students;
- 2. you must list all members of the discussion in your solution;
- 3. you may **not** share/exchange/discuss written material and/or code;
- 4. you must write up your solutions individually;
- 5. you must fully understand and be able to explain your solution in any amount of detail as requested by the instructor and/or the TAs.

Anything that you use in your work and that is not your own creation must be properly cited by listing the original source. Failing to cite others' work is plagiarism and will be dealt with as an academic offence.

First name:	
Last name:	
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Collaborators:	

### 1. (Monte Carlo)

(a) [30 points] Implement rejection sampling in Python 3 by editing the rejection\_sampled\_expectation function in the provided rejectionSampling.py. The function should compute and return the expectation of the provided function f on the provided target distribution using rejection sampling. The rejectionSampling.py file contains an example monte\_carlo\_expectation function, and main function that will automatically test your implementation. You may edit the main file to perform any additional tests that you like.

We will run your code by importing the rejectionSampling module and calling rejection\_sampled\_expectation, so it is important that your code follow these naming conventions.

Submit all of your code for this question and question 2 (including provided boilerplate files) in a single zip file.

- (b) [3 points] Estimate the expected value of a Gaussian distribution with mean 1.75 and standard deviation 0.5, truncated below 0.75 and above 2.75. (This distribution is provided as trunc). Use your rejection sampling implementation to draw 2,000 samples from the target distribution. Use a Uniform[-3,3] distribution (the U33 distribution) as a proposal distribution.
  - i. What was the estimated expectation?
  - ii. How many samples were rejected?
- (c) [3 points] Estimate the expected value of a Gaussian distribution with mean 1.75 and standard deviation 0.5, truncated below 0.75 and above 2.75. (This distribution is provided as trunc). Use your rejection sampling implementation to draw 2,000 samples from the target distribution. Use an untruncated Gaussian distribution with mean 2.75 and standard deviation 0.5 (the untrunc distribution) as a proposal distribution.
  - i. What was the estimated expectation?
  - ii. How many samples were rejected?
- (d) [10 points] Were substantially more samples rejected using one proposal distribution than the other? If so, explain why. If not, explain why not.

(e) [6 points] Suppose you are evaluating a trained classifier using 0/1 loss on a test set of 1,000 examples. Your classifier's accuracy on the test set is 0.85 (i.e., 85%). Give an upper bound on the probability that the classifier's true accuracy (i.e., on the population from which the test set was drawn) is more than 5% different from 85%.

2. (Neural Networks) The MNIST dataset is a set of images of handwritten digits labelled by their actual digit. We will operate on two versions of this dataset: one with the images shifted 2 pixels to the upper-left, and one with the images shifted 2 pixels to the bottom-right.

This question requires the use of TensorFlow. You may need to install Tensorflow using the following command:

#### pip3 install tensorflow

(a) [10 points] Implement a fully-connected feed-forward neural network for classifying MNIST images according to the digit that they represent by editing the mlp2 function in the provided cnn.py file.

The network should have two hidden layers: one with 128 rectified linear ('relu') units, and one with 64 rectified linear units. The output should be a fully-connected layer of 10 units with the softmax activation. The cnn.py file contains an example implementation of a network with a single hidden layer in the mlp1 function that you may template from. The main function will test your program for you; you may add any tests that you like. It will also create a file called examples.png that contains examples images from the two test sets.

The function should train the network using the training features train\_x and labels train\_y, and then evaluate the accuracy of the trained network on two different test sets: test1\_x, test1\_y, and test2\_x, test2\_y. This is demonstrated in mlp1.

We will run your code by importing the cnn module and calling mlp2, so it is important that your code follow these naming conventions.

Submit all of your code for this question and question 1 (including provided boilerplate files) in a single zip file.

(b) [30 points] Implement a convolutional neural network for classifying MNIST images by editing the cnn function in the provided cnn.py file.

The network should have the following architecture:

- A layer of 32 convolutional units with a kernel size of  $5 \times 5$  and a stride of 1, 1.
- A max-pooling layer with a pool size of  $2 \times 2$  and a stride of 2, 2.
- A layer of 64 convolutional units with a kernel size of  $5 \times 5$  and the default stride.
- A max-pooling layer with a pool size of  $2 \times 2$  and the default stride.
- A Flatten layer (to reshape the image from a 2D matrix into a single long vector)
- $\bullet\,$  A layer of 512 fully-connected relu units
- A layer of 10 fully-connected softmax units (the output layer)

Submit all of your code for this question and question 1 (including provided boilerplate files) in a single zip file.

- (c) [2 points] What was the accuracy of your trained 2-hidden-layer feedforward network on the two test sets?
- (d) [2 points] What was the accuracy of your trained convolutional neural network on the two test sets?
- (e) [10 points] Did one of your implementations perform substantially better on one of the test sets than the other implementation did? If so, why? If not, why not?

## 3. (Bayesian Learning)

Suppose that you have three models  $(\theta_1, \theta_2, \theta_3)$  of changes in the price of a single stock. You know that one of these models is the true model. Each model gives the probability that tomorrow's price will be higher than today's price  $(y_{t+1})$ , based on whether today's price was higher than the price the day before  $(y_t)$ . So you can make money on average by buying the stock when  $p(y_{t+1} \mid y_t, \theta^*) > .5$  and selling when  $p(y_{t+1} \mid y_t, \theta^*) < .5$ , where  $\theta^*$  is the true model.

Your prior belief is that  $\theta_1$  and  $\theta_2$  are equally likely to be true, and  $\theta_3$  is three times more likely than  $\theta_1$  to be true.

You have a dataset D of past observations, and you have computed that

$$p(D \mid \theta_1) = .00084$$

$$p(D \mid \theta_2) = .00105$$

$$p(D \mid \theta_3) = .00007.$$

4. [6 points] What are the posterior probabilities of each model being the true model?

5. [4 points] Now suppose that you have run each model, and they make the following predictions:

$$p(y_{t+1} \mid y_t, \theta_1) = .75$$

$$p(y_{t+1} \mid y_t, \theta_2) = .4$$

$$p(y_{t+1} \mid y_t, \theta_3) = .6.$$

What is the maximum a posterior estimate for  $p(y_{t+1} | y_t)$ ? Based on the MAP estimate, would you be better off buying or selling?

#### 6. [4 points]

What is the estimate according to the posterior predictive distribution for  $p(y_{t+1} | y_t)$ ? (I.e., using model averaging.) Based on the PPD, would you be better off buying or selling?

# Submission

The assignment you downloaded from eClass is a single ZIP archive which includes this document as a PDF and its LATEX source as well as Python files needed for the coding questions. You are to unzip the archive into an empty directory, work on the problems and then zip the directory into a new single ZIP archive for submission.

Each assignment is to be submitted electronically via eClass by the due date. Your submission must be a single ZIP file containing:

- 1. a single PDF file with your answers;
- 2. file(s) with your Python code.

To generate the PDF file with your answers you can do any of the following:

- insert your answers into the provided LATEX source file between \begin{answer} and \end{answer}. Then run the source through LATEX to produce a PDF file;
- print out the provided PDF file and *legibly* write your answers in the blank spaces under each question. Make sure you write as legibly as possible for we cannot give you any points if we cannot read your hand-writing. Then scan the pages and include the scan in your ZIP submission to be uploaded on eClass;
- use your favourite text processor and type up your answers there. Make sure you number your answers in the same way as the questions are numbered in this assignment.