

Synthetic Control (Sam's version)

INFO/STSCI/ILRST 3900: Causal Inference

7 Nov 2023

Learning goals for today

At the end of class, you will be able to:

1. Explain the intuition behind synthetic control
2. Understand how synthetic control relates to other causal inference methods

Logistics

- ▶ This week, read Ch 10 of The Causal Inference Mixtape

What is the effect of personal events on google searches?

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- ▶ When is the last time you googled a celebrity?
- ▶ Why do people google celebrities?
- ▶ Do certain events cause google searches on an individual to increase/decrease?

NFL Top 100

Before the start of each season, all current NFL players vote on the top players



(1) Mahomes



(2) Jefferson



(3) Hurts

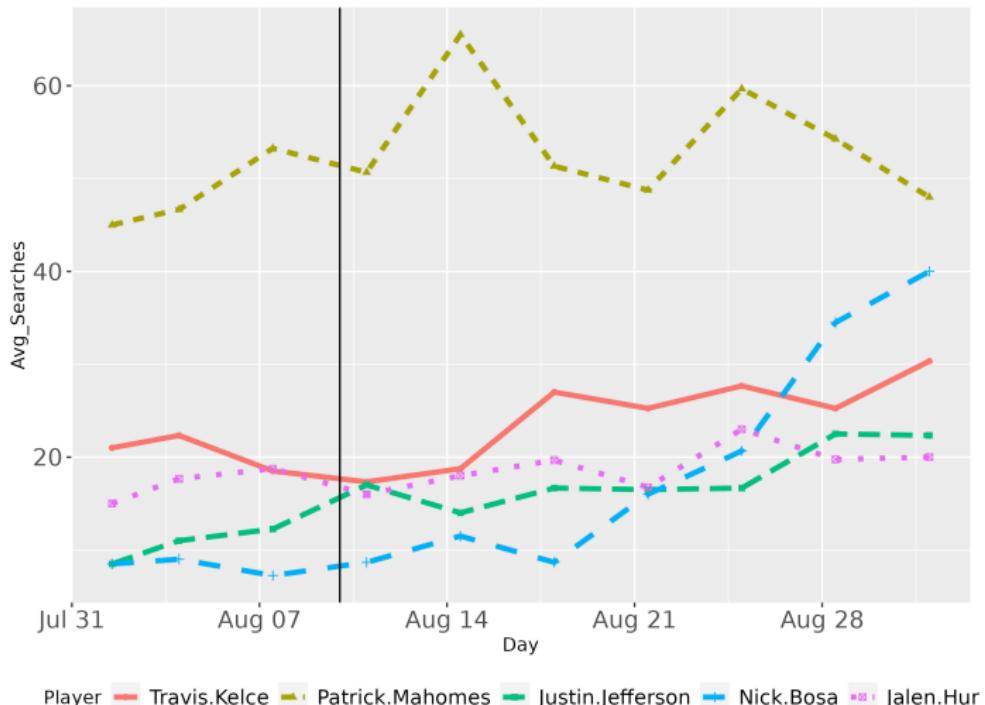


(4) Bosa

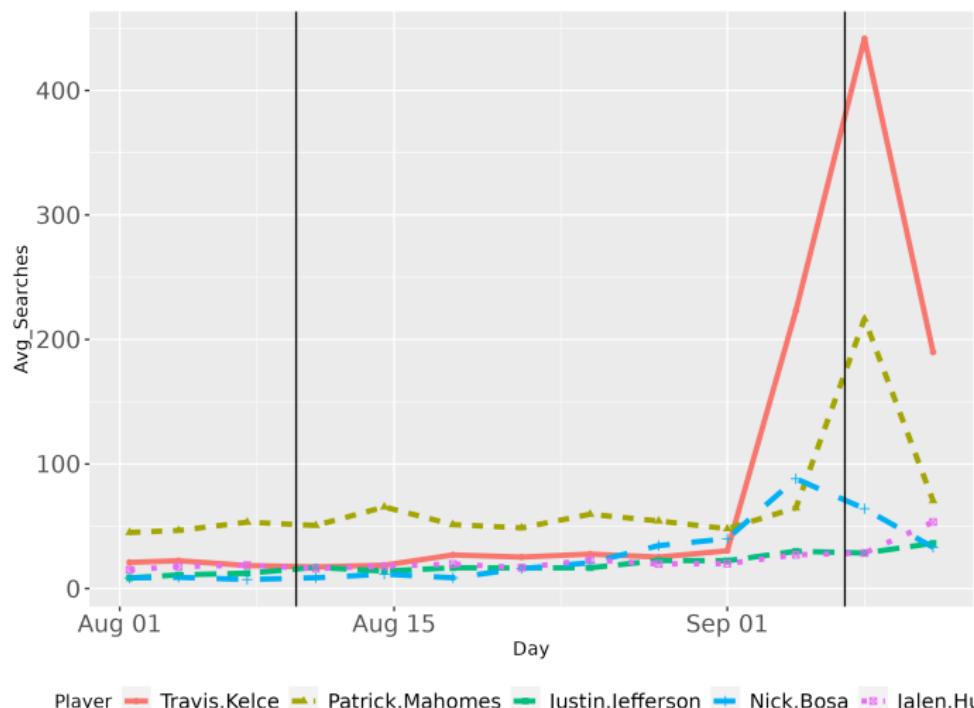


(5) Kelce

Google searches for NFL players



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≡ **CNN** entertainment Movies Television Celebrity

Jason Kelce addresses Travis Kelce and Taylor Swift dating speculation

By Lisa Respers France, CNN
Published 11:57 AM EDT, Fri September 15, 2023



Google searches for NFL players

Forbes

Taylor Swift's The Eras Tour Could Generate \$4.6 Billion For Local Economies

Hugh McIntyre Senior Contributor 

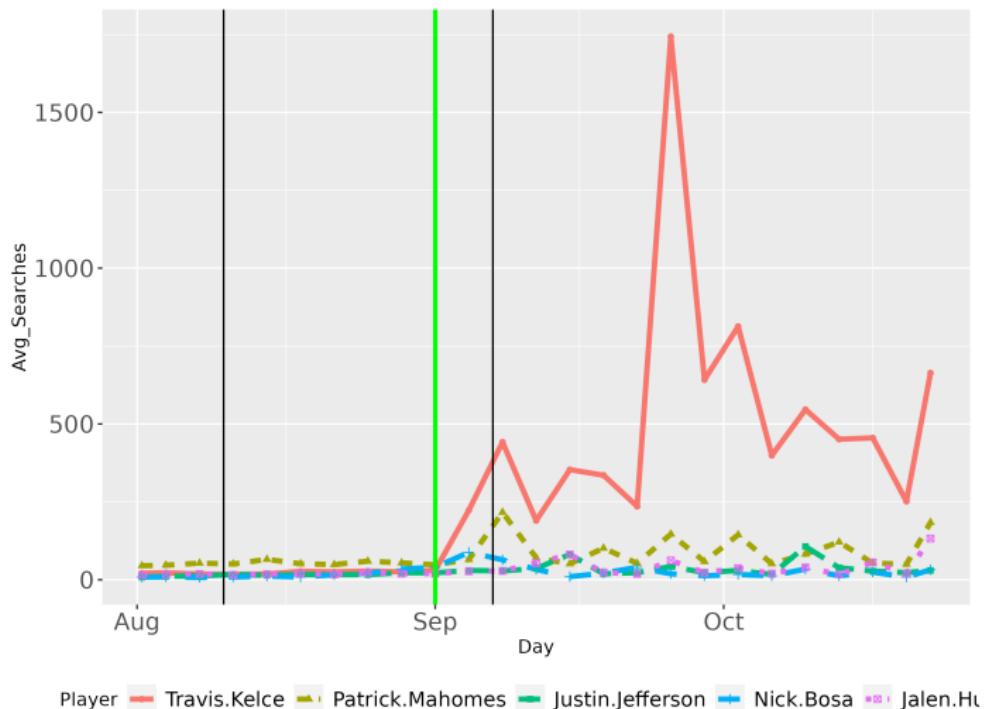
 Jun 9, 2023, 08:00am EDT

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- ▶ Causal effect at time t

$$\tau_{t,Kelce} = Y_{t,Kelce}^{\text{Swift}} - Y_{t,Kelce}^{\text{NoSwift}}$$

- ▶ For notation, let T_0 denote the time that the treatment occurs
- ▶ We observe $Y_{t,Kelce}^S$ for $t > T_0$ and $Y_{t,Kelce}^{NS}$ for $t < T_0$, but not at the same time!

Google searches for NFL players

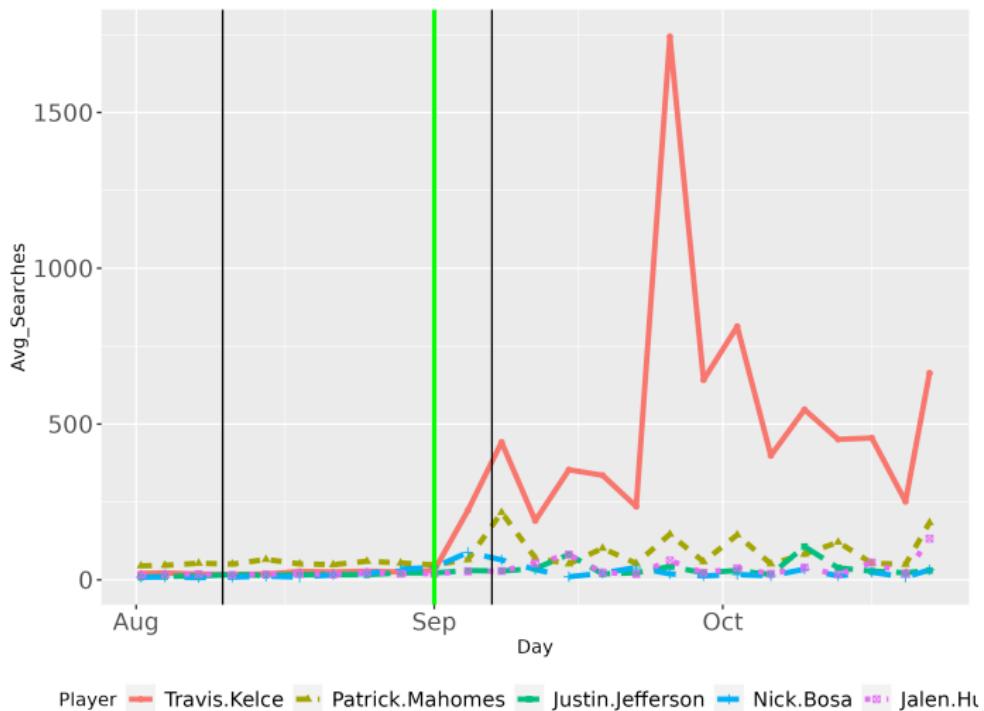
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- ▶ Blank space in our data

Google searches for NFL players



- ▶ Kelce and Mahomes play for the same team
- ▶ Kelce and Jefferson play similar positions
- ▶ Kelce and Bosa both went to college in Ohio

Synthetic Control

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- ▶ Estimating the effect far away from the treatment seems iffy
- ▶ Kelce doesn't quite match any individual player exactly, but is similar to other players in different ways

Synthetic Control

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- We don't observe $Y_{t,Kelce}^{\text{NS}}$ after T_0
- We do observe $Y_{t,Mahomes}^{\text{NS}}$, $Y_{t,Hurts}^{\text{NS}}$, etc.

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- We do observe $Y_{t, \text{Mahomes}}^{\text{NS}}$, $Y_{t, \text{Hurts}}^{\text{NS}}$, etc.
- Create a “synthetic” version of of Kelce by weighting other players

$$Y_{t, \text{Kelce}}^{\text{NS}} \approx w_1 Y_{t, \text{Mahomes}}^{\text{NS}} + w_2 Y_{t, \text{Hurts}}^{\text{NS}} + w_3 Y_{t, \text{Bosa}}^{\text{NS}} + w_4 Y_{t, \text{Jefferson}}^{\text{NS}}$$

where $w_j \geq 0$ and $\sum w_j = 1$

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- So perhaps, Synthetic Kelce is
 - 50% Patrick Mahomes
 - 25% Justin Jefferson
 - 25% Nick Bosa
 - 0% Jalen Hurts

Synthetic Control

- ▶ Estimate counterfactual Travis Kelce $Y_{t,Kelce}^{\text{NS}}$ by using Synthetic Kelce

$$Y_{t,Synthetic}^{\text{NS}} = .5 \times Y_{t,Mahomes} + .25 \times Y_{t,Bosa} + .25 \times Y_{t,Jefferson}$$

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- ▶ Straightforward approach boils down to picking “good” weights

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- ▶ We observe $Y_{t,Kelce} = Y_{t,Kelce}^{NS}$ before treatment when $t < T_0$

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- We observe $Y_{t,Kelce} = Y_{t,Kelce}^{NS}$ before treatment when $t < T_0$
- Select weights to minimize

$$\sum_{t < T_0} \left(Y_{t,Kelce} - \underbrace{w_1 Y_{t,M} + w_2 Y_{t,H} + w_3 Y_{t,B} + w_4 Y_{t,J}}_{Y_{t,Synthetic}} \right)^2$$

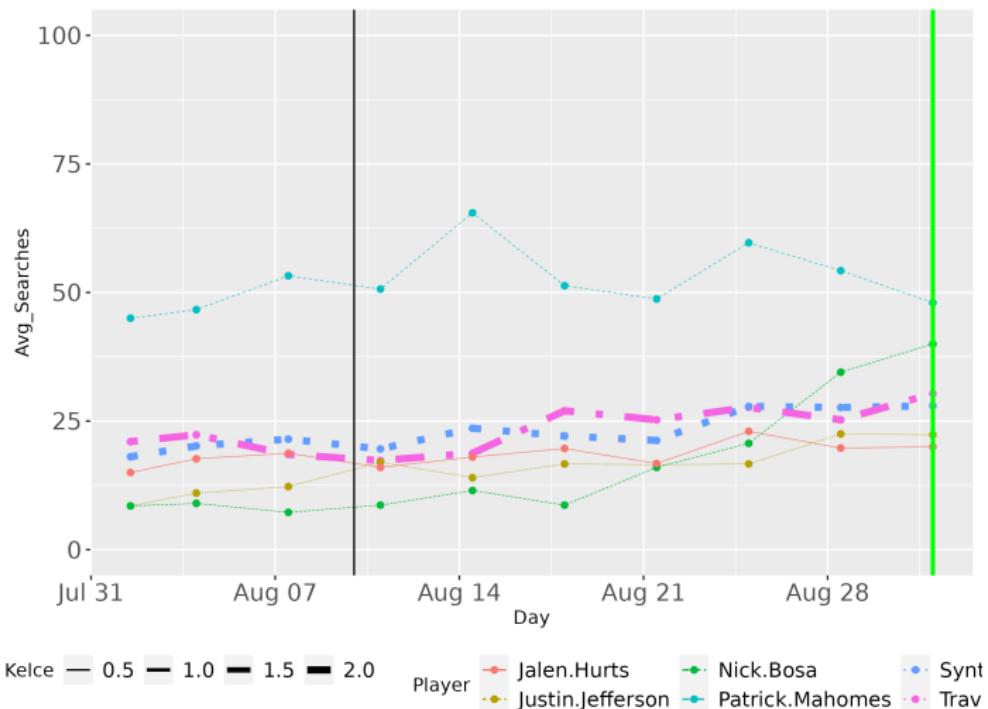
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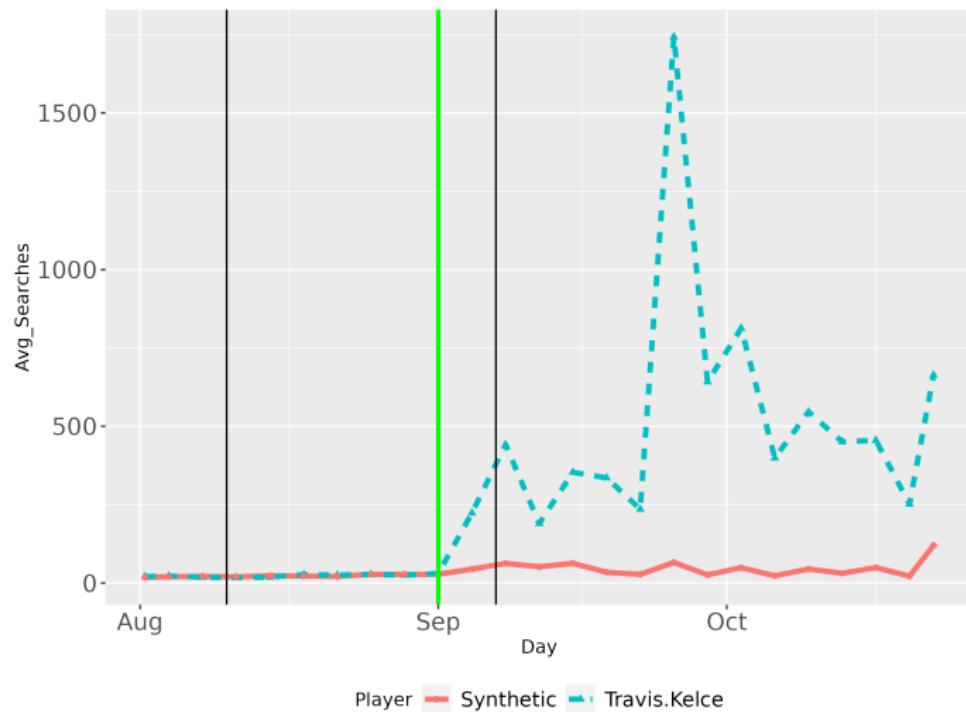
- Can also be selected to minimize discrepancy between other pre-treatment covariates (preview of discussion)

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- ▶ Data across time (longitudinal) so we also observed untreated outcomes of (eventually) treated unit
- ▶ Can directly match to minimize pre-treatment fit

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- ▶ In synthetic control, we have a similar assumption, but parallel trends holds for synthetic unit
- ▶ Generally, Diff-in-Diff has fixed set of comparison units using prior knowledge (i.e., NJ vs PA)
- ▶ Synthetic control, we can start with a large “donor pool” and select weights using data

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