# A COMPARISON OF CRYPTOGRAPHY COURSES

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ABSTRACT. The author taught two courses on cryptography, one at Duke University aimed at non-mathematics majors and one at Rose-Hulman Institute of Technology aimed at mathematics and computer science majors. Both tried to incorporate technical and societal aspects of cryptography, with varying emphases. This paper will discuss the strengths and weaknesses of both courses and compare the differences in the author's approach.

## 1. Introduction

This paper is a description, and to some degree a comparison, of two courses on cryptography that I have taught. One was a course in "Cryptography and Society" at Duke University, aimed at non-mathematics majors and intended to explore both technical and societal aspects of cryptography. The other was a course in cryptography at my current school, the Rose-Hulman Institute of Technology, an undergraduate engineering college in Indiana. This course was more technically oriented and aimed at mathematics and computer science majors.

# 2. "Cryptography and Society"

During the fall of 2000, I taught a new course entitled "Cryptography and Society" at Duke University. This course was intended to introduce the student to the basic ideas of modern cryptography and its applications. It was primarily aimed at non-mathematics majors; mathematics majors were allowed to enroll but did not get credit towards their major. The course was suggested to me by my chair, Richard Hain, and was designed in part to fit a new university requirement in Science, Technology, and Society, and thus had a combination of technical and social topics. I also made an effort in the course to engage the students by bringing in examples from their daily lives. My approach to this course and many of the materials used were strongly influenced by courses taught by Stephen Greenfield at Rutgers University [5], Susan

 $Key\ words\ and\ phrases.$  teaching cryptography, course development, cryptography and society.

Landau at the University of Massachusetts at Amherst [6], and William Pardon at Duke University [12].

The course was a seminar, and by university policy thus had an enrollment cap of fifteen. Fifteen students started the course, and thirteen completed it. All levels of undergraduate from first-year through senior were present. The students' majors included Biological Anthropology and Anatomy, Biology, Economics, Mathematics, Political Science, Public Policy Studies, and undeclared. The published prerequisite was high school algebra only. Roughly half the students seemed to have no significant amount of college mathematics, while the others had varying amounts up through most of a mathematics major program. Students were required to buy four textbooks for the course: Joseph Silverman's A Friendly Introduction to Number Theory [17], Albrecht Beutelspacher's Cryptology [1], Whitfield Diffie and Susan Landau's Privacy on the Line [2], and Simson Garfinkel and Gene Spafford's Web Security & Commerce [3]. (Mathematics and Computer Science professors who are used to assigning only one textbook for the course should keep in mind the range of topics addressed and the fact that humanities courses generally assign more textbooks than technical ones.) More information about the course may be found at my archived copy of the course web page [7].

Three main themes were addressed throughout the course: how modern cryptographic protocols are implemented and their strengths and weaknesses; how one encounters (and will increasingly encounter in the future) cryptography in one's daily life; and the implications of widespread use of cryptography in the digital age both for individuals and for society. In addition to studying the mathematics behind modern cryptographic systems, we also examined the impact that the invention of modern cryptographic systems has had and will have on political, economic, philosophical, and sociological aspects of society. In order for the students to fully grasp this third theme, of course, they needed to something about the mathematics of cryptography, how it works and how it is used.

I tried in the course to schedule one day of mathematics, one technical day, and one day of societal issues in each week rather than splitting the course into blocks. (The course was taught on Monday, Wednesday, and Friday.) Of course, this could not be followed strictly for various reasons. I also scheduled three guest speakers, including someone from the Duke Medical Center, a Duke Law professor, and the Mathematics Department system administrator.

The mathematical part of the course introduced basic number theory and work with congruences, up through the Euler phi function and Euler's Theorem. The goal was to get all of the mathematics necessary to understand the RSA system of public-key encryption. There was also a short introduction to finite fields as a prequel to the discussion of the Advanced Encryption Standard (AES/Rijndael). My goals here were twofold. Firstly, I wanted to make sure students understood the mathematics behind the cryptosystems. Secondly I wanted them to see some of the basic ideas of number theory and abstract algebra, notably the concept of numbers as things which could behave differently depending on their context, that is, as an example of abstract elements in a field or ring.

I did my best to introduce the mathematics gently, using A Friendly Introduction to Number Theory supplemented by a few handouts. However, the material quickly became quite hard for many of the students with less mathematics background, and many seemed to feel that the textbook did not help. In retrospect, I think that the lack of mathematical prerequisites may have given them the impression that the course was going to be less mathematically intense than it turned out to be. More mathematical sophistication would have made the course easier, but I feel that it was important to teach a course which students of all backgrounds could take. Perhaps the answer was simply to be more up front (and more aware myself) about how much mathematics there was going to be and how hard it was going to get. Also, some topics, such as AES and elliptic curve cryptography (ECC), required special mathematical material to be introduced just for that topic. Some students thought this wasn't well integrated into the class.

Cryptosystems covered in the course included shift and affine ciphers, Hill ciphers, linear feedback shift registers, DES, AES/Rijndael, RSA, Diffie-Hellman key exchange, and ECC. The more technical systems were covered only in overview; notably DES, AES, and ECC. We also covered a number of related protocols and technical matters which were not cryptosystems, including digital signatures, message digests, subliminal channels, zero-knowledge proofs, and systems for secure e-mail and secure web browsing. A certain amount of cryptanalysis was also discussed, including the different types of information that a cryptanalyst might have available. There were three main goals for the selection of this group of topics. Firstly, I wanted to introduce a large selection of different types of ciphers and other systems. Secondly, I wanted ciphers which reinforced the mathematics concepts I thought the students should know. Thirdly, I wanted the students to see at least some ciphers which they might encounter in their daily lives.

In addition, I tried to keep this aspect of the course grounded in what cryptography could and could not be used for in practice, with an emphasis on the limitations of algorithms in the face of the real world. The textbook *Cryptology* was used for this part of the course along with a large number of handouts and web sites. Many of the students were quite comfortable with programming and computers and this seemed to be the easiest part of the course for them.

Discussions of the impact of cryptography on society were roughly grouped into political, economic, and philosophical spheres. Political implications that were discussed included the impact of cryptography on law enforcement, on patent law, the possibility of electronic voting, and the debate over personal privacy versus national security. Economic aspects centered around the startling growth of electronic banking and electronic commerce in the last few years, as well as the possibilities of legally binding digital signatures and the use of "digital cash". Philosophical and sociological implications included outgrowths of many of the above areas, especially the need to balance personal privacy with the public interest. In particular, we discussed law enforcement and the ability of the government to eavesdrop on private communications, government and corporate access to medical and banking records, and the ability to track electronic purchases or prevent them from being tracked.

Readings from *Privacy on the Line* were assigned to guide the discussion of the political and philosophical issues, while that book and *Web Security & Commerce* were used for economic issues. A number of handouts and web sites were also used in this part of the course. (A fairly complete list of readings for the course may be found in the course syllabus [8].) Classes for this part of the course were generally conducted as open discussions, as opposed to the more lecture-oriented classes in the rest of the course. This was a new experience for me as a mathematics professor, and as you might guess, student interest waxed and waned depending on the topic, the point in the course, the weather, and so on. In general, however, I felt that the discussions were useful and informative for everyone, myself included. Students also seemed very positive about the discussions. Many (though not all) students also liked the readings used in this part of the course.

Assignments for the course included weekly homework, a reading journal, a term paper, an in-class midterm, and a take-home final. There was also a small part of the grade based on classroom participation. (I did not, in the end, feel it necessary to penalize anyone for lack of participation.) The first weekly homework was an ungraded student survey, which included some basic information about the students, a pretest on some of the mathematical content of the course, and an opinion survey with four questions:

- (1) You should be able to copy any picture or music that you find on the Internet.
- (2) Suitable government authorities should be able to have access to your e-mail.
- (3) Personal financial and medical information should be totally secure from every inquiry.
- (4) Math is needed to build rockets. In order to make decisions about business or government policy, most people don't need to know very much math or even very much about what math can do.

(These questions, and several others on the pretest, were taken from a similar pretest used by Stephen Greenberg in his course.) I asked for a rating of how strongly they agreed or disagreed and some justification. There was a wide range of responses, which were also reflected in the way the students responded during class discussions. In retrospect, it would have been valuable to have re-done the survey at the end of class; I suspect that student answers would have changed somewhat, though probably not completely. (It might also have been interesting to see how a mathematics post-test went!)

Other weekly assignments included cipher problems to encode, decode, or break, purely mathematical problems, and essays ranging from paragraphs to 2–3 pages. There was also an assignment in which they had to use the computer program PGP to send, receive, and sign encrypted e-mail messages. Students seemed to enjoy the cipher problems most, although some also got rather creative with their essays. I graded the essays on aspects of composition as well as content; on the whole I was quite happy with the student writing. The mathematics problems seemed to cause the most problems. I allowed student to work in groups and had some difficulties early on with students who were clearly copying.

The reading journal consisted of paragraph summaries collected every week. The articles were supposed to be related to cryptography and published in a newspaper or newsmagazine during the previous month. Most students in fact got these articles off of the web. I did not insist that the article originate in a print publication, but I did try to make it clear that it should come from a professional news organization rather than a weblog or similar site. I also tried to focus these journals on summarizing the article rather than commentary, although I encouraged them to use their thoughts on the articles in their essays (perhaps not as much as I could have).

The term paper assignment was a 1–2 page proposal followed by two drafts of an 8–12 page paper. The topic was left open; it could be oriented towards mathematics, towards programming or software design, or towards discussions of policy and social aspects of cryptography. I gave a list of some examples. Many of the students chose to write on historical topics such as the Enigma cipher or the ADFGVX cipher. (The movie *U-571*, which was tangentially related to the Enigma cipher, had recently premiered at the time.) The class focused largely on modern ciphers rather than historical ones and some students, who were more historically minded, used the term paper as an opportunity to bring more of their interests to the course. This seemed quite appropriate to me, as I was interested in historical topics myself but did not feel that there was sufficient time to cover them in the course.

Both the in-class midterm exam and the take-home final were divided into short answer questions, mathematics problems and ciphers, and an essay. Short answer problems included:

- (1) Name two requirements mandated by HIPAA.
- (2) Name two public-key cryptosystems. Name two symmetric-key cryptosystems. (Specify which are which!)
- (3) Define operations intelligence and give an example.
- (4) What is Kerckhoff's Principle? Why is it important when defending against known-plaintext attacks?
- (5) In a paragraph, describe three ways in which Rijndael is similar to DES and three ways in which Rijndael is different from DES. Be complete and thorough.
- (6) In a paragraph, describe the difference between wiretaps, pen registers, and trap and trace. What sort of authorization (under normal circumstances) does a law-enforcement officer need in order to use each of these techniques?
- (7) In a paragraph, describe the differences between symmetrickey cryptosystems, message digests, and message authentication codes. Include the name of a system that you might use for each of these, and the mode of use if appropriate.
- (8) In a paragraph, describe three different uses we have made of "cut-and-choose" or "sealed envelope" techniques. Why were the envelopes sealed in each case? Why in each case did we choose some of the envelopes to open and others to remain sealed?
- (9) In a paragraph, explain how digital watermarking is a form of steganography. Then explain one form of steganography other than digital watermarking.

The mathematics and cipher section of the final exam had two long problems:

- (1) Your organization has just captured the secret plans (shown below) for the nonlinear feedback shift register that the enemy has been using to encrypt his communications. Unfortunately, the nonlinear table of values was smeared when your operative (Mallet) was forced to hide the plans in her mouth. However, Mallet was also able to learn that when the initialization string 1001 was used, the the letters "MA" (in ASCII) were encrypted as ciphertext 11010000 11011100. Mount a known ciphertext attack by using subtraction mod 2 to find the output of the nonlinear feedback shift register. Then work your way backwards, using subtraction mod 2 again where necessary, to fill in the missing table.
- (2) In this problem we will learn why we use modular arithmetic in the Diffie-Hellman key exchange system.
  - (a) You are Eve, and have captured Alice and Bob and imprisoned them. You overhear the following dialog.

Bob: Oh, let's not bother with the prime, it will make things easier.

Alice: Okay, but we still need a base s to raise things to. How about s = 3?

Bob: All right, then my result is 27.

Alice: And mine is 243.

What is Bob's secret b and Alice's secret a? What is their secret combined key?

(b) Alice and Bob continue:

Bob: How should we use our new secret key?

Alice: Oh, that's easy; we'll use it as a one-time pad. Divide the key into 2-digit groups. Use our cipher table (shown below) to change the plaintext letters into numbers, and write the plaintext numbers left to right under the key groups. Then add modulo 26 and convert it back to letters.

Bob: I can do that. (Shouts) Eve is a TQYR!

What did Bob say?

(c) Alice and Bob really should have reduced all their answers modulo some prime, such as p=37. If they had done that, how would the exchange in part (a) have gone? What would have been their secret key?

- (d) What advantages did you, as Eve, have in part (a) that Eve would not have in part (c)?
- (e) Would having a subliminal channel in part (a) have helped Alice and Bob? Why or why not?

In retrospect, choosing two long problems seems to have been a mistake. For each of the two problems, most students got either all of the points or none of them, which did not allow for fine evaluation. Also, there was not much room for different ways of phrasing the answers, which made it easier to grade but difficult to tell if there was copying going on. (In the end I am still not certain in the case of one incident whether copying occurred.)

The midterm exam essay asked the student to write at least three good-sized paragraphs on one of the following topics:

- (1) The U.S. recently instituted new rules on export controls for cryptography. What are the main points of the new rules? Was the NSA for or against the new rules? Why? What about the Department of Commerce? Why?

  or:
- (2) A major cryptographic patent recently was released by its holder. What was it? Why was it released? In your opinion, should the patent have been granted in the first place? Why or why not? What do you think the impact will be of this patent passing into the public domain? Why?

The final exam essay asked the student to revisit one of the questions from the opinion survey conducted during the first week of class.

# 3. "Cryptography" at Rose-Hulman

More recently, I have been teaching a course entitled "Cryptography" at the Rose-Hulman Institute of Technology. This was taught once before I arrived at Rose-Hulman, by Prof. David Mutchler of the Computer Science department. Prof. Mutchler and I then team-taught the course during the Spring Quarters of 2002 and 2003. The course was listed as a topics course in Computer Science during 2002, and was cross-listed in both the Computer Science and Mathematics Departments in 2003 (and will be in the future). This course is primarily aimed towards majors in the two departments, and could be can be counted toward major programs in the departments in which it was listed. The topics in this course were fairly similar to those in the Duke course, but the tone was much more technically oriented. We did try to introduce some issues in the societal impact of cryptography.

In 2002, thirty-three students started the course and thirty-one completed it. (The official institute enrollment cap was thirty.) In 2003, twenty-five students started the course and twenty-one completed it. (The official institute enrollment cap was twenty-five.) In both cases, sophomores (including advanced standing first-years), juniors, and seniors were all represented, with more of the more advanced students. Majors were predominantly computer science or computer science mathematics double majors, with a few each of computer engineering, mathematics, and physics/computer science majors. The published prerequisites were one quarter of discrete mathematics (taken any time after the completion of calculus) and two quarters of computer science courses. The discrete mathematics prerequisite was waived in one case, which proved not to be a good idea. Students were required to buy two textbooks for the course: Williams Stallings' Cryptography and Network Security [18] and Stephen Levy's Crypto: How the Code Rebels Beat the Government — Saving Privacy in the Digital Age [10]. (Once again, two textbooks were necessary because of the incorporation of both technical and non-technical subjects.) More information about the course may be found at the course web page [9].

This course focused primarily on the mathematical background and practical implementation of modern cryptographic protocols. Although not formally a seminar, we tried to encourage an attitude where learning interesting material was primary and grades were secondary. To this end, there were no tests in the course and assignments were designed to allow students to focus on topics they found most interesting. As in the course at Duke, the mathematics and the technical details were intertwined with each other and with some discussion of societal issues. A typical four-class week might have one day concentrating on mathematics, two on cryptosystems or other protocols, and one on (recent) historical or societal issues.

The mathematical part of the course was very similar to the Duke course. The students were somewhat more mathematically sophisticated and had an easier time absorbing the topics, although the topics themselves were still mostly new to all but a few of the students. We spent more time on finite fields and elliptic curves than I did in the Duke course and thus were able to go into more detail with AES and elliptic curve cryptography. The goals of the mathematical part of the course were similar to those at Duke, although we also aimed to impart a degree of practical knowledge that the students might need in their future careers.

Cryptosystems covered in the course included shift and affine ciphers, Hill ciphers, Simplified DES, DES, Simplified AES, AES/Rijndael, RSA, Diffie-Hellman key exchange, and elliptic curve cryptography. The more technical background of the students allowed us to cover DES and AES in quite a bit more detail than I could at Duke. We used the simplified versions of these two algorithms created by Ed Schaefer (Santa Clara University) and his students [11, 14] in order to give our students hands-on experience with these ciphers. We also covered digital signatures, subliminal channels, zero-knowledge proofs, and a discussion of the information-theoretic idea of perfect secrecy. The mathematical and technical aspects of the course used Cryptography and Network Security as a textbook, along with some handouts and web sites. Some students seemed to think that a cryptography reference book would be more useful than a traditional textbook, and we may recommend one in the future, although I do not think we will require students to buy it. (Bruce Schneier's Applied Cryptography [15] is one possibility.)

Discussions of cryptography and society revolved around readings from Crypto: How the Code Rebels Beat the Government — Saving Privacy in the Digital Age. This is a popular, if somewhat sensational, account of the development of modern cryptography from roughly 1970 to the present. The story told in the book includes the development of many of the key ideas and protocols we discussed in the course. It also explores the reactions of government, business, and society to these developments, giving us a handle on which to hang class discussions on some of the same political, economic, and philosophical ideas covered in the Duke course. The book is certainly more lively than the books used in the Duke course. However, the overtly political tone put off some of the students in the course.

Assignments for the course included weekly homework, an oral report, and a research proposal. Students were also given points for readings and class discussions on *Crypto*. In the 2002 version of the course students were not given enough weekly homework and I think this was detrimental to their learning, especially of the more advanced topics. In the 2003 version students were given homework slightly less than weekly (six times during the ten-week course). Each homework was divided into "mathematics-inspired problems" and "computer science-inspired problems". The "mathematics-inspired problems" ranged over mathematical, algorithmic, and protocol-based topics but were all intended to be solved with paper and pencil and perhaps the assistance of a small computer program or a computer algebra system such as Maple. Many, but not all, were taken from *Cryptography and Network Security*. The "computer science-inspired problems" were slightly larger programming projects and included implementations of various

cryptosystems and protocols discussed in the class, investigations of cryptanalytic techniques, and the gathering of empirical evidence for various theorems and conjectures related to the course.

More homework problems were made available than students could possibly be expected to do. Each was assigned a number of points, and a certain minimum number of points was required on each part ("mathematics" and "computer science") of each homework assignment for a passing grade. Students could increase their grade beyond the minimum by earning points on any part of any assignment, without restriction. Our object was to encourage students to find problems which interested them, while still making sure they had some basic understanding of all areas of the course. Most students found the mathematics part of the homework more difficult than the computer science part, which was not surprising since most were computer science majors.

There were also several in-class projects which gave students a handson experience with some of the more important cryptosystems. The students worked through worksheets in small groups with assistance from the instructors. Most of these could also be turned in for homework credit. The topics included Simplified DES, the cryptanalysis of Simplified DES, Simplified AES, and RSA. (The RSA worksheet focused on the algorithms for fast exponentiation and fast probabilistic primality testing.)

The oral presentation was based on a technical article on cryptography chosen by the students with help from the instructors. Suggested sources included Cryptologia, the Journal of Cryptology, and the proceedings of CRYPTO, EUROCRYPT, ASIACRYPT, and similar conferences. Presentations were 20 minutes long and were intended to show that the student understood the basic technical ideas of the article and could communicate them in a way that impressed their importance upon the audience. Students were encouraged to use PowerPoint or similar presentation software. The difficulty of the material varied widely, depending on the level of the student. We took this into account to a degree when grading the article, but more emphasis was placed on making sure the student understood the material, regardless of difficulty. Quantum cryptography was a popular subject during the 2002 version of the course. Primality testing was very popular during the 2003 course, with three students collaborating on a series of presentations about the AKS deterministic primality test. Image-based steganography was a popular subject during both years. Quality of presentations varied quite a bit, to the degree that we had to ask some of the students in 2003 to repeat their presentations in order to get credit.

The research proposal was a 2–5 page paper which was intended to give students a chance to think about open problems and a taste of academic research in the field of cryptography. Students were asked to formulate and clearly state an open problem, explain why solving the problem would be valuable, and propose some promising directions for solving the problem. The students were told that the proposal would be considered a success if the student could convince the instructors that he or she had promising ideas that had a reasonable chance of contributing to the solution of the problem. Students were encouraged to get their open problems from the presentations of other students, although this was not strictly required. Students were discouraged from choosing a famous unsolved problem in the field, e.g., a proof of the security of RSA. Students were not required to carry out any of the actual research, of course.

Some proposals made by students included designing switching networks for use with quantum cryptography, the use of "cwatsets" [16] in symmetric-key cryptography, finding new ways to attack the one-time pad statistically, detecting cheating in translucent cryptography systems, and detecting image steganography using statistical methods. This was the first time most students had ever been asked to consider finding a significant problem of their own to investigate, and many students had to be encouraged to apply some creative and original thought. Also, few had any experience judging what made an idea likely to work in solving a research problem. In the end, some of the proposals were rather pedestrian, but some included some genuinely creative ideas. On the whole we thought the experience was very valuable for students, especially those who were nearing graduation and the "real world".

The final portion of the grade was based on the readings from *Crypto* and the accompanying classroom discussions, which were conducted in a similar fashion to the Duke course. At the beginning of each discussion, students were asked to do a "two-minute essay" answering two easy questions from the reading. Often, the questions asked the students what found most interesting on a certain topic. These "essays" were use to judge whether the students had done the reading and also sometimes to stimulate the classroom discussions. Students were also given points for being present on the day of the discussion. Not all students participated actively in the discussions, but many contributed comments and there was a certain amount of heated debate. In general, students in the Rose-Hulman course did not seem as inclined to

argue about these topics as the students in the Duke course. This was probably due to a combination of the difference in the course and the difference in the student body as a whole.

### 4. Conclusion

One of the striking things about these two courses is how a fairly similar set of material can produce two entirely different courses depending on the emphasis of the instructor and the abilities and interests of the students. Obviously, the stronger technical background of the Rose-Hulman students allowed a greater amount of depth in the technical areas of the course. On the other hand, the less technically oriented non-mathematics majors at Duke were perhaps better able to come to grips with the social aspects and implications of cryptography which we tried to bring out in both courses. One of the things that I hoped to achieve in the Duke course was to demonstrate that there was value in bringing technical material on cryptography to students with a limited background but a strong interest. This was not as successful as I would have liked, and a comparison of my experiences in the two courses makes it clear that a stronger technical background does lead to a better understanding of the material. This is perhaps no surprise. I still feel, however, that introducing the Duke students to technical aspects of cryptography also enhanced their understanding of the non-technical aspects.

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### References and Other Resources

[1] Beutelspacher, A. 1994. *Cryptology*, MAA Spectrum. Washington DC: Mathematical Association of America.

- [2] Diffie, W. and Landau, S. 1998. Privacy on the Line. Cambridge MA: MIT Press.
- [3] Garfinkel, S. and Spafford, G. 1997. Web Security & Commerce. Sebastopol CA: O'Reilly.
- [4] Garfinkel, S. and Spafford, G. 2001. Web Security, Privacy & Commerce, 2nd ed. Sebastopol CA: O'Reilly.
- [5] Greenfield, S. Math 103\_H1 in Fall 1999. http://www.math.rutgers.edu/~greenfie/currentcourses/math103/math103\_index.html
- [6] Landau, S. Susan Landau. http://research.sun.com/people/slandau/
- [7] Holden, J. Math65S. http://www.rose-hulman.edu/Class/ma/holden/ Duke/Math65S/
- [8] Holden, J. Math65S Syllabus. http://www.rose-hulman.edu/Class/ma/holden/Duke/Math65S/syllabus/
- [9] Holden, J. and Mutchler, D. MA 479 / CSSE 490: Cryptography. http://www.rose-hulman.edu/class/ma/holden/Math479/
- [10] Levy, S. 2002. Crypto: How the Code Rebels Beat the Government Saving Privacy in the Digital Age. New York NY: Penguin Books.
- [11] Musa, M., Schaefer, E., and Wedig, S. 2003. A simplified AES algorithm and its linear and differential cryptanalyses. *Cryptologia*. **27**(2): 148–177.
- [12] Pardon, W. William L. Pardon. http://www.math.duke.edu/~wlp/
- [13] Phan, R. C.-W. 2002. Mini Advanced Encryption Standard (Mini-AES): a testbed for cryptanalysis students. *Cryptologia*. **26**(4): 283–306.
- [14] Schaefer, E. 1996. A simplified Data Encryption Standard algorithm. *Cryptologia*. **20**(1): 77–84.
- [15] Schneier, B. 1996. Applied Cryptography, 2nd ed. John Wiley and Sons.
- [16] Sherman, G. Cwatsets Page. http://www.cwatsets.org
- [17] Silverman, J. 1996. A Friendly Introduction to Number Theory. Prentice Hall.
- [18] Stallings, W. 2003. Cryptography and Network Security: Principles and Practice, 3rd ed. Prentice Hall.

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