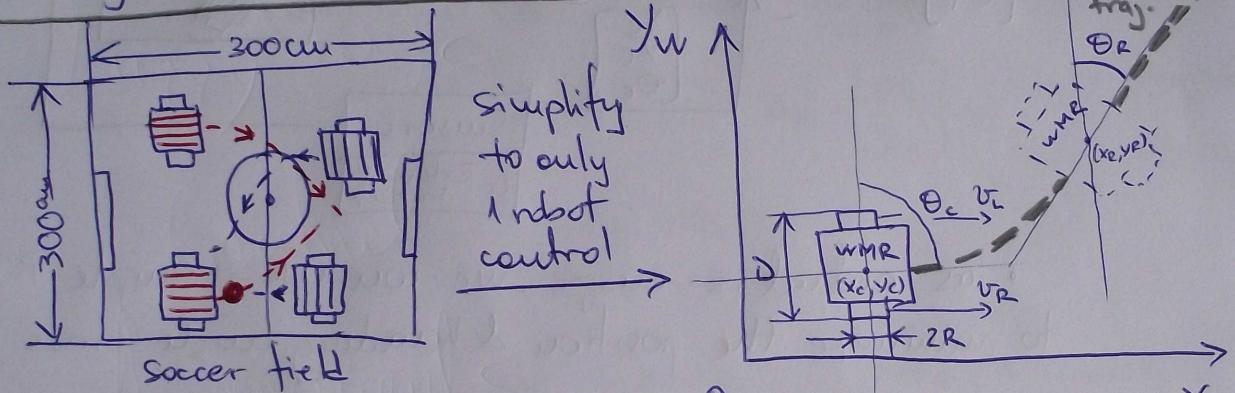


# Mobile robot Fuzzy logic Controller for Robot Soccer

Scenarios:

- ⊕ in robot soccer each team of 2 robots has a strategy to score in opponent's team post
- ⊕ robots' movement is described by reference trajectories on the field which must be tracked by robots in a certain time (trajectory tracking)



Robot kinematics

$$\left\{ \begin{array}{l} v_{wmr} = \frac{(v_L + v_R)}{2}; \\ \omega_{wmr} = \frac{(v_L - v_R)}{D}; \end{array} \right. ; \quad \left\{ \begin{array}{l} \dot{x}_c = v_{wmr} \cdot \cos \theta_c; \\ \dot{y}_c = v_{wmr} \cdot \sin \theta_c; \\ \dot{\theta}_c = \omega_{wmr}; \end{array} \right.$$

• trajectory tracking  
robot should track a parametrized curve in a given time with minimal error in distance & angle

The problem reduces in minimizing the mismatch between the current pose of the robot  $[x_c, y_c, \theta_c]^T$  and the reference (given by the curve)  $[x_r, y_r, \theta_r]^T$ .

The errors used are given as:

$$\left\{ \begin{array}{l} \text{dist. error} \\ \text{angle error.} \end{array} \right. \quad \left\{ \begin{array}{l} d_e = \sqrt{(x_r - x_c)^2 + (y_r - y_c)^2}; \\ \theta_e = \theta_r - \theta_c; \end{array} \right.$$

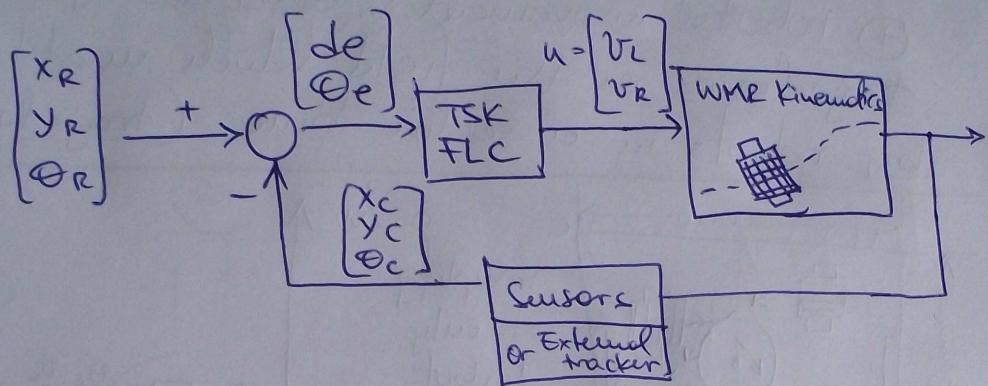
## 2 Proposals for problemsolving:

### ① TSK (Takagi - Sugeno - Kang) Fuzzy Controller

Problem

- no need for defuzzification, output is already crisp (real-world value) and ready to be sent to robot actuators (e.g. voltage / velocity reference)

- control loop architecture:



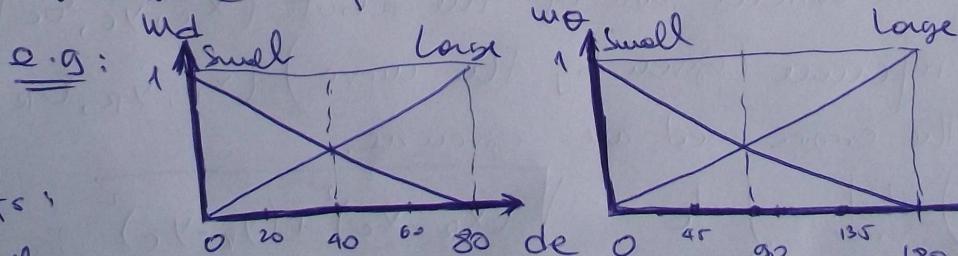
- as output is crisp, we can use a simple P-controller to minimize the position & heading angle errors:

$$u = \begin{bmatrix} v_L \\ v_R \end{bmatrix} = \begin{bmatrix} k_d \cdot de + k_\theta \cdot \theta_e \\ k_d \cdot de - k_\theta \cdot \theta_e \end{bmatrix}$$

### Fuzzy Controller Setup:

#### ① Fuzzification:

- only the 2 inputs  $[de, \theta_e]^T$  have membership values (are fuzzified)



sample mfs:

$$m_d^{\text{small}}(de) = \min\left(\max\left(0, \frac{de-80}{-160}\right), 1\right)$$

$$m_d^{\text{large}}(de) = 1 - m_d^{\text{small}}(de)$$

$$m_\theta^{\text{small}}(\theta_e) = \frac{-|\theta_e| + 180}{180}$$

$$m_\theta^{\text{large}}(\theta_e) = 1 - m_\theta^{\text{small}}(\theta_e)$$

## ② Fuzzy rules:

- as we chose only 2 membership functions for each of the inputs we have 4 rules

e.g.:

(R<sub>1</sub>): if de is small and |θ<sub>e</sub>| is small

$$\text{then } u_1 = \begin{bmatrix} v_{L1} \\ v_{R1} \end{bmatrix} = \begin{bmatrix} K_{d1} \cdot de + K_{\theta_1} \cdot \theta_e \\ K_{d1} \cdot de - K_{\theta_1} \cdot \theta_e \end{bmatrix}$$

where  $\begin{cases} K_{d1} = 0.250; \\ e.g. \quad K_{\theta_1} = 0.125; \end{cases}$

(R<sub>2</sub>): if de is small and |θ<sub>e</sub>| is large

$$\text{then } u_2 = \begin{bmatrix} v_{L2} \\ v_{R2} \end{bmatrix} = \begin{bmatrix} K_{d2} \cdot de + K_{\theta_2} \cdot \theta_e \\ K_{d2} \cdot de - K_{\theta_2} \cdot \theta_e \end{bmatrix}$$

where  $\begin{cases} K_{d2} = 0.250; \\ e.g. \quad K_{\theta_2} = 0.250; \end{cases}$

(R<sub>3</sub>): if de is large and |θ<sub>e</sub>| is small

$$\text{then } u_3 = \begin{bmatrix} v_{L3} \\ v_{R3} \end{bmatrix} = \begin{bmatrix} K_{d3} \cdot de + K_{\theta_3} \cdot \theta_e \\ K_{d3} \cdot de - K_{\theta_3} \cdot \theta_e \end{bmatrix}$$

where  $\begin{cases} K_{d3} = 0.800; \\ e.g. \quad K_{\theta_3} = 0.125; \end{cases}$

(R<sub>4</sub>): if de is large and |θ<sub>e</sub>| is large

$$\text{then } u_4 = \begin{bmatrix} v_{L4} \\ v_{R4} \end{bmatrix} = \begin{bmatrix} K_{d4} \cdot de + K_{\theta_4} \cdot \theta_e \\ K_{d4} \cdot de - K_{\theta_4} \cdot \theta_e \end{bmatrix}$$

where  $\begin{cases} K_{d4} = 0.800; \\ e.g. \quad K_{\theta_4} = 0.250; \end{cases}$

### ③. Output computation

- the output is just a weighted average of the individual rule outputs (only true for TSK)

$$u = \frac{\sum_{i=1}^4 w_i \cdot u_i}{\sum_{i=1}^4 w_i}$$

where  $w_i$  are the membership degrees computed using prod operation (as we have the and between the antecedents we can use min or prod when aggregating) such that:

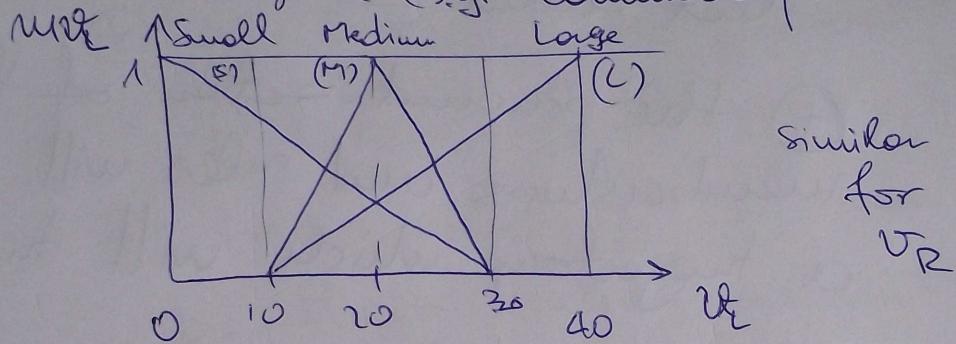
$$\left\{ \begin{array}{l} w_1 = \text{Mid}^{\text{Small}} \cdot \text{M}_0^{\text{Small}} \\ w_2 = \text{Mid}^{\text{Small}} \cdot \text{M}_0^{\text{Large}} \\ w_3 = \text{Mid}^{\text{Large}} \cdot \text{M}_0^{\text{Small}} \\ w_4 = \text{Mid}^{\text{Large}} \cdot \text{M}_0^{\text{Large}} \end{array} \right.$$

2<sup>nd</sup>  
Problem

## Mamdani Fuzzy Controller

- the difference between this and the first problem is that the output is now fuzzy (membership degree) and must be defuzzified considering both components  $[v_L]$  and  $[v_R]$

e.g.: add membership for output signal (e.g. command for robot)



similar  
for  
 $v_R$

Rules become:

- R1: if  $de$  is small and  $\theta_{el}$  is small then  $v_L$  is S &  $v_R$  is S  
 R2: if  $de$  is small and  $\theta_{el}$  is large then  $v_L$  is M &  $v_R$  is L  
 R3: if  $de$  is large and  $\theta_{el}$  is small then  $v_L$  is L &  $v_R$  is M  
 R4: if  $de$  is large and  $\theta_{el}$  is large then  $v_L$  is L &  $v_R$  is L

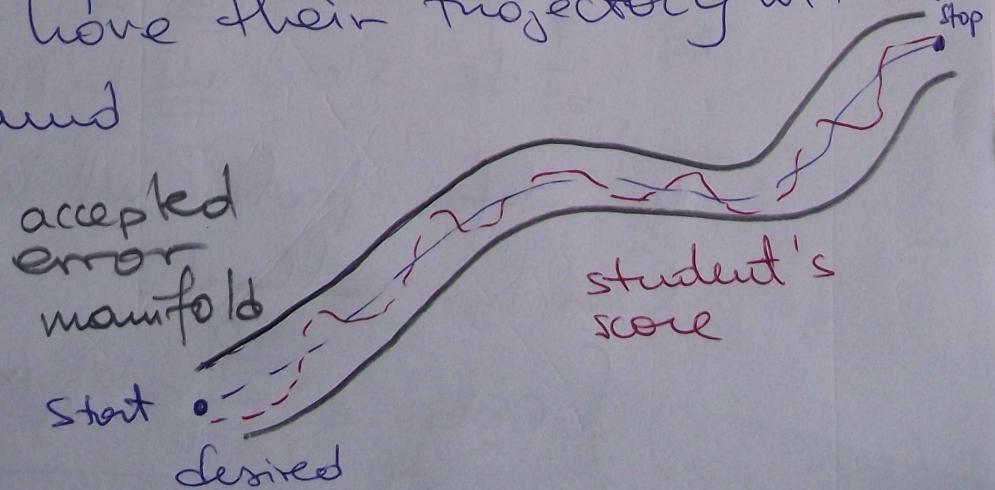
The defuzzification will happen using Center Of -

Gravity method:

$$\left\{ \begin{array}{l} COG_{v_L} = \frac{\sum_{x=0}^{40} M_{v_L}(x) \cdot x}{\sum_{x=0}^{40} M_{v_L}(x)} \\ COG_{v_R} = \frac{\sum_{x=20}^{40} M_{v_R}(x) \cdot x}{\sum_{x=20}^{40} M_{v_R}(x)} \end{array} \right.$$

## Students' tasks:

- ④ choose proper membership functions  
(e.g. shape and number for given bounds of inputs and/or output)
- ④ build the rules as the inputs  $(d_e, \theta_e)$  are given and we mention that output is a P-controller ( $u = [u_i]$ )
- ④ the parametrization of their membership and rules will provide a trajectory which will try to approach the reference.
  - We set a bound of accepted error on the reference and scorers will need to have their trajectory within the bound



## What we provide as support code:

⊕ source file with all the needed tools:

- ⊕ 2/3 membership function types
- ⊕ 1 defuzzification method
- ⊕ robot kinematic model in the control loop.

⊕ rule processing depending on their linking elements  
(e.g. and, or)

⊕ parametrized curves as reference trajectories

